Lecture 1: Basics, hard scattering processes in nuclei

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#### Cronin effect: a "case study"

#### An early measurement

Cronin *et al,* Phys. Rev. D11 (1975) 3105

- Inclusive invariant cross-section for π<sup>-</sup> production as a function of p<sub>T</sub>
  - -At 90° in center of mass
  - -For three different fixed target collision energies
    - ⇒Clear variation in yield at high p<sub>T</sub> with collision energy.



#### **Some basics**

 First, center of mass energies:  $-200 \text{ Gev} \rightarrow \sqrt{s} = 19.4 \text{ GeV}$  $-300 \text{ Gev} \rightarrow \sqrt{s} = 23.7 \text{ GeV}$  $-400 \text{ Gev} \rightarrow \sqrt{s} = 27.4 \text{ GeV}$  Kinematic limits: -At nucleon-nucleon level single particle p<sub>T</sub> must satisfy  $p_T < \sqrt{s}/2$ ⇒ 12.0, 13.9, 15.6 GeV Invariant cross-section  $-E d^3 p$  is Lorentz invariant



#### Early measurement: x<sub>T</sub>

 Define a scaling variable:  $-x_\perp = p_T/(\sqrt{s}/2)$ -Measurements extend to significant fraction of kinematic limit. Shapes of x<sub>T</sub> spectra between different energies are similar. -But have different normalization.  $\Rightarrow$ Correct for  $\sqrt{s}$  in  $p_T \rightarrow x_\perp$ transformation



#### **XT scaling**

#### High-p<sub>T</sub> invariant cross-sections have power-law shape:

$$- E rac{d^3\sigma}{dp^3} \propto \left(rac{1}{p_T}
ight)^n$$



• Then, under  $p_T \rightarrow x_{\perp}$ pick up factor of  $\left(\frac{1}{\sqrt{s}}\right)^n$ 



#### A dependence

• Cross-sections were observed to vary (inclusively) as  $A^{\alpha}$ .



FIG. 1. The invariant cross section for  $\pi$  production relative to tungsten for various atomic numbers at 400 GeV; (a)  $\pi^-$  at  $p_{\perp} = 3.85 \text{ GeV}/c$ , (b)  $\pi^+$  at  $p_{\perp} = 3.85 \text{ GeV}/c$ (c)  $\pi^-$  at  $p_{\perp} = 5.38 \text{ GeV}/c$ , (d)  $\pi^+$  at  $p_{\perp} = 5.38 \text{ GeV}/c$ .

# A dependence

 Extracted values of  $\alpha(\mathbf{p}_{\mathsf{T}})$  for pions, kaons and protons.  $-0.9 < \alpha(pT) < 1.1$ for pions  $\Rightarrow$ Surprise:  $\alpha > 1$  $\Rightarrow$  Varies with particle type This is the wellknown "Cronin effect" ⇒Why?



## **Physics: pQCD, geometry**

# Hard Scattering in p-p Collisions





From Collins, Soper, Sterman Phys. Lett. B438:184-192, 1998 **STAR** p-p di-jet Event

$$\sigma_{AB} = \sum_{ab} \int dx_a dx_b \,\phi_{a/A}(x_a,\mu^2) \,\phi_{b/B}(x_b,\mu^2) \,\hat{\sigma}_{ab} \left(\frac{Q^2}{x_a x_b s},\frac{Q}{\mu},\alpha_s(\mu)\right) \,\left(1 + \mathcal{O}\left(\frac{1}{Q^P}\right)\right)$$

Factorization: separation of σ into

 Short-distance physics: σ̂
 Long-distance physics: φ's (universal)

# **Single High-pt Hadron Production**

 For single hadron production need fragmentation functions

 Describe inclusive hadron longitudinal momentum distribution inside a jet

 $\Rightarrow D_i^a(z)$  for parton  $i \rightarrow$  hadron a

⇒z is fraction of parton/jet momentum carried by the hadron

Fragmentation functions satisfy sum rule

$$-\sum_{a}\int_{0}^{1}dz\,zD_{i}^{a}(z)=1$$



- •Starting point, nuclear nucleon density distribution:  $\rho(r)$
- •Then, assuming straight-line trajectory at impact parameter b,



