

# $\Sigma^-$ production in kaon absorptions by FINUDA

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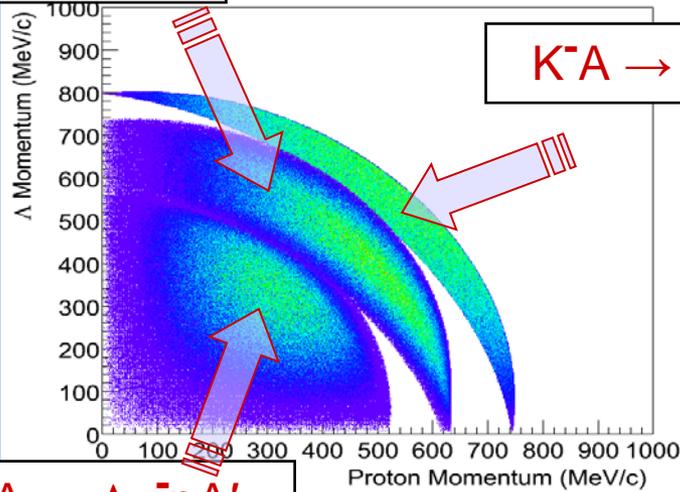
# Outline

- Introduction: hyperon production in single/two nucleon kaon absorptions
- Free  $\Sigma$  production in FINUDA: signal extraction in  $\Sigma^\pm\pi^\mp$  vs  $\Sigma^-p$  reactions
  - Data features
  - production rates
- $\Sigma^-p$ : global fit to the data –  ${}^6\text{Li}$ ,  ${}^7\text{Li}$  ( ${}^9\text{Be}$ ,  ${}^{13}\text{C}$ ,  ${}^{16}\text{O}$ )
  - Method: binned likelihood fits
  - Basic hypotheses (Quasi-Free dynamics)
    - Ingredients
    - Backgrounds and contaminations
    - Results and fits quality
  - Add-ons
- Conclusions

# $K^-$ stop absorption by one vs many nucleons

$K^- A \rightarrow \Sigma^0 p A'_{gs}$   
 $\Sigma^0 \rightarrow \Lambda \gamma$

Phase space simulation:  $K^-_{stop} {}^6\text{Li}$

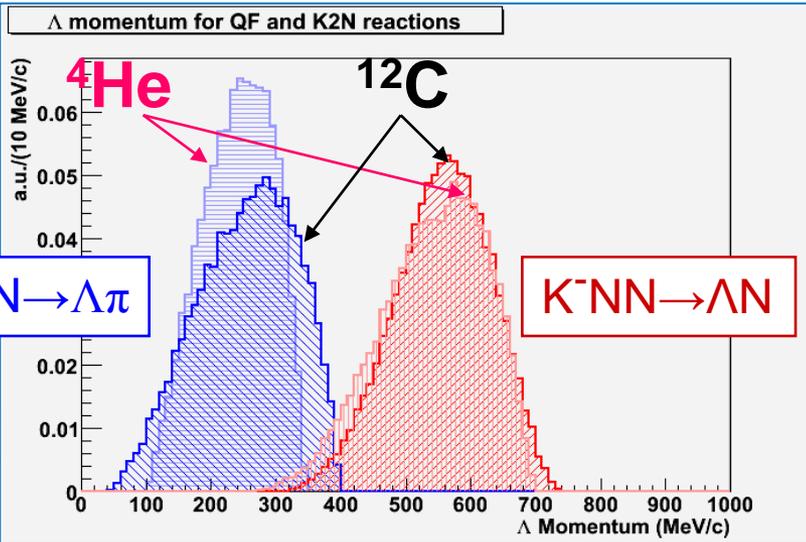
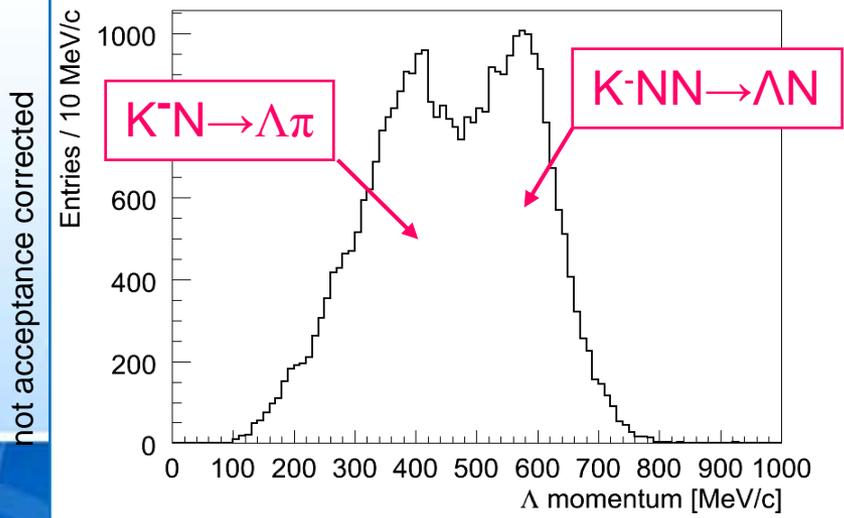


