

CHIRAL SU(3) DYNAMICS of the $\bar{K}NN - \pi\Sigma N$ SYSTEM

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- Low-energy QCD with strange quarks
- Important observables and constraints:
 - ▶ $\bar{K}N$ threshold physics
 - ▶ $\pi\Sigma$ mass spectra
- Nature and properties of $\Lambda(1405)$: the two-poles scenario
- $\bar{K}NN$ quasibound systems ? Theory status report

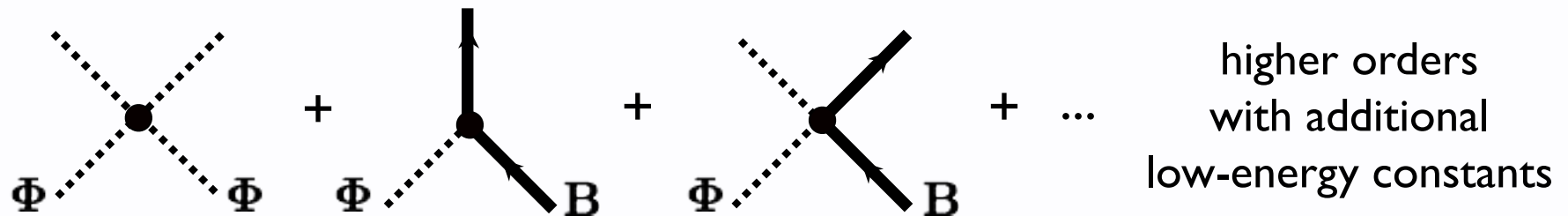


CHIRAL SU(3) EFFECTIVE FIELD THEORY

- Interacting systems of **NAMBU-GOLDSTONE BOSONS** (**pions, kaons**) coupled to **BARYONS**

$$\mathcal{L}_{eff} = \mathcal{L}_{mesons}(\Phi) + \mathcal{L}_B(\Phi, \Psi_B)$$

- Leading **DERIVATIVE** couplings (involving $\partial^\mu \Phi$) determined by spontaneously broken **CHIRAL SYMMETRY**



- Low-Energy Expansion: **CHIRAL PERTURBATION THEORY**

“small parameter”:

$$\frac{p}{4\pi f_\pi} \sim \frac{\text{energy / momentum}}{1 \text{ GeV}}$$

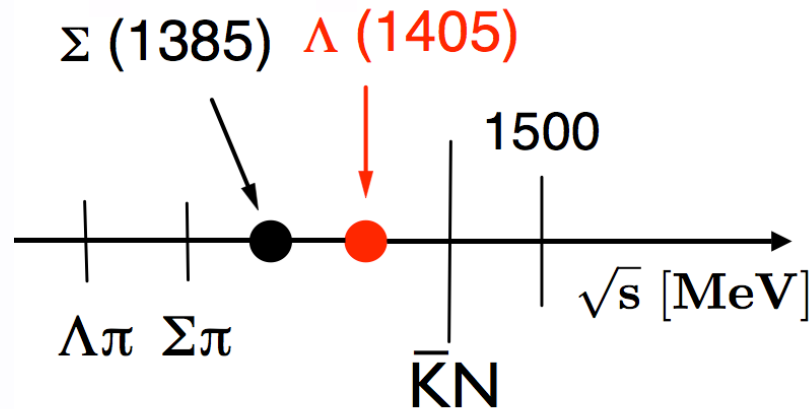
- works well for low-energy **pion-pion** and **pion-nucleon** interactions

► ... but **NOT** for systems with **strangeness** $S = -1$ ($\bar{K}N$, $\pi\Sigma$, ...)



Low-Energy $\bar{K} N$ Interactions

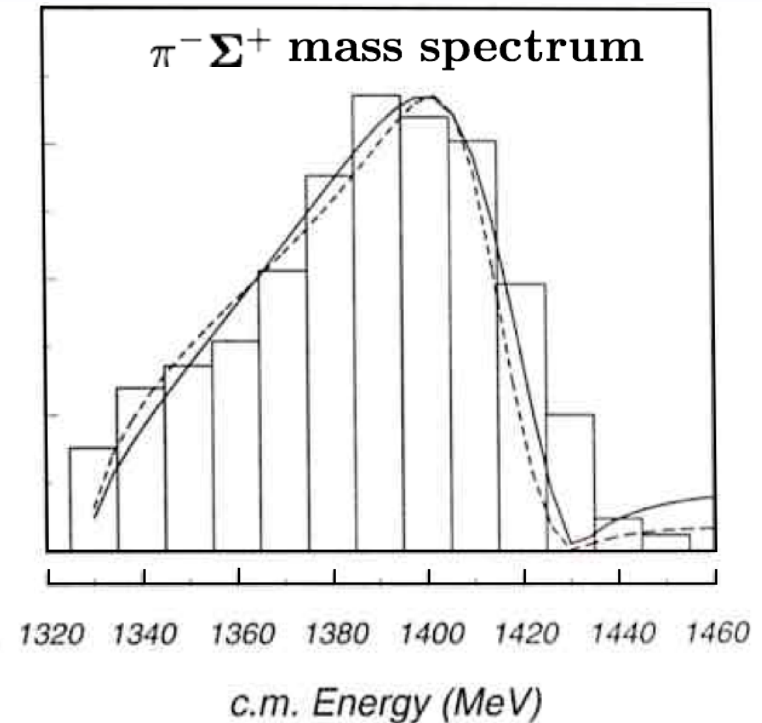
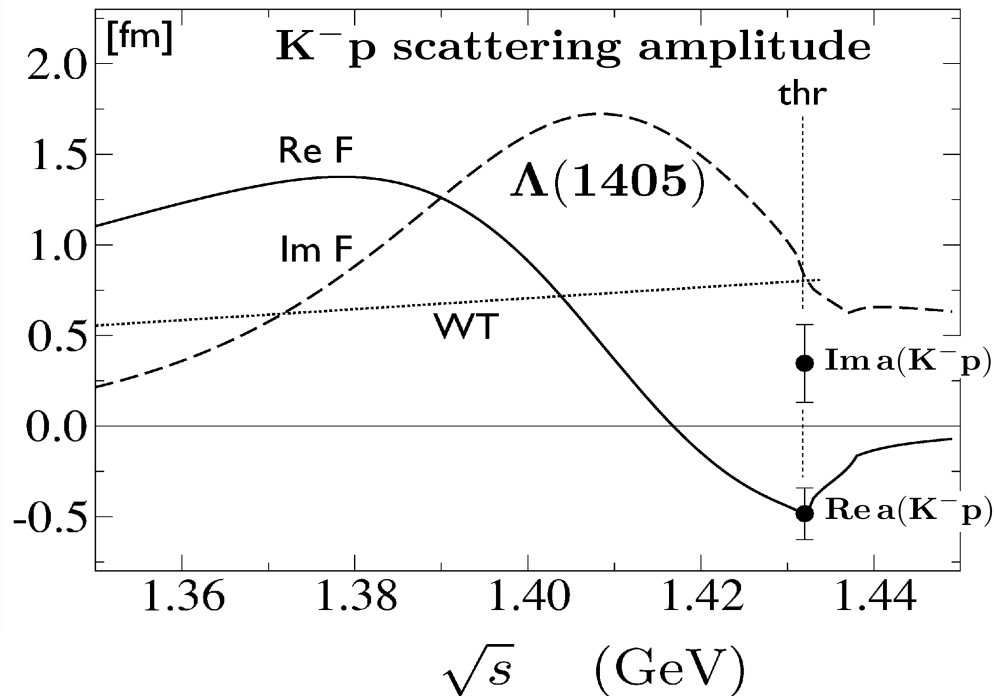
- Chiral Perturbation Theory **NOT** applicable: $\Lambda(1405)$ just below K^-p threshold



Non-perturbative
Coupled Channels
approach based on
Chiral SU(3) Dynamics

N. Kaiser, P. Siegel, W.W. (1995)

E. Oset, A. Ramos (1998)

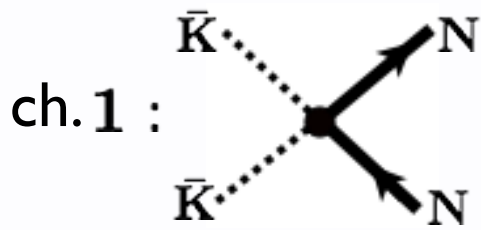


CHIRAL SU(3) COUPLED CHANNELS DYNAMICS

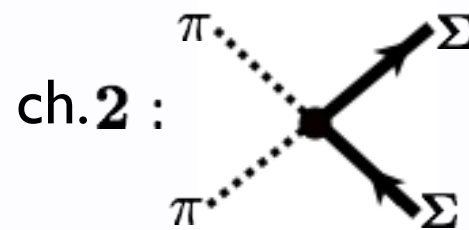
$$T_{ij} = K_{ij} + \sum_n K_{in} G_n T_{nj}$$