- electron or proton passes through "thickness"
  - $T(b)=\int_{-\infty}^\infty dz\,
    ho(\sqrt{b^2+z^2})$
- T(b) has dimensions 1/L<sup>2</sup>
   ⇒ T(b) x cross-section = number of scatterings

 Then, e.g. produce high-p<sub>T</sub> hadrons in p-A collisions at rate/event:

$$\overline{\phantom{a}} E \, rac{d^3 n^{pA(b)}}{dp^3} = T(b) imes E \, rac{d^3 \sigma^{pp}}{dp^3}$$

•With a corresponding differential crosssection per impact parameter:

$$- E rac{d\sigma^{pA}}{db \, d^3 p} = 2\pi b \left( E \, rac{d^3 n^{pA(b)}}{dp^3} 
ight) = 2\pi b \left( T(b) imes E \, rac{d^3 \sigma^{pp}}{dp^3} 
ight)$$

#### Integrate over b:

$$- E rac{d \sigma^{pA}}{d^3 p} = \int db \; 2 \pi b T(b) \; imes E \, rac{d^3 \sigma^{pp}}{d p^3}$$

#### •But,

 $-\int db \ 2\pi bT(b) = \int db dz \ 2\pi b\rho(\sqrt{b^2 + z^2}) = \int d^3 r \rho(r) = A$ • So,  $-E \frac{d\sigma^{pA}}{d^3 p} = A \times E \frac{d^3 \sigma^{pp}}{dp^3}$ 

You'll sometimes here that this result depends on small p-p cross-section ⇒ complete nonsense!
In principle, can have a total hard scattering rate/event n<sup>pA(b)</sup> = T(b)σ<sup>pp</sup> that is > ~ 1 ⇒ especially in p+Pb @ LHC

# •So what assumptions did we make in:

$$E\,rac{d^3n^{pA(b)}}{dp^3}=T(b) imes E\,rac{d^3\sigma^{pp}}{dp^3}$$



-That *\phi***'s**, *D***'s** are the same when colliding with proton and nucleus

-That  $\phi$ 's, D's are the same everywhere along the path (z) of the proton through the nucleus.

⇒Universality

- -That multiple hard scatterings are incoherent
- That the hard scattering occurs over a small transverse distance.
- -That T(b) is constant over transverse size of p 15

# •Why is there no knowledge of the finite (transverse) size of the proton in

$$\sigma_{AB} = \sum_{ab} \int dx_a dx_b \,\phi_{a/A}(x_a,\mu^2) \,\phi_{b/B}(x_b,\mu^2) \,\hat{\sigma}_{ab} \left(\frac{Q^2}{x_a x_b s},\frac{Q}{\mu},\alpha_s(\mu)\right) \,\left(1 + \mathcal{O}\left(\frac{1}{Q^P}\right)\right)$$

- Suppose we consider some spatial distribution of partons in proton: η(z, r<sub>T</sub>)
  - -longitudinal physics complicated but it's the transverse part of the problem that matters
- Define proton thickness

 $\int_{-\infty}^{\infty} dz \, \eta(\sqrt{r_T^2+z^2})$ 

 Consider proton-proton collision in transverse plane.