$K^- A \rightarrow \Lambda p A'_{gs}$

$K^- A \rightarrow \Lambda \pi^- p A'_{gs}$

Expected signatures:  
 in pionless reactions  
 emission of **high momentum nucleons**  
 (or light nuclei) and  
**hyperons**

FINUDA DATA:  $K^-_{stop} {}^6\text{Li} \rightarrow \Lambda X$



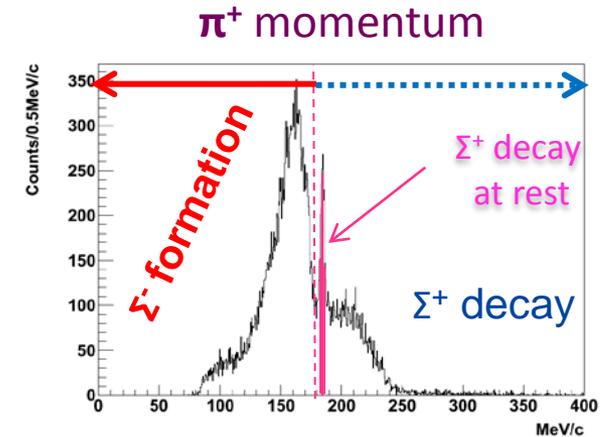
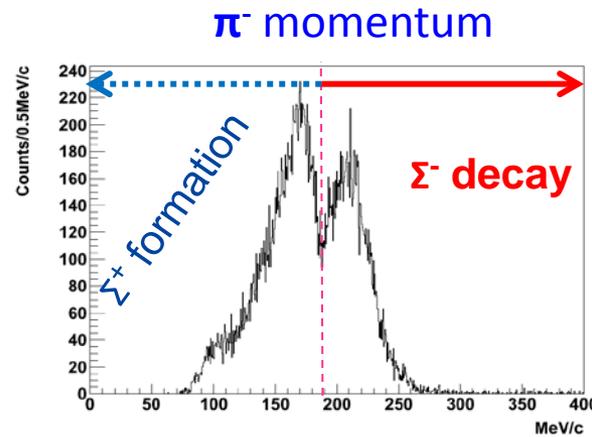
# $\Sigma^-$ signal extraction in FINUDA ( ${}^6\text{Li}$ target)

- One charged pion, one neutron
- The  $\pi^-$  from the  $\Sigma^-$  decay has the largest momentum
- $\Sigma^+$  can decay at rest,  $\Sigma^-$  are always absorbed by the hit nucleus
- Study of the **decay pion** & the **prompt particle** (raw spectra)

particle	Momentum resolution ( $\sigma$ )	Det+rec efficiency
proton	1%	75%
$\pi^-$	0.6%	73%
neutron	5%	3%

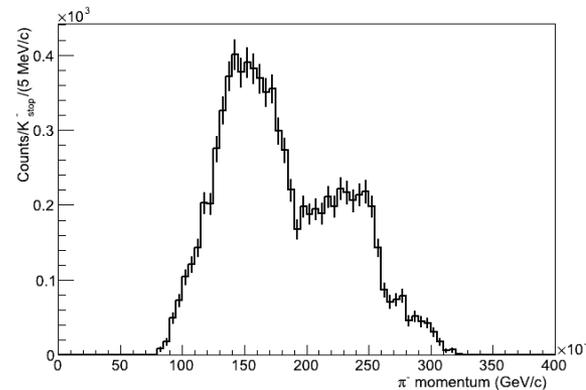
$n\pi^+\pi^-$

FINUDA Coll.,  
PLB704 (2011), 474

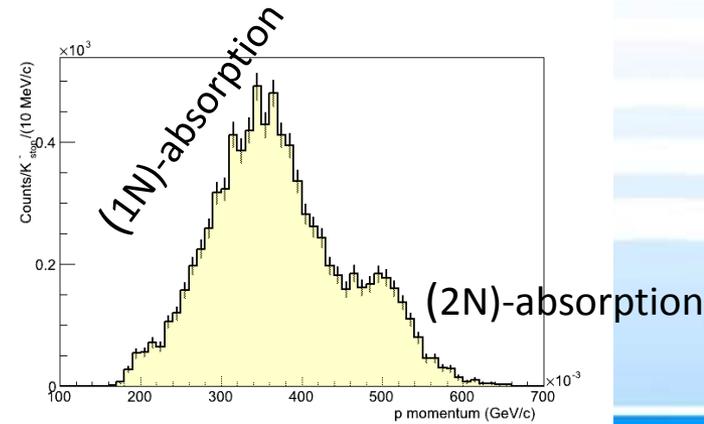


$np\pi^-$

Large background!