- Leading s-wave $l = 0$ meson-baryon interactions (Weinberg-Tomozawa)

Note: **ENERGY DEPENDENCE** characteristic of Nambu-Goldstone Bosons



$$K_{11} = \frac{3}{2f^2}(\sqrt{s} - M_N)$$



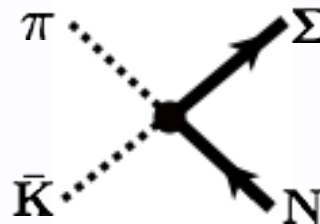
$$K_{22} = \frac{2}{f^2}(\sqrt{s} - M_\Sigma)$$

strong enough to produce

▶ **$\bar{K}N$ bound state**

▶ **$\pi\Sigma$ resonance**

strong
channel coupling
 $12 \leftrightarrow 21$:



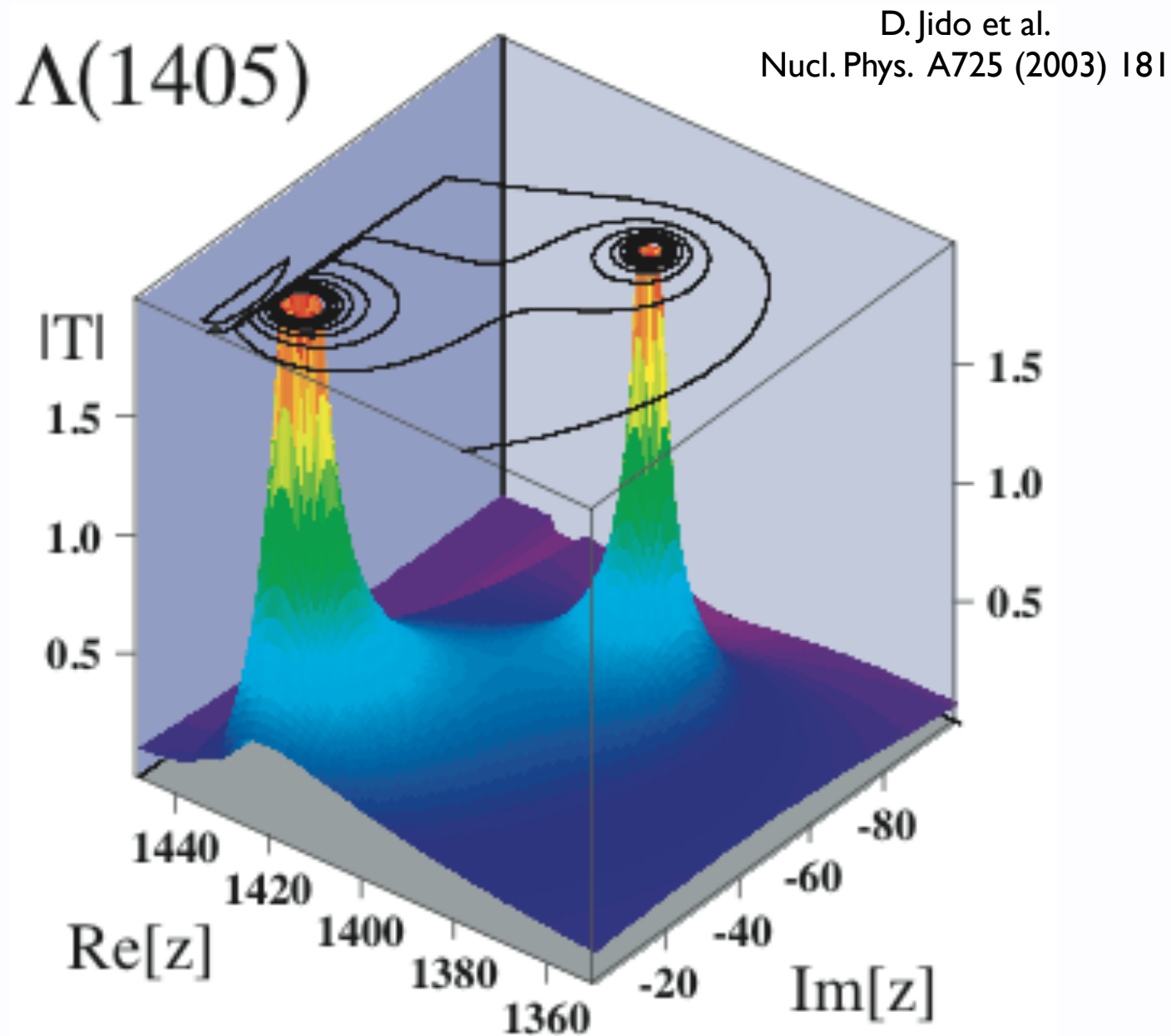
$$K_{12} = \frac{-1}{2f^2} \sqrt{\frac{3}{2}} \left(\sqrt{s} - \frac{M_N + M_\Sigma}{2} \right)$$

- Dynamical generation of $\Lambda(1405)$ as **quasi-bound $\bar{K}N$ ($l = 0$) state**

early history: R.H. Dalitz et al. (1967)



The TWO POLES scenario



The TWO POLES scenario

T. Hyodo, W.W., Phys. Rev. C77 (2008) 03524

- Singularities of $\bar{K}N$ amplitude in the complex energy plane

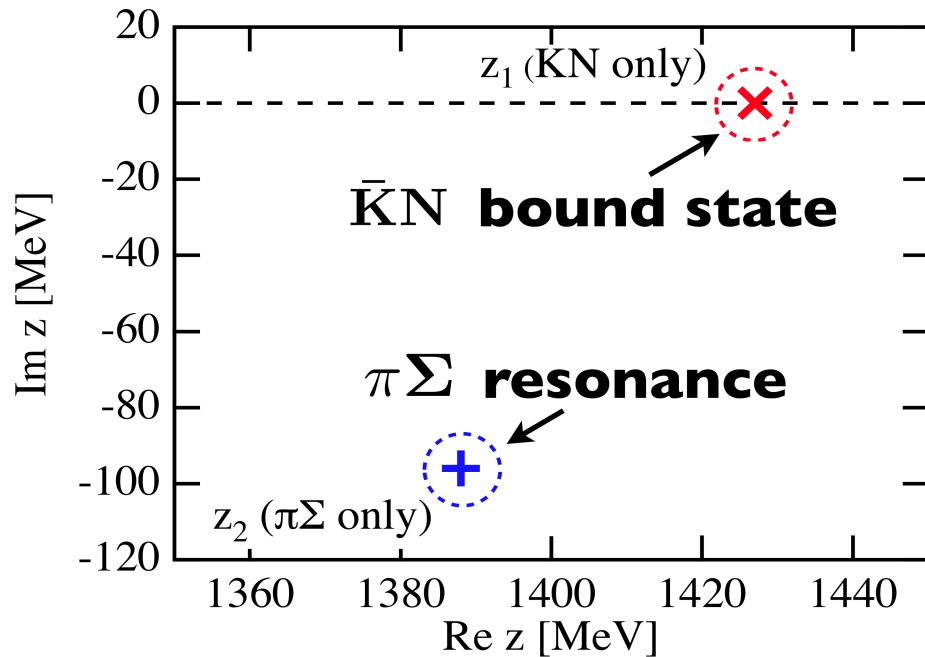
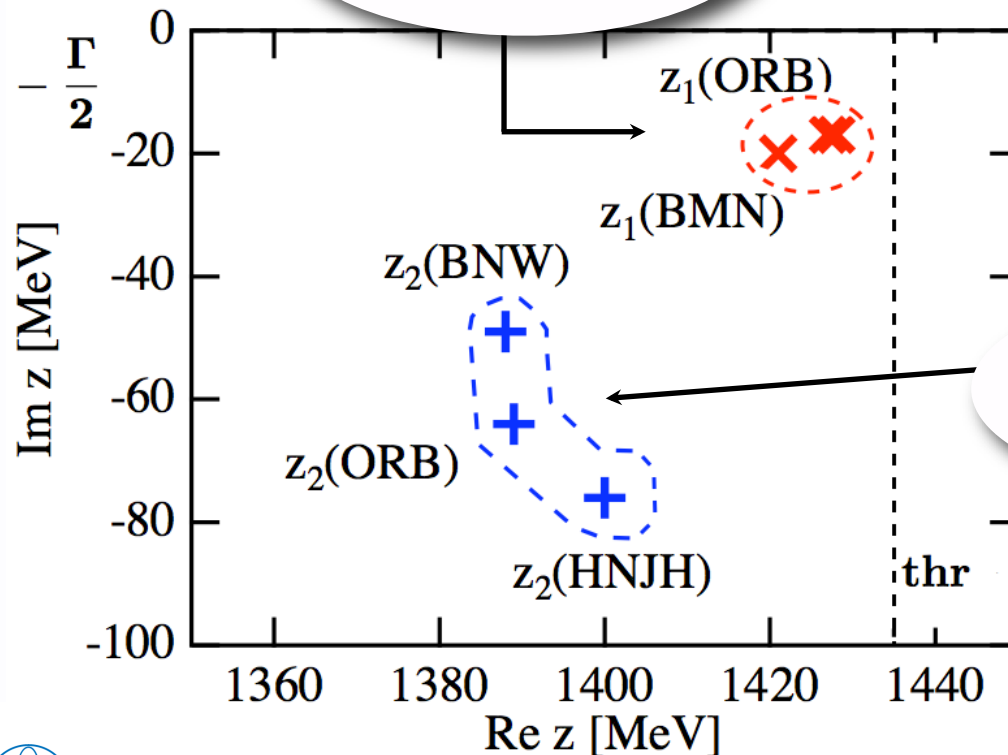
starting point:

no channel coupling



Pole I

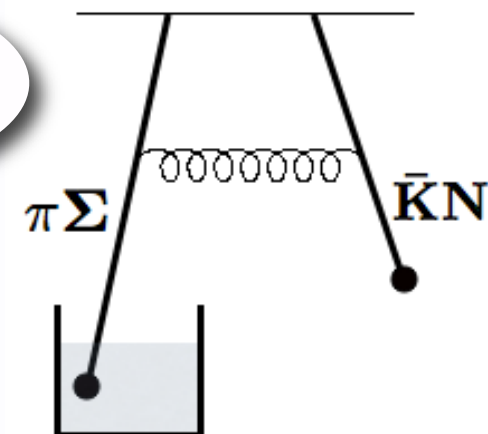
(dominantly $\bar{K}N$)



channel coupling at work

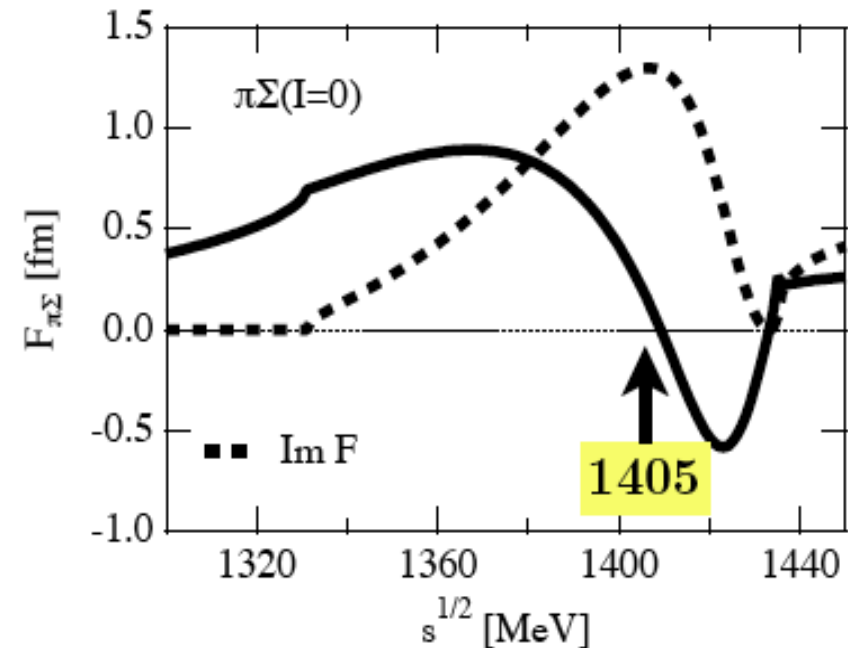
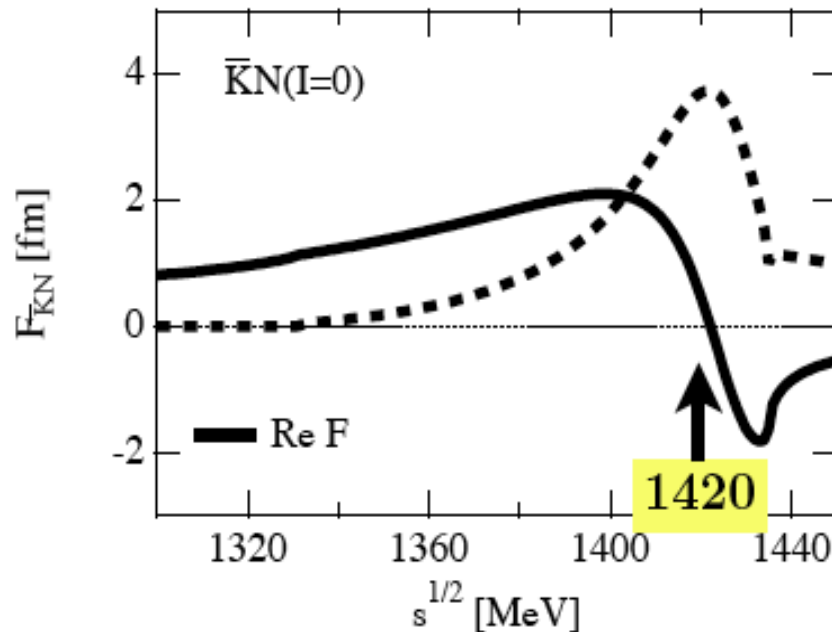
Pole II

(dominantly $\pi\Sigma$)



The TWO POLES scenario (contd.)

- $\bar{K}N$ and $\pi\Sigma$ amplitudes



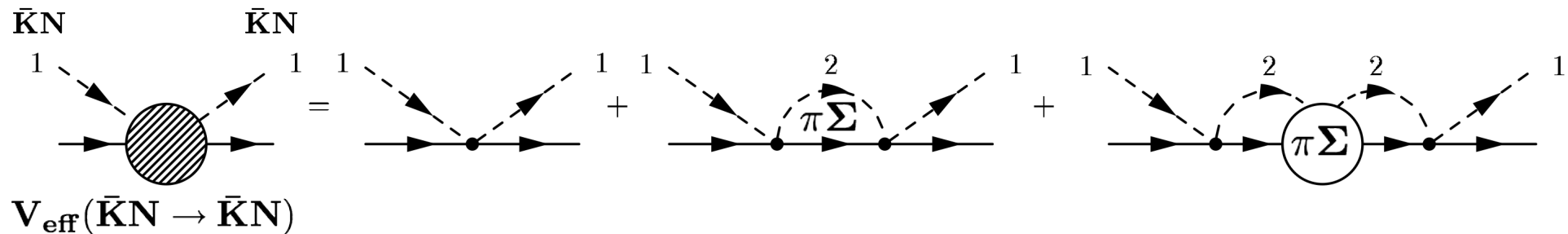
- **Note difference** in pole positions and spectra of $\bar{K}N$ and $\pi\Sigma$

D. Jido et al., NPA725 (2003) 263

- Equivalent $\bar{K}N$ **effective interaction** should produce quasibound state at **1420 MeV (not 1405 MeV)**

$I = 0 \quad \bar{K}N \quad \text{Effective Interaction}$

T. Hyodo, W.W.: Phys. Rev. C 77 (2008) 03524

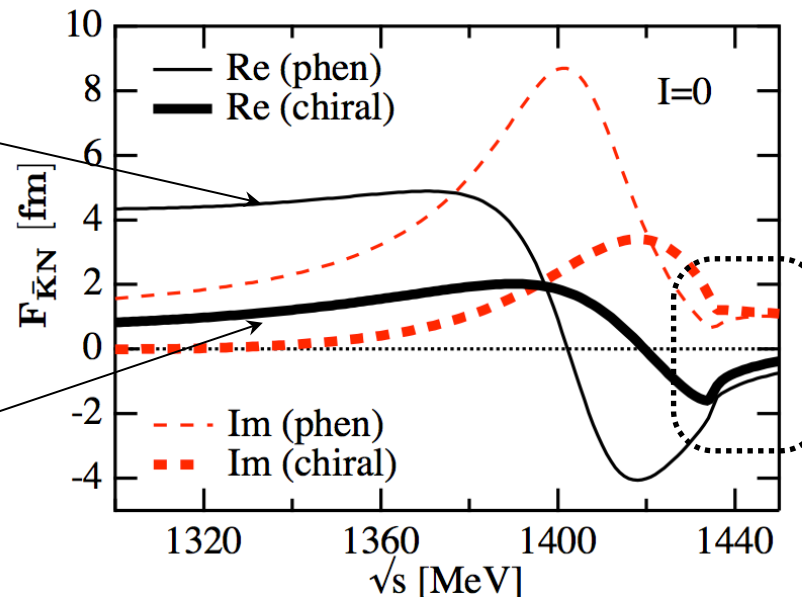


$V_{\text{eff}}(\bar{K}N \rightarrow \bar{K}N)$ is:

- **complex**
- **energy dependent**
- **non-local**

Akaishi-Yamazaki
phenom.
potential

chiral
SU(3)
dynamics

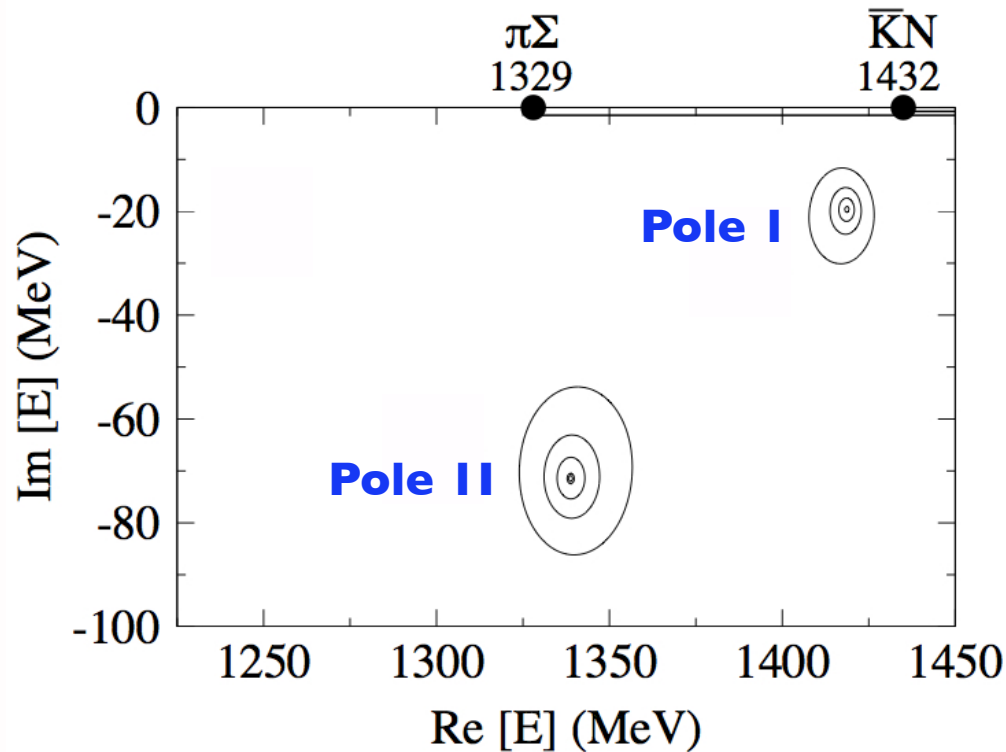


large differences
in
subthreshold
extrapolations

- **Chiral dynamics** predicts significantly **weaker attraction** than Akaishi - Yamazaki (local, energy independent) potential



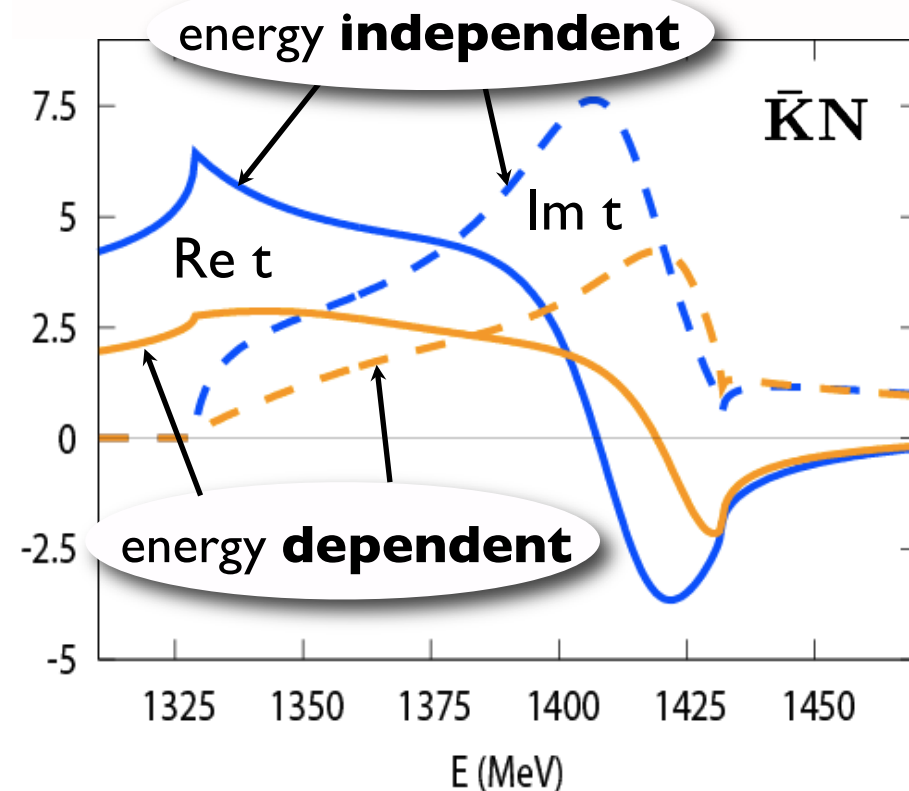
The TWO POLES scenario (contd.)



- Note: **NO** differences at and above $\bar{K}N$ threshold
- But: **STRONG** differences for subthreshold extrapolations

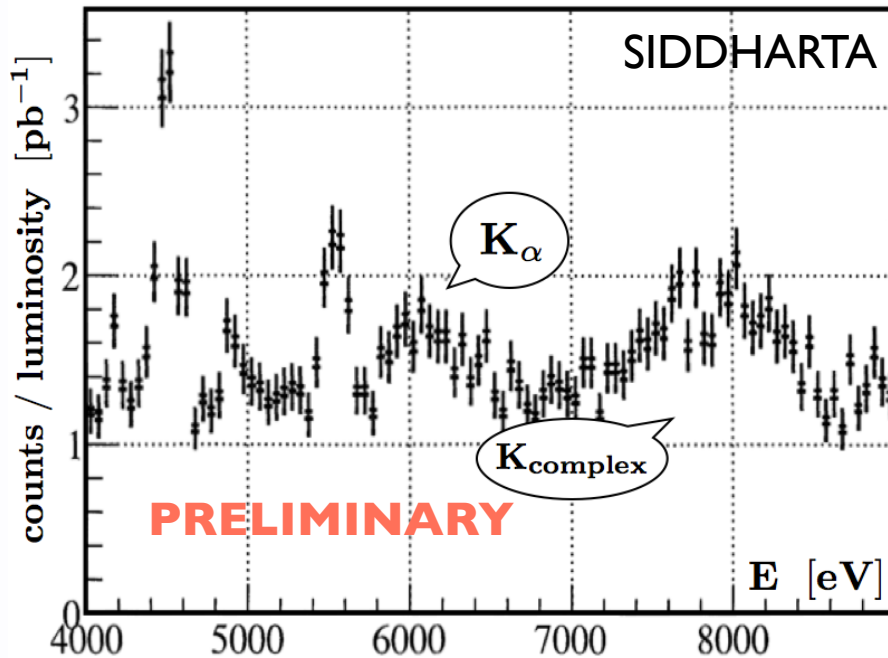
Y. Ikeda, H. Kamano, T. Sato
arXiv:1004.4877 [nucl-th]

- Two-pole scenario confirmed
- Role of **energy dependent** (chiral) driving interactions



NEWS from SIDDHARTA

- New **kaonic hydrogen** precision data (2010)



- note:
remarkable agreement with
Tomozawa-Weinberg
(leading order) prediction
from chiral SU(3) dynamics

- fine-tuning in progress
T. Hyodo, Y. Ikeda, W.W. (2010)