- Consider two partons at transverse positions relative to proton centers of  $\vec{r_{T1}}$  and  $\vec{r_{T2}}$
- •Separated by a distance  $\vec{\Delta r}$

 $\vec{\Delta r} = \vec{b} + \vec{r_{T2}} - \vec{r_{T1}}$ 



•Write differential cross-section for scattering between the two partons  $= d^2\sigma/d\vec{\Delta r}^2$ 

•Then,  $\sigma^{pp}_{hard} = \int d^2b \int d^2r_{T1} \int d^2r_{T2} t(r_{T1})t(r_{T2}) rac{d^2\sigma}{d \Delta \vec{r}_{A2}^2}$ 

 But, large momentum transfer scattering occurs over small transverse distance

$$\Rightarrow rac{d^2\sigma}{dec{\Delta r}^2} \propto \delta^2(ec{\Delta r})$$

#### Then,

 $- \sigma^{pp}_{hard} 
ightarrow \int d^2 r_{T1} \int d^2 r_{T2} \, t(r_{T1}) t(r_{T2}) 
ightarrow n_1 imes n_2$ 

- Of course neglects all QM, kinematics, etc
   ⇒But gets the essence of the transverse physics right.
- So, what happens in p+A collisions? – In principle, replace:  $\eta(z, \vec{r_{T2}}) \rightarrow \eta_A(z, \vec{r_{T2}})$  $t(\vec{r_{T2}}) \rightarrow t_A(\vec{r_{T2}})$

 But, write in terms of convolution of nucleon parton density and nuclear density function:

 $egin{aligned} &\eta_A(z,ec{r_T}) = \int dz_A \int d^2 r_{TA} \; 
ho(z_A,ec{r_T}_A) \; \eta(z-z_A,r_T-r_{TA}) \ &t_A(z,ec{r_T}) = \int d^2 r_T' \; T(ec{r_T}-ec{r_T}') \; t(ec{r_T}') \end{aligned}$ 

 Now write the p+A hard scattering probability at an impact parameter b

 $P_{hard}(b) = \int d^2 r_{T1} \int d^2 r_{T2} \int d^2 r_{TA} t(\vec{r_{T1}}) T(\vec{r_{TA}}) t(\vec{r_{T2}} - \vec{r_{TA}}) rac{d^2 \sigma}{d ee d ee r_{TA}}$ 

• If everything works as above this should reduce to  $\sigma_{pp}^{hard} T(b)$ 

#### Put in the delta function

 $P_{hard}(b) = \int d^2 r_{T1} \int d^2 r_{T2} \int d^2 r_{T'} t(\vec{r_{T1}}) T(\vec{r_{T2}} - \vec{r_{T'}}) t(\vec{r_{T'}}) \frac{d^2 \sigma}{d\vec{\Delta r^2}}$ 

 $P_{hard}(b) = \int d^2 r_{T1} \int d^2 r_{T'} T(\vec{r_{T1}} - \vec{r_{T'}} - \vec{b}) t(\vec{r_{T1}}) t(\vec{r_{T'}})$ 

-No simple reduction.

- •But, the ranges of  $\vec{r_{T1}}$  and  $\vec{r_T}'$  over which  $t(\vec{r_{T1}})$  and  $t(\vec{r_T}')$  are finite are small (< 1 fm).
  - -we are sampling nuclear thickness over a small region around  $\vec{b}$

#### If T is ≈ constant over that region:

 $= P_{hard}(b) \approx T(b) \int d^2r_{T1} \int d^2r_{T'} t(\vec{r_{T1}}) t(\vec{r_{T'}}) \rightarrow T(b)\sigma_{hard}$ 

### **Go back to Cronin**

So hard scattering rates in p+A varying as A<sup>1</sup> make sense.
What about < 1?</li>
What about > 1?
Why particle species dependent?



#### Why α < 1 @ low p<sub>T</sub> ?

Cronin *et al,* Phys. Rev. D 29, 2476–2482 (1984)



FIG. 4. The ratio  $R = \langle n \rangle_{pA} / \langle n \rangle_{pp}$  versus the average number  $\overline{v}(n_p)$  of projectile collisions for pXe (circles), pAr (triangles), and pNe (squares) collisions. A line of the form  $R = 0.5[\overline{v}(n_p) + 1]$  is shown for comparison.