$\pi^-$  momentum

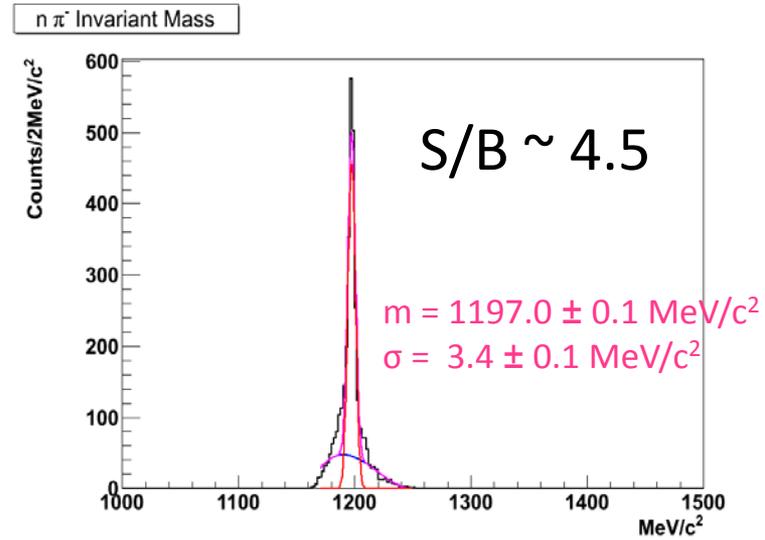
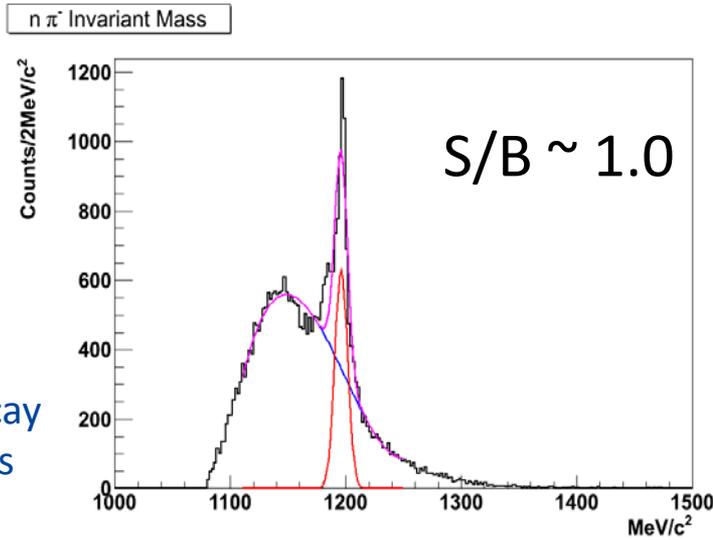


p momentum

# $\Sigma^-$ signal identification

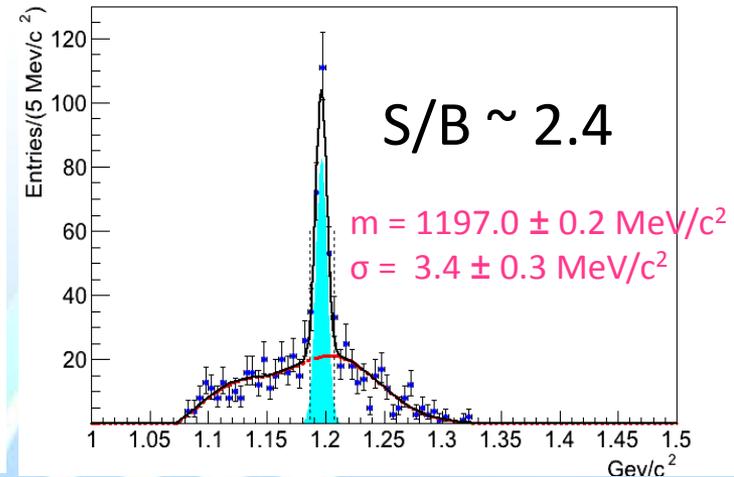
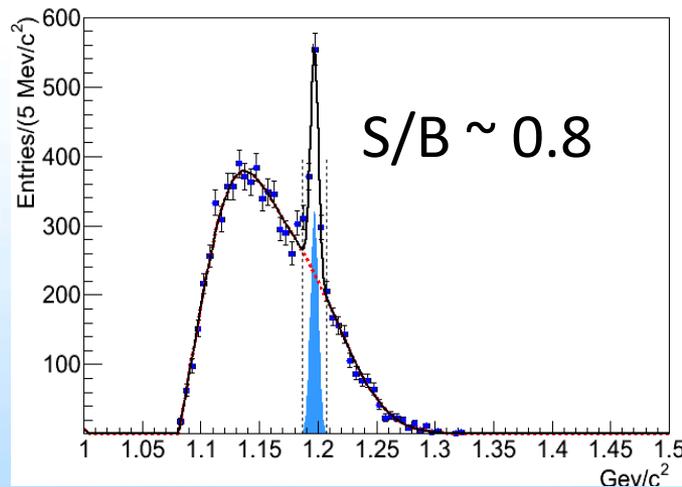
## $n\pi^+\pi^-$