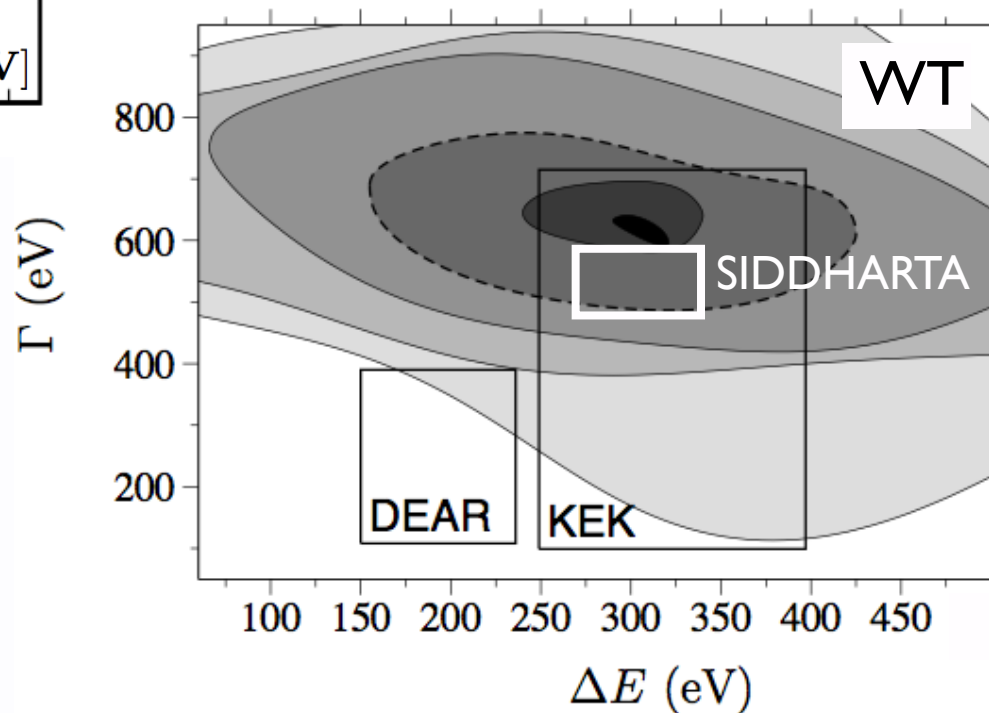
- strong interaction shift and width:
(preliminary)

$$\Delta E = 305 \pm 31 \text{ eV}$$

$$\Gamma = 512 \pm 77 \text{ eV}$$

B. Borasoy, R. Nissler, W.W.
Eur. Phys. J. A25 (2005) 79

R. Nissler
PhD thesis (2008)



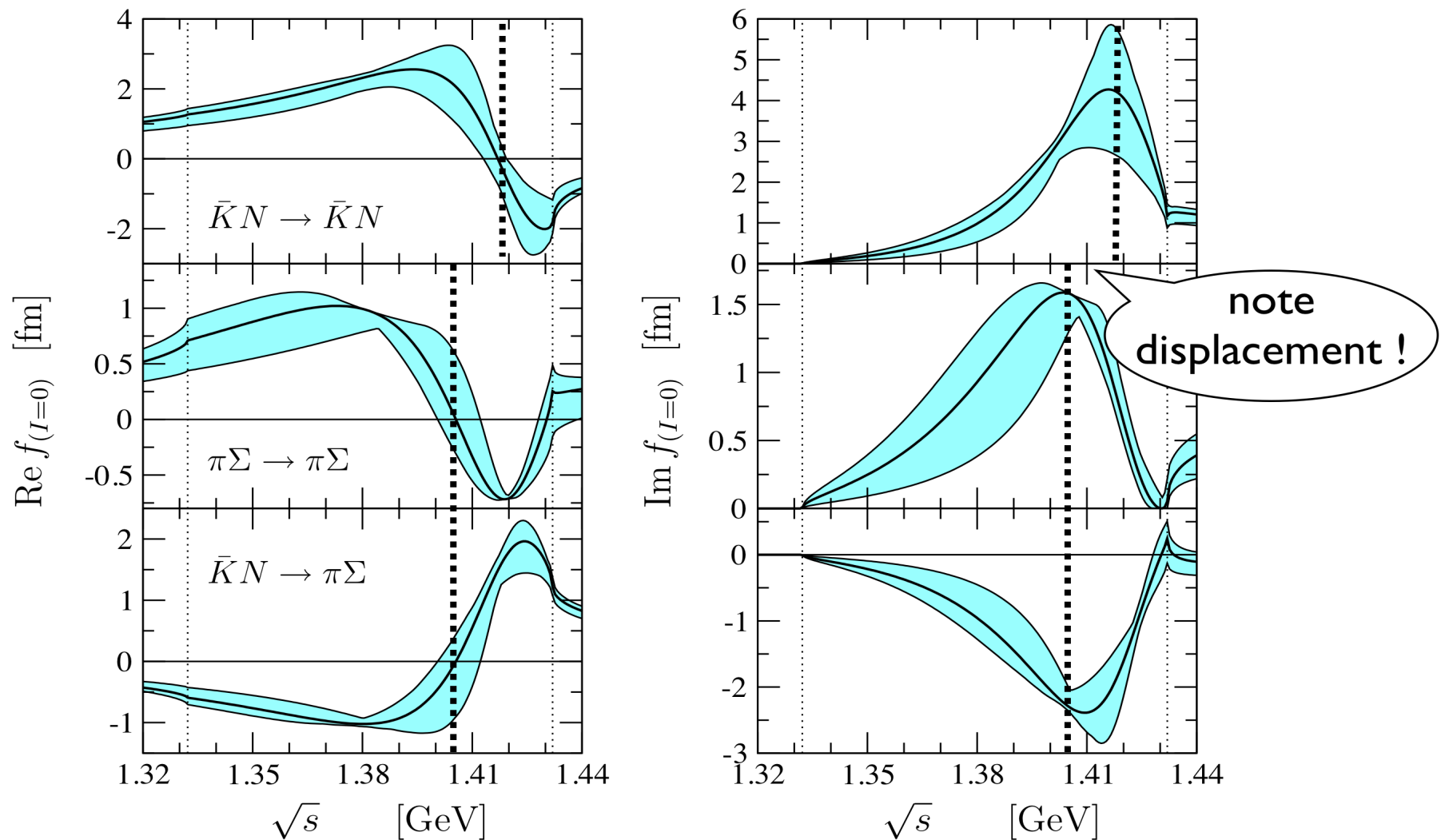
Chiral SU(3) Coupled Channels Dynamics

- Relevant amplitudes, subthreshold extrapolations and uncertainty analysis

R. Nissler PhD thesis (2008)

B. Borasoy, R. Nissler, W.W.: Eur. Phys. J. A25 (2005) 79

B. Borasoy, U.-G. Meissner, R. Nissler, Phys. Rev. C74 (2006) 055201



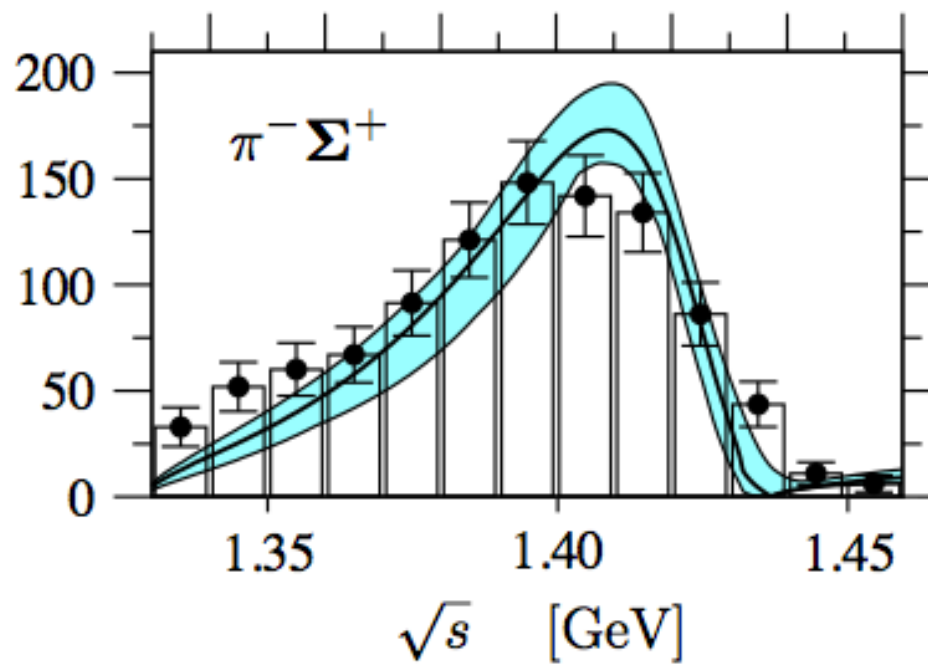
- reduction of uncertainties expected in view of new SIDDHARTA data



$\pi\Sigma$ MASS SPECTRA

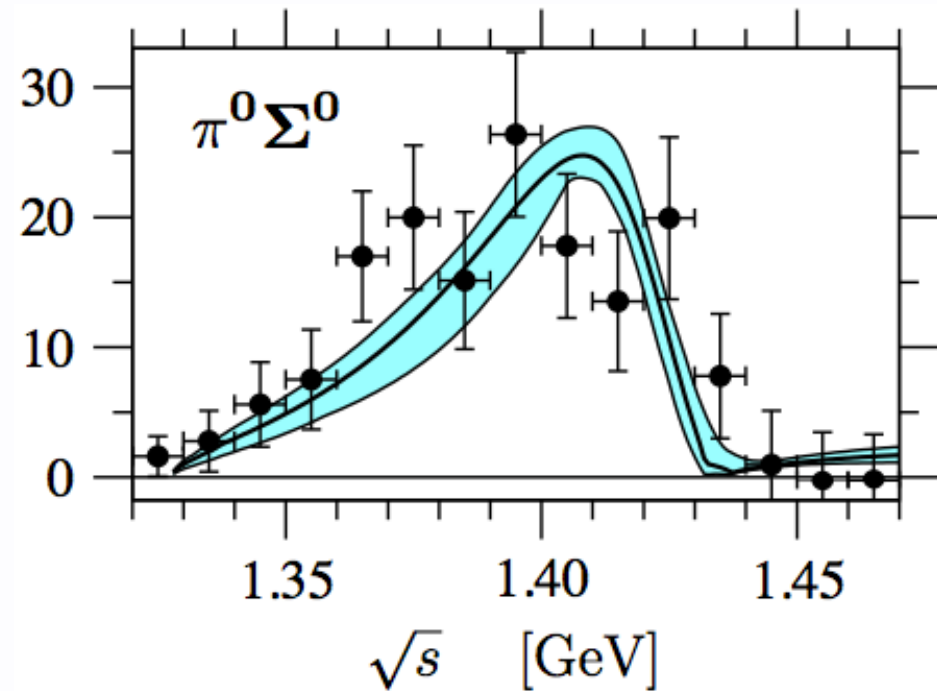
- Chiral SU(3) dynamics with uncertainty analysis

R. Nissler, PhD thesis (2008)



“old” data

R.J. Hemingway,
Nucl. Phys. B253 (1985) 742



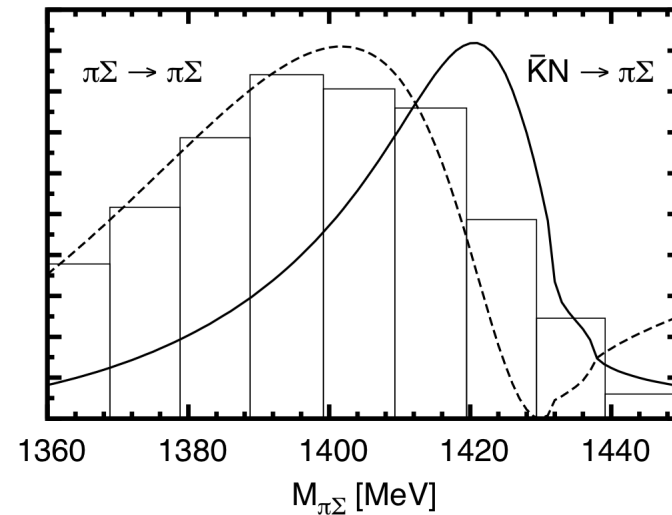
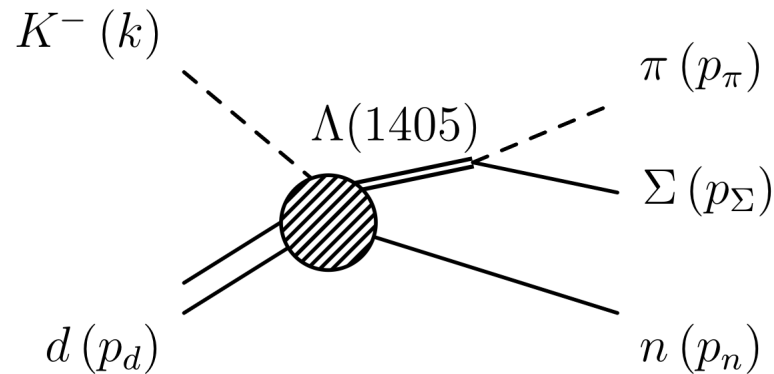
ANKE data (COSY / Jülich)

I. Zychor et al.
Phys. Lett. B660 (2008) 167

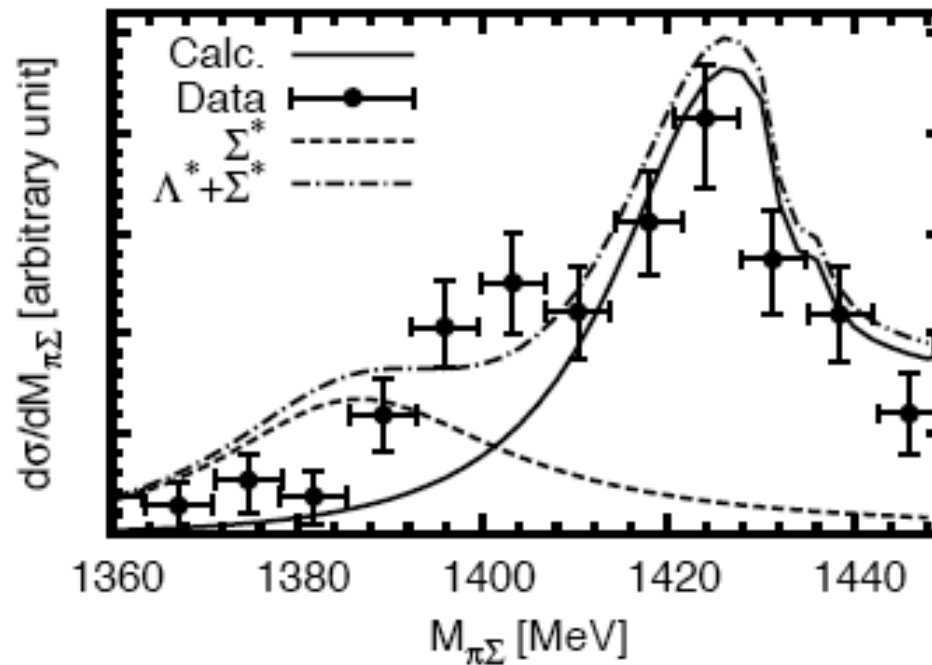


$\pi\Sigma$ MASS SPECTRA (contd.)

- Kaonic (in-flight) production of $\Lambda(1405)$ from deuterium



Two-Pole scenario



D. Jido, E. Oset, T. Sekihara
Eur. Phys. J. A42 (2009) 268

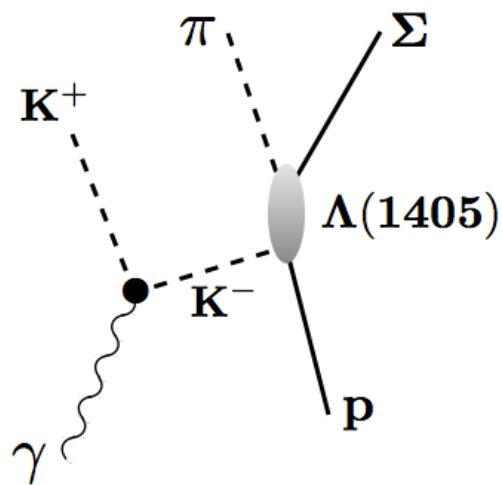
exp. data:
O. Braun et al.
Nucl. Phys. B129 (1977) 1



$\pi\Sigma$ MASS SPECTRA (contd.)