• Soft particle production does not grow proportional to number of soft N-N scatterings,  $\nu = \sigma_{inel} T(b)$  $\Rightarrow$ Instead varies like number of wounded nucleons (participants),  $N_w = \frac{1}{2} (1 + \nu)$ 

## Why α < 1 @ low p<sub>T</sub> ?

- If we integrate over impact parameter the contribution from the "1" is proportional to the total p+A inelastic cross-section  $\Rightarrow A^{2/3}$
- •While the contribution proportional to v varies like  $A^1$ 
  - ⇒So the soft production varies with A at a power between 2/3 and 1.
- Strictly, pure wounded-nucleon scaling only applies for total multiplicities
  - Depending on kinematic region covered soft A dependence can be closer to 2/3 or 1.
    - $\Rightarrow$ Beware,  $\alpha \neq R_{pPb}$

# Why α > 1 @ high p<sub>T</sub> ?

$$\sigma_{AB} = \sum_{ab} \int dx_a dx_b \,\phi_{a/A}(x_a,\mu^2) \,\phi_{b/B}(x_b,\mu^2) \,\hat{\sigma}_{ab} \left(\frac{Q^2}{x_a x_b s},\frac{Q}{\mu},\alpha_s(\mu)\right) \left(1 + \mathcal{O}\left(\frac{1}{Q^P}\right)\right)$$

#### • The $\alpha$ > 1 results from higher twist terms $\Rightarrow$ involve additional soft (<< Q<sup>2</sup>) exchanges between ingoing/outgoing parton of hard scattering and other partons from target In case of Cronin effect: -Usual explanation is soft multiple scatterings of ingoing and outgoing partons $\Rightarrow$ broadens the p<sub>T</sub> distribution -fragmentation no longer universal! ⇒hadron species dependence ⇒Poorly understood

### **Quarks fragmenting in nuclei**



#### Study the fragmentation of quarks (?) in nucleus using semi-inclusive deep inelastic scattering

## "Stopping" quarks in nuclei

 z = fraction of quark energy (v) carried by hadron

 Ratio of yields relative to those on deuterium

⇒A and flavor dependent reduction in yield of high-z hadrons



# "Stopping" quarks in nuclei

Weak Q<sup>2</sup>
 dependence

 "Stopping" decreases with increasing quark energy.



# "Stopping" quarks in nuclei



 E665 (v > 100 GeV) and EMC see little/no stopping of quarks in nucleus

#### "Cold nucleus" energy loss

- Existing data suggest that cold nucleus energy loss is small for quark energies greater than ~ 100 GeV.
  - -Better data needed  $\rightarrow$  EIC.
- Consider effects in d/p+A at RHIC, LHC.
  - -mid-rapidity jets with transverse mass

 $m_T=\sqrt{p_T^2+m^2}$ 

- -Have energies in the nuclear rest frame given by  $E=m_T\cosh\Delta y$
- -With  $\Delta y$  the rapidity difference between the jet and the nucleus.

#### • For RHIC @ mid-rapidity, $E = m_T imes 106$

- ⇒ weak cold nucleus energy loss
- $\Rightarrow$  even less @ LHC except maybe at large y. <sup>29</sup>

#### E609, Corcoran et al, PLB 259 (1991) 209



#### • Broadening of the dijet $\Delta \varphi$ distribution

#### E609, Corcoran et al, PLB 259 (1991) 209



 Similar results with calorimetric energy flow instead of jets.

#### E557, Stewart et al, Phys. Rev. D 42, 1385–1395 (1990)

800 GeV (fixed target) p+p, Be, C, Cu, and Pb

Single jets





E557, Stewart et al, Phys. Rev. D 42, 1385–1395 (1990)

800 GeV (fixed target) p+p, Be, C, Cu, and Pb

dijets (Ejj is scalar sum of dijet E<sub>T</sub>'s)



FIG. 8. (a) Dependence of  $d^3\sigma/dE_i^{\mu}d\eta_1^{\bullet}d\eta_2^{\bullet}$  on dijet  $E_i^{\mu}$  for pA interactions at 800 GeV/c, where  $E_i^{\mu}$  is the scalar sum of transverse energy of the two jets. (b)  $\alpha$  vs  $E_i^{\mu}$ . (c) and (d) Same as (a) and (b) after correction for the underlying event (see text) was applied to the heavier nuclei data.