- reject events with unphysical missing mass
- track fitting
- vertex selection
- $\Sigma^-$  decay angle
- $\pi^+\pi^-$  production/decay kinematic constraints



## $n\rho\pi^-$

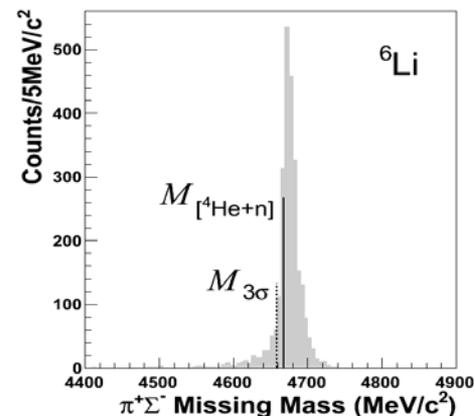
- reject events with unphysical missing mass
- track fitting
- vertex selection
- $\Lambda$  rejection



# Missing mass studies ( $K^- {}^6\text{Li}$ – (final state particles))

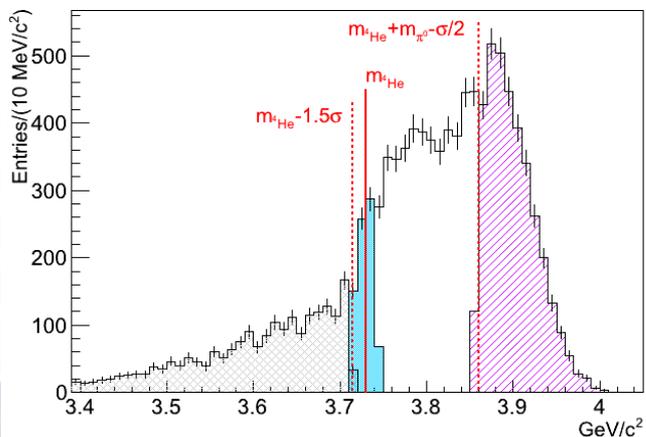
$n\pi^+\pi^-$

- pure QF  $\Sigma^-\pi^+$  reaction: very little missing energy ( $\sim 4\%$ )
- exclusive measurement (no missing  $\pi$ , N)
- peak:  $\sim 3$  MeV above physical threshold
- width:  $\sigma \sim 9$  MeV

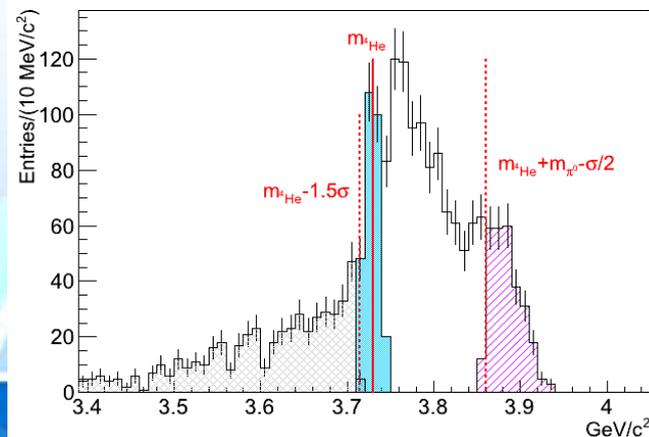


$np\pi^-$

- large amount of unphysical events: neutron rescattering, reconstruction errors, misidentifications (wrong n, n/ $\gamma$ , ...)
- missing mass resolution:  $\sigma \sim 10$  MeV
- inclusive  $\Sigma^-p$  reaction (all physical data) vs **exclusive QF  $\Sigma^-p$  (“g.s. region”)**
- QF reactions identifications:  $\Sigma^-p$ ,  $\Sigma^-p\pi^0$