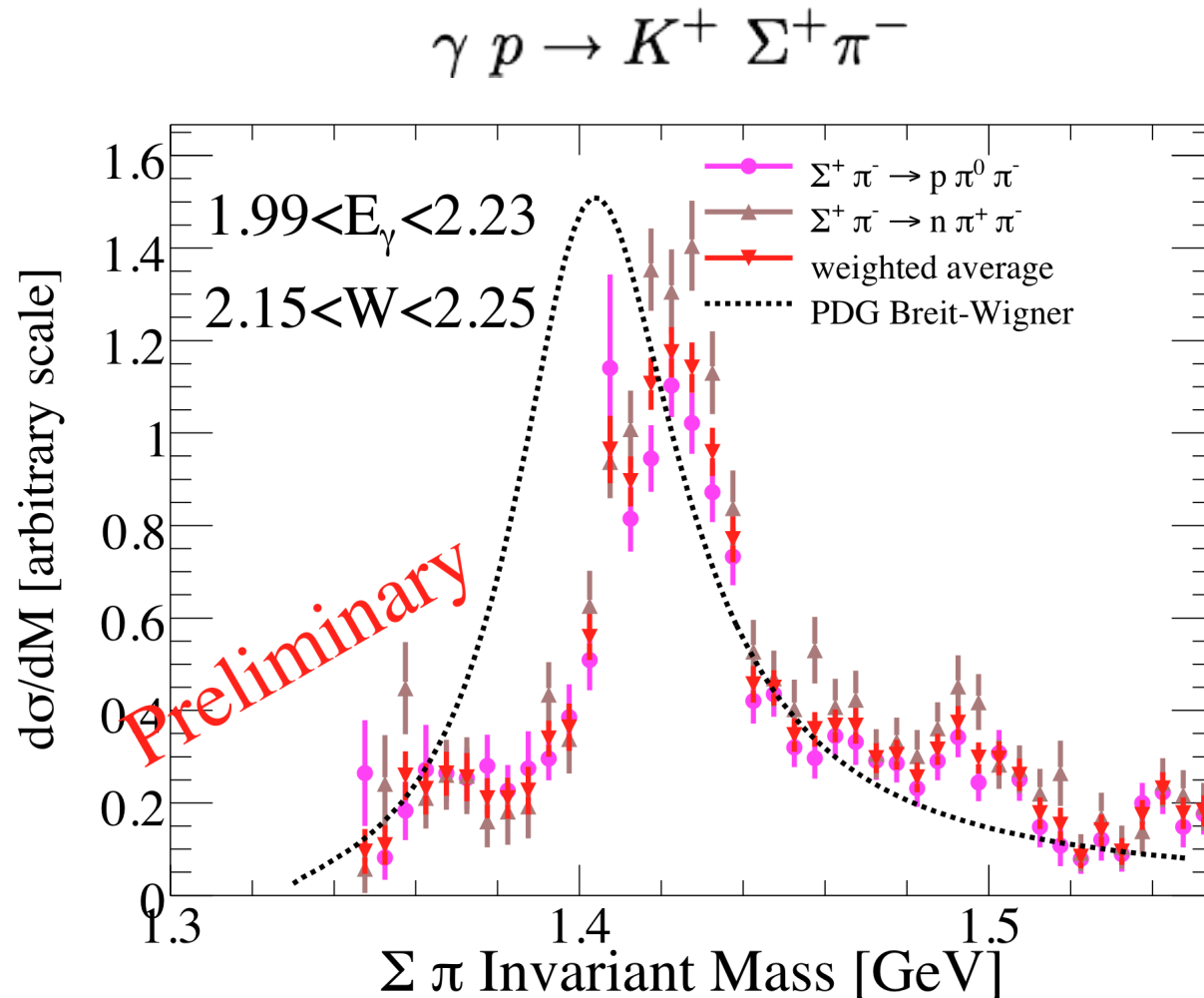
● Photoproduction of $\Lambda(1405)$

(CLAS @ JLAB)



K. Moriya, R. Schumacher
HYP-X Conference (2009)
Nucl. Phys.A 835 (2010) 231

K. Moriya, NFQCD
Kyoto (2010)

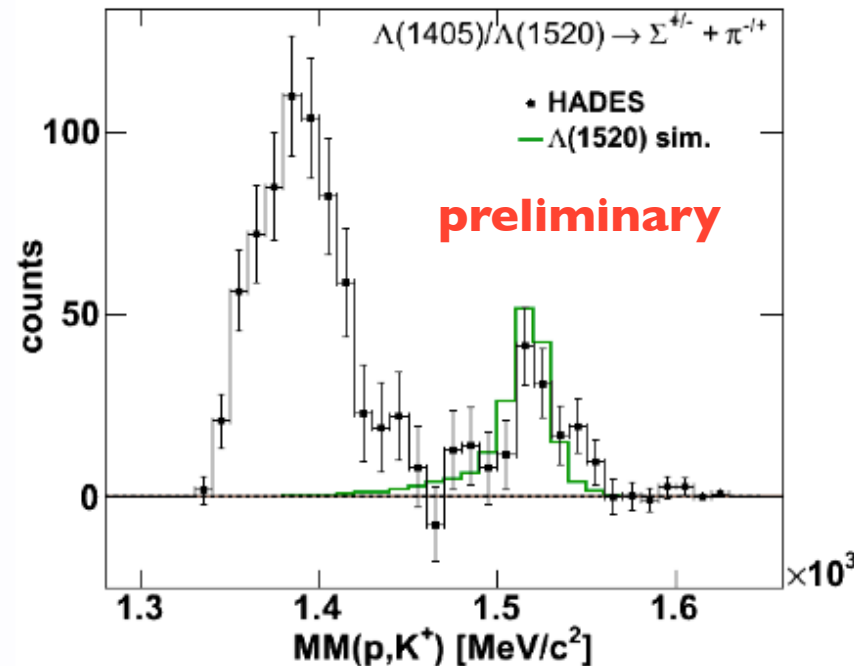


● Note: shift of $\Lambda(1405)$ spectrum as compared to “standard” PDG listing

$\pi\Sigma$ MASS SPECTRA (contd.)

- News from HADES

$$pp \rightarrow pK^+ \{\pi^\pm \Sigma^\mp\}$$

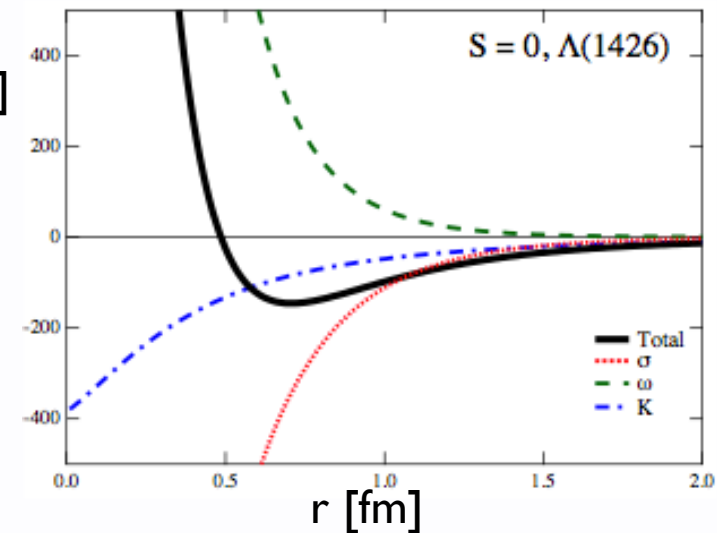


L. Fabbietti,
E. Eppe, J. Siebensohn,
et al. (2010)

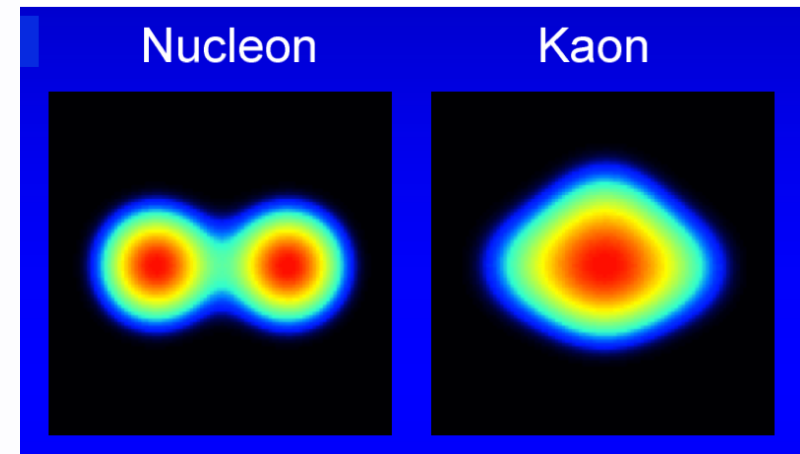
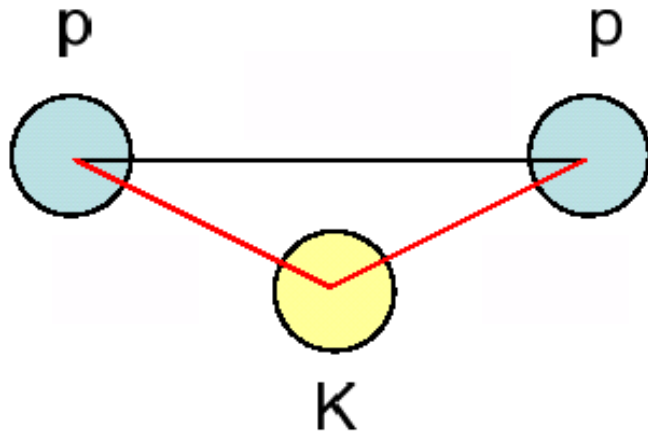
- Downward shift of $\Lambda(1405)$ by final state interactions ?
- hint:
model calculation of $\Lambda^* N$ potential based on chiral SU(3) coupled channels and boson exchange

T. Hyodo, T. Uchino, M. Oka (2010)

[MeV]



Prototype Antikaon-Nuclear Few-Body System: K^-pp



- **3-Body (Faddeev) Calculations**
- **Variational Calculations**
- **Issues** in both approaches:
energy dependence of basic input amplitudes,
subthreshold / off-shell extrapolations, necessary approximations, ...



OVERVIEW

- Binding energies and widths of quasibound $\{\bar{K}[\text{NN}]_{T=1}\}_{I=1/2}$

Variational

B [MeV]	Γ	two-body input:
48	61	phenomenological potential (energy independent) [1]
20 ± 3	40 – 70	chiral SU(3) dynamics [2]
40 – 80	40 – 85	coupled channels phenomenological (incl. p wave) [3]

[1] T.Yamazaki, Y.Akaishi
Phys. Lett. B535 (2002) 70
Phys. Rev. C76 (2007) 045201

[2] A. Doté, T. Hyodo, W.W.
Nucl. Phys. A804 (2008) 197
Phys. Rev. C79 (2009) 014003

[3] S.Wycech, A.M. Green
Phys. Rev. C79 (2009) 014001

Faddeev

B [MeV]	Γ	3-body coupled channels two-body input:
50 – 70	90 – 110	phenomenological [4]
45 – 80	45 – 70	(energy independent) [5]
$14^{*})$	$58^{*})$	chiral SU(3) dynamics (energy dependent) [6] *) KbarNN pole position

[4] N.V. Shevchenko, A. Gal, J. Mares
Phys. Rev. Lett. 98 (2007) 082301
(+ J. Révay)
Phys. Rev. C76 (2007) 044004

[5] Y. Ikeda, T. Sato
Phys. Rev. C76 (2007) 035203
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[6] Y. Ikeda, H. Kamano, T. Sato
arXiv:1004.4877 [nucl-th] (2010)



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OVERVIEW

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Phys. Lett. B535 (2002) 70
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$14^{*})$	$58^{*})$	chiral SU(3) dynamics [6] (energy dependent) $^{*})$ $\bar{K}$ barNN pole position

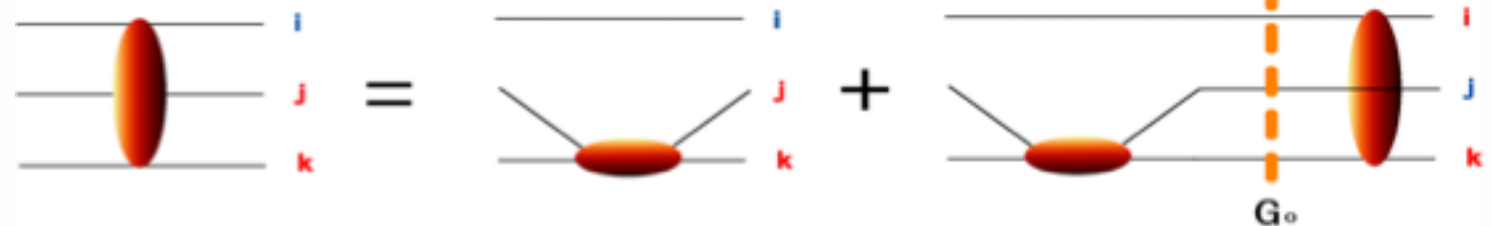
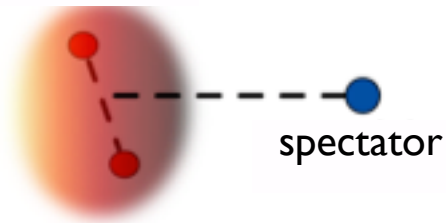


K⁻pp System: Coupled-Channels Faddeev Approach

(contd.)

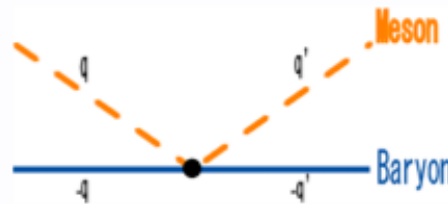
Y. Ikeda, H. Kamano, T. Sato: arXiv:1004.4877 [nucl-th]

interacting
pair



- Recent advanced calculation:
Importance of full, **energy dependent** $\bar{K}N$ and $\pi\Sigma$ interactions

based on



chiral SU(3) dynamics

$$V_{MB}(q', q) = -4\pi\lambda_{\alpha\beta}^{(I)} \frac{1}{(2\pi)^3} \frac{1}{8F_\pi^2} \frac{1}{\sqrt{\omega'\omega}} \frac{\omega' + \omega + E'_B + E_B - M' - M}{2}$$

► **Two-pole structure** also seen in **3-body** amplitude



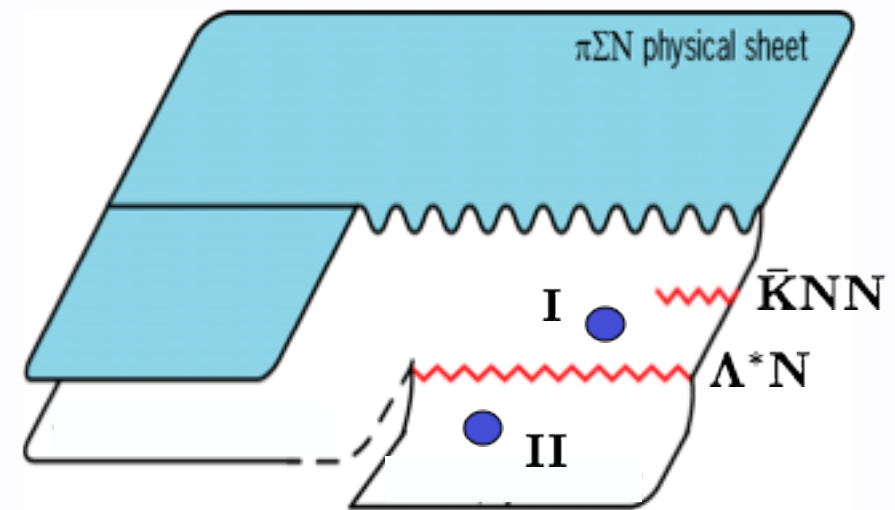
K⁻pp System: Coupled-Channels Faddeev Approach

(contd.)

Y. Ikeda, H. Kamano, T. Sato

arXiv:1004.4877 [nucl-th]

- Search for **3-body resonances** on $\bar{K}NN$ physical sheet
- **Energy dependent** interactions
 - ▶ **two poles** in 3-body amplitude



	pole I	pole II	
$\bar{K}$ - and N -exchanges	$-14.5 - i28.7$	$-36.7 - i109.3$	
$\bar{K}$ -, N - and π -exchanges	$-13.6 - i27.8$	$-45.8 - i104.0$	
Full	$-13.7 - i29.0$	$-37.2 - i93.3$	[MeV]

▶ implications for spectral functions ?

▶ **weak binding**



Summary

- **Low-Energy QCD:**
spontaneous chiral symmetry breaking scenario well established
 - ▶ **Chiral $SU(3) \times SU(3)$ Effective Field Theory :**
Successful framework for low-energy hadron physics with s-quarks
 - ▶ Structure of $\Lambda(1405)$ governed by (chiral) $SU(3)$ coupled-channels dynamics and two-poles scenario
- **Antikaons** in interaction: **$\bar{K}NN$ quasibound** systems ?
 - ▶ Extrapolations to **far-subthreshold** region still an issue
 - ▶ **Weak binding** + large width from chiral $SU(3)$ dynamics
 - ▶ DISTO and FINUDA signals are **not** understood in terms of deeply bound $\bar{K}NN$ states ($\rightarrow \pi YN$ dynamics ?)
 - ▶ needed:
high-precision **$\bar{K}N$ threshold data**
much improved **$\pi\Sigma$ mass spectra**

answers in sight: SIDDHARTA ... J-PARC, AMADEUS, GSI