#### Jets in fixed-target p+A

- Data suggest that in p+heavy nucleus collisions, for jets with p<sub>T</sub> ~ 4-6 GeV
  - "nuclear enhancements" are observed in the single jet, dijet rates
  - -and dijet acoplanarity.
- But, E557 data show that at higher jet p<sub>T</sub>, at most weak modifications

once underlying event is subtracted

 "nuclear effects" are dying away more rapidly with jet energy in p+A than in e+A?
 ⇒due to larger Q<sup>2</sup> in p+A vs DIS?

#### **Summary**

- Studies of hard scattering processes in proton-nucleus and lepton-nucleus collisions show non-trivial A dependence
   Separate from nuclear PDF modifications
- Those effects are consistent with initial and/or final-state transverse momentum broadening
  - -Cronin effect, Dijet broadening
- And cold nuclear energy loss
  - -semi-inclusive deep inelastic scattering
- Confined to p<sub>T</sub> scales <~ 10 GeV</li>
   ⇒Though relevant scales for broadening & energy loss may be different

#### **Geometry, again**

#### Go back to:

 $\int - E \, rac{d^3 n^{pA(b)}}{dp^3} = T(b) imes E \, rac{d^3 \sigma^{pp}}{dp^3}$ 

 Most fundamental expression of the impact of the nuclear geometry on hard scattering
 ⇒assuming factorization

Often, the right-hand side is reinterpreted

$$- E \, {d^3 n^{pA(b)} \over dp^3} = T(b) imes \sigma^{pp}_{inel} imes E {d^3 n^{pp} \over dp^3}$$

•Then,  $N_{coll}$  is defined  $N_{coll} = T(b) \sigma_{inel}^{pp}$ -Yielding,  $E \frac{d^3 n^{pA(b)}}{dp^3} = N_{coll} \times E \frac{d^3 n^{pp}}{dp^3}$ 

#### Geometry, again

# •Which might motivate a definition of $R_{pA}$ - $R_{pA} \equiv rac{d^3 n^{pA(b)}/dp^3}{N_{coll} \ d^3 n^{pp}/dp^3}$

This is an abomination!
Measuring E d<sup>3</sup>n<sup>pp</sup>/dp<sup>3</sup> is difficult due to ⇒diffraction (in inelastic cross-section)
⇒inefficiencies in triggering on or reconstructing low-multiplicity events.
But, if we use T(b) and p-p cross-section for hard process, R<sub>pA</sub> is robust

$$^-R_{pA}\equiv rac{d^3n^{pA(b)}/dp^3}{T(b)~d^3\sigma^{pp}/dp^3}$$

## **RHIC: a new regime**



7-200 GeV/A Au+Au, d+Au, Cu+Cu 32-500 GeV p+p, ...

**STAR** 





#### The early days of jet quenching

PHENIX, Phys. Rev. Lett. 91, 241803 (2003)



## **A-A Hard Scattering Rates**

 For "partonic" scattering or production processes, rates are determined by T<sub>AB</sub>

$$T_{AB}(b) = \int dec{r} \ T_A(ec{r}ec{}) \ T_B(ec{b}-ec{r}ec{})$$

- -t-integrated A-A parton luminosity
- Normalized relative to p-p
- If factorization holds, then

$$\frac{dn_{hard}^{AB}}{dp_{\perp}^{2}} = \frac{d\sigma_{hard}^{NN}}{dp_{\perp}^{2}}T_{AB}(b)$$

- Define R<sub>AA</sub>
  - Degree to which factorization is violated



 $T(r_t) = \int dz \, \rho_A^{nucleon}(z, r_t)$ 

#### PHENIX: "jet" quenching @ 130, 200 GeV



#### Limited reach in pT compared to what we are used to in the LHC era.

 Qualitative features of single hadron suppression already established in 2003.
 ⇒In particular, apparent weak p<sub>T</sub> variation

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# Single/di-hadron suppression w/ control



#### **PHENIX Au+Au** π<sup>0</sup> Spectra



 Control over systematic errors w/ two measurements using different electromagnetic calorimeter

# PHENIX Au+Au π<sup>0</sup> R<sub>AA</sub>



• Factor of ~ 5 violation of factorization in central Au+Au

 Smooth evolution of high-p<sub>T</sub> π<sup>0</sup> suppression with centrality.