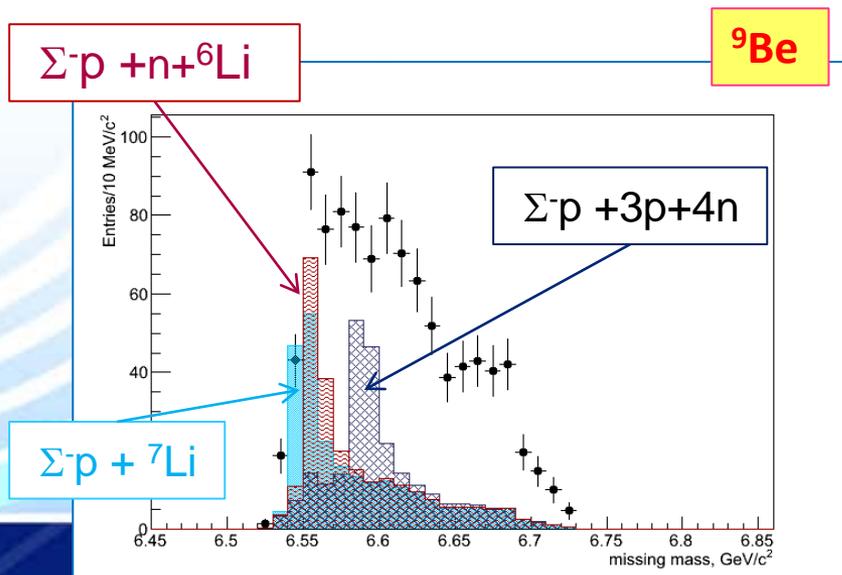


$\Sigma^-$  selection in proper ( $n\pi^-$ ) mass window

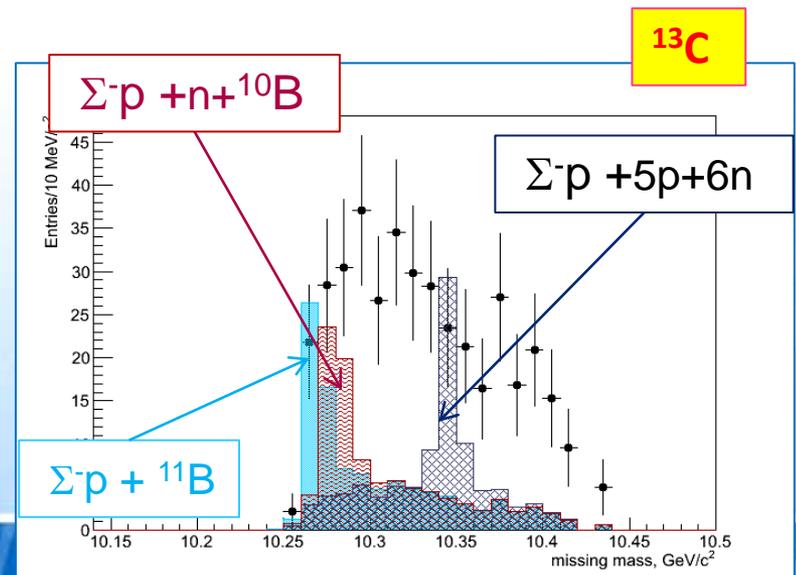


# “Exclusive” QF $\Sigma^-p$ absorption

- $\Sigma^-p$  production recoiling against a nuclear system in its minimal mass configuration – occurs when the absorption is *exactly* on a (pn) pair
- Many nucleon absorptions can also occur leaving the recoiling system in a fragmented/excited configuration with larger mass/energy
- Important effect especially for heavy nuclei (energy difference  $> 40 \text{ MeV}/c^2$ ), but not negligible for lighter ones
- **Missing mass resolution: 9-12  $\text{MeV}/c^2$** 
  - The width of the missing mass band chosen for the selection is optimized to exclude the overlap of the farthest configurations
  - Unavoidable overlap with closer energy configurations: included in the rate calculation
    - **“Ground state”**: minimal mass state within the experimental resolution (i.e.,  $\sim 3\sigma$ )



Arbitrary normalizations

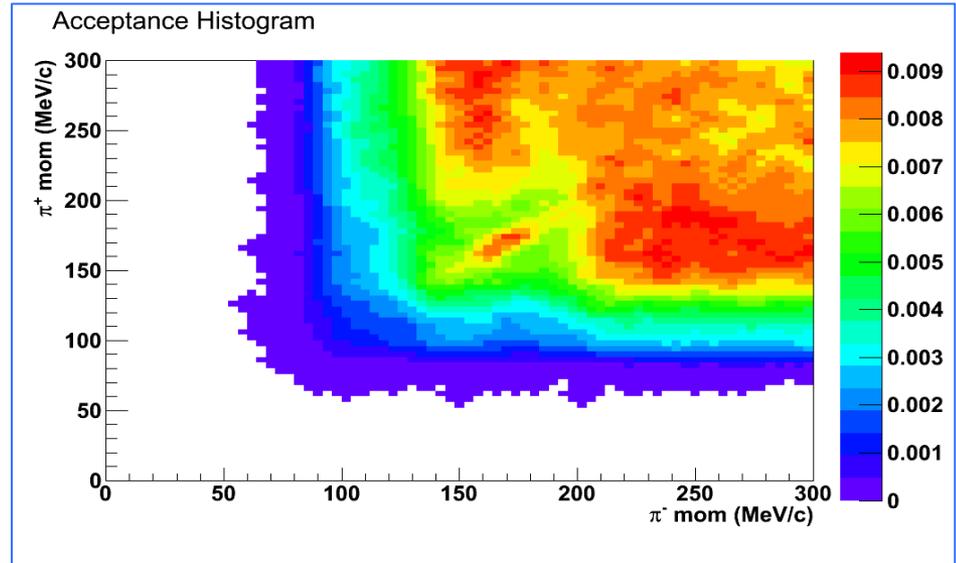


Arbitrary normalizations

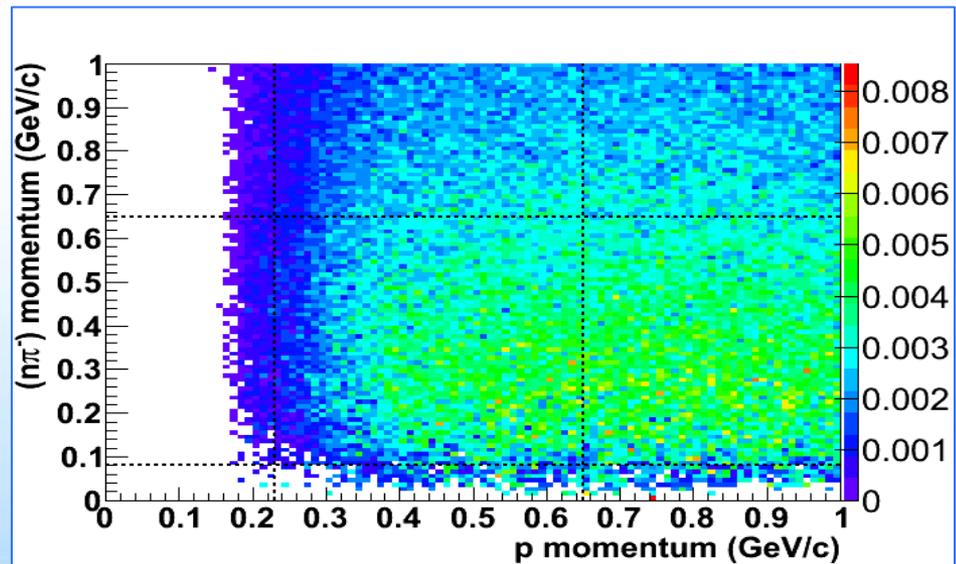
# Acceptance corrections

- Simulations of three particles with flat momenta in the relevant kinematic range of the reaction
  - $O(10^9)$  events simulated
- Event-by-event correction: each event is assigned a weight according to its location in phase space (9 coordinates/particle)
- Critical correction at edges: large statistical+systematic error
  - Cuts to reduce the total uncertainty at the phase space borders

$$n\pi^+\pi^-$$

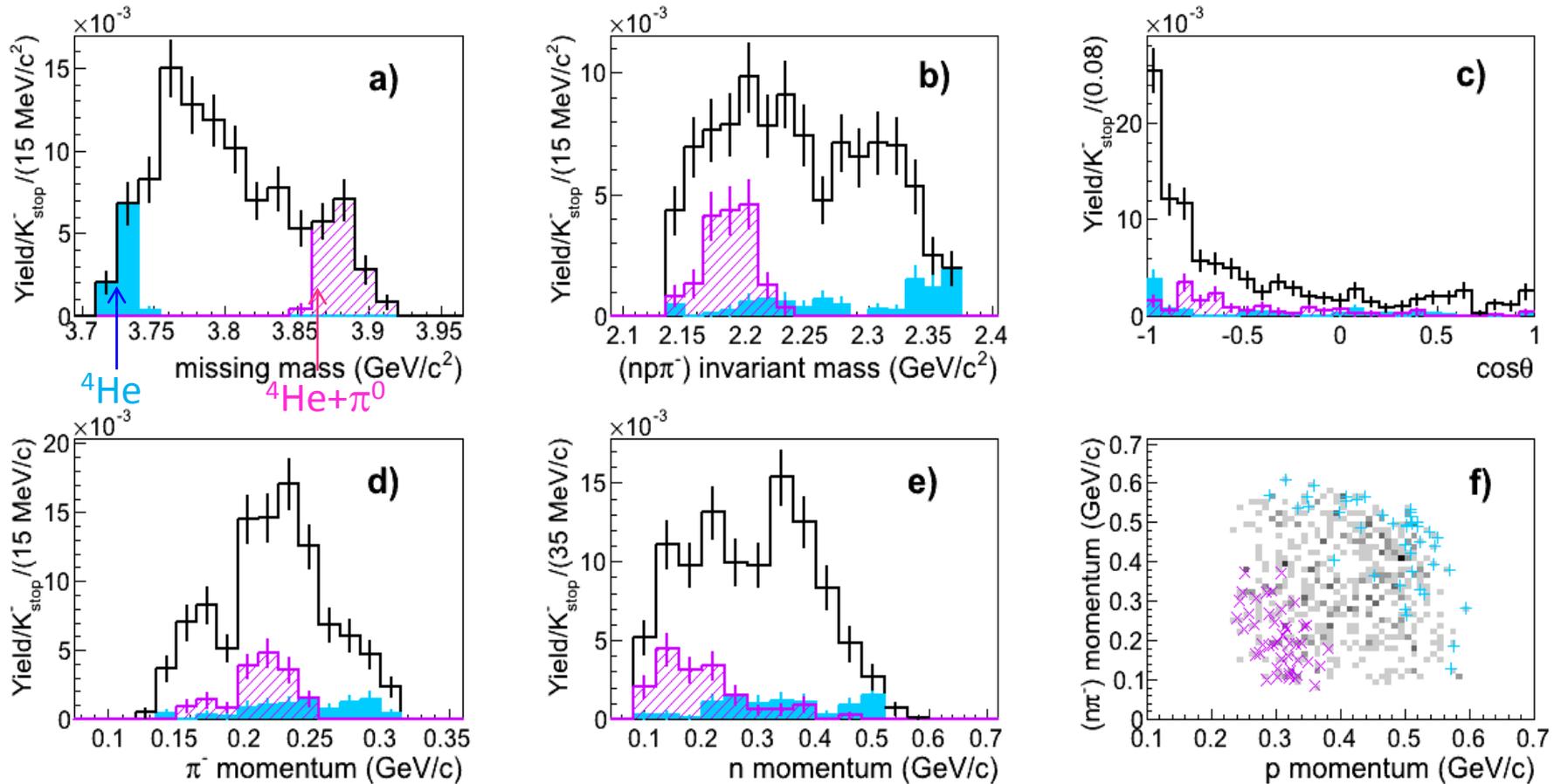


$$np\pi^-$$



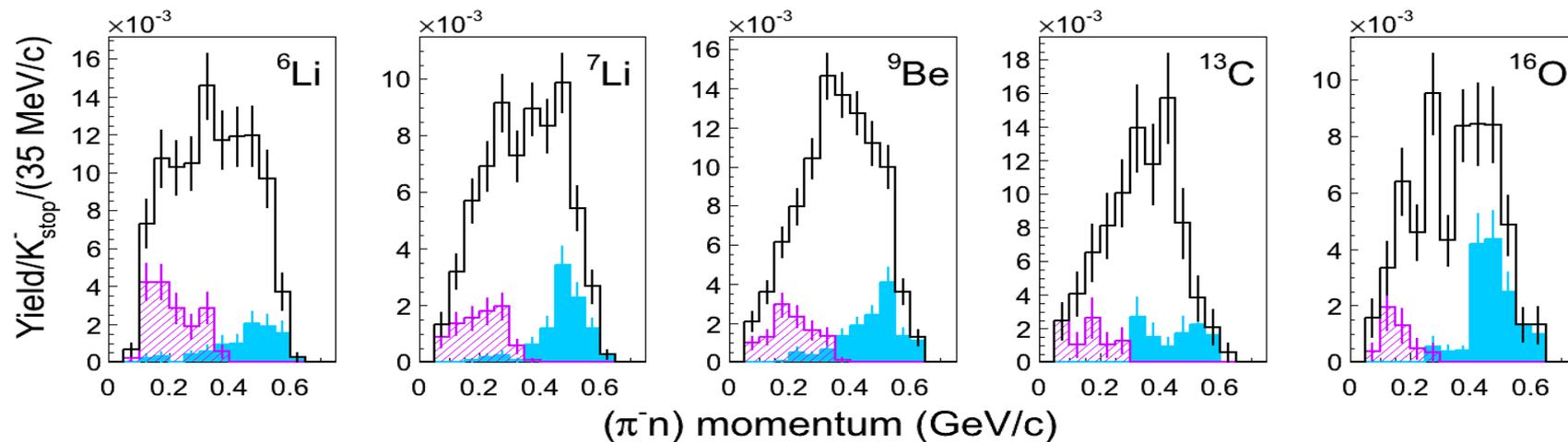
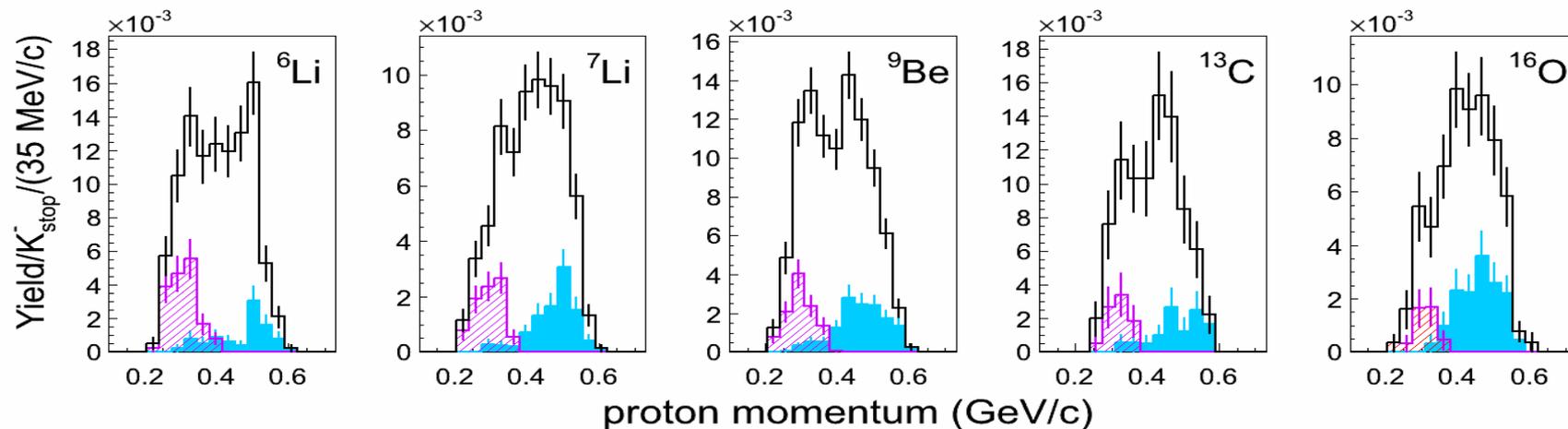
# $\Sigma^- p$ : acceptance corrected spectra, $\Sigma^-$ region selection – ${}^6\text{Li}$

Events selected in the  ${}^4\text{He}$  missing mass band distribute as expected by the QF  $\Sigma^- p$  reaction



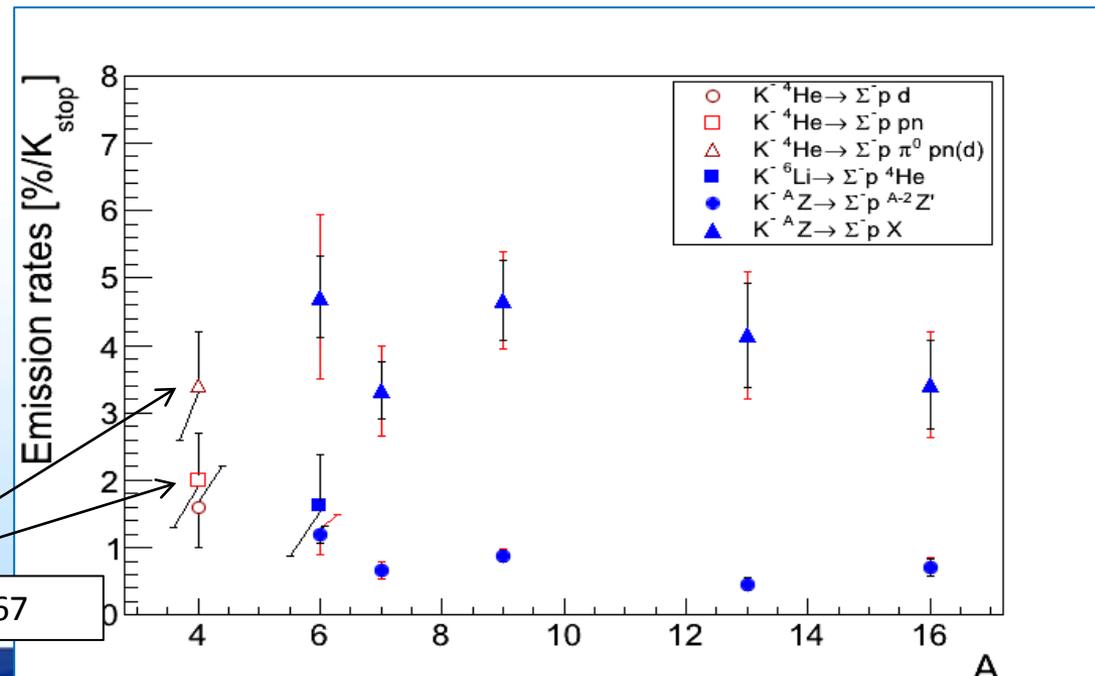
# $\Sigma^-$ p: acceptance corrected spectra proton and $\Sigma^-$ momenta in all targets

Similar trends for both p and ( $n\pi^-$ ) momentum in all targets: **QF  $\Sigma^-$ p reaction almost at rest**



# $\Sigma^-$ p emission rates in p-shell nuclei

- **Emission rates**: from the number of events in the  $\Sigma^-$  peak, background subtracted
  - both for the inclusive and the exclusive sample
    - Inclusive measurement: integrated over the full phase space volume
  - corrected for the fraction of  $\Sigma^-$ 's lost for nuclear capture (PLB 704 (2011), 474)
  - No correction for pion attenuation nor  $\Sigma\Lambda$  conversion
- Measured rates are in agreement with older (few) data
  - **New measurements for  $A > 6$**



Katz