 ≈ constant for p<sub>T</sub> > 4 GeV/c (more on this later).

### **STAR charged hadron suppression**

STAR, PRL 91 (2003) 172302



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### Single hadrons, photon



 "State of the art" in single hadron suppression measurements @ RHIC.

## Single hadron and quenching "theory"



 suggests qhat values >> larger than ones we currently think are appropriate (~ 1 GeV<sup>2</sup>/fm)

## Jet tomography

#### • How to probe geometry?

- Use spatial asymmetry of medium @ non-zero impact parameter
- Measure orientation
   (ψ) event-by event
- Measure  $R_{AA}$ vs  $\Delta \phi = \phi - \psi$





# Jet tomography

0.5

PH ENIX

1.5

0.5

- How to disentangle two contributions?
  - Use spatial asymmetry of medium @ non-zero impact parameter
  - Measure orientation
     (ψ) event-by event
- Measure  $R_{AA}$ vs  $\Delta \phi = \phi - \psi$
- Characterize by amplitude of Δφ modulation:



0.5

 $\Delta \phi$  (rad)

1.5 0

0.5



1.5

# **Single hadron suppression**



Wicks et al., NPA784, 426
Marquet, Renk, PLB685, 270
Drees, Feng, Jia, PRC71, 034909
Jia, Wei, arXiv: 1005.0645

**Calculations:** 

#### Two calculations: weak, strong coupling

- N<sub>part</sub> dependence same for both
- But  $v_2$  (modulation vs  $\Delta \phi$ ) prefers strong coupling

## **Single hadron suppression**



Two calculations: weak, strong coupling

- N<sub>part</sub> dependence same for both
- But  $v_2$  (modulation vs  $\Delta \phi$ ) prefers strong coupling

# **STAR Experiment: "Jet" Observations**

#### proton-proton jet event

Analyze by measuring (azimuthal) angle between pairs of particles



In Au-Au collisions we see one "jet" at a time
 Strong jet quenching
 Enhanced by surface bias



#### **Two-particle correlations**



Indirect dijet measurement via dihadron correlations



STAR, Phys. Rev. C82 (2010) 024912

 Through very detailed measurements from STAR and PHENIX we've learned that most of this has little to do with high-p<sub>T</sub> physics, though it is very interesting 53

# **Heavy quark suppression**



 Measure heavy quark production via semi-leptonic decays (B+D) to electrons
 See suppression comparable to light mesons
 Unexpected due to mass suppression of radiative contributions, especially for b quark.

# RHIC – Where We Stand (from 2009)

#### Significant theoretical uncertainties

- Role of collisional energy loss.
- Differences in approximations.
- Choice of strong coupling constant.
- Description of medium
- Incorporating position, time dependence of medium.
- Fluctuations in # emitted gluons.
- Energy loss biases.

 Currently single hadron data do not sufficiently discriminate, test theoretical differences.

- Use more "differential" measurements.
- Use multi-hadron measurements.

#### **Better: use full jet measurements**

#### Where are we?

 Studies of "jet" modification in nuclei show clear, but modest effects in e+A/p+A collisions.

-Clearly decrease with increasing jet energy

Geometry plays an critical role in hard scattering in nuclei

– and influencing initial/final-state interactions

 Start of RHIC program opened a new frontier where much larger effects are observed due to (s)QGP.

 But single, two-particle, heavy quark measurements have not provided unique understanding of quenching physics ⇒ jets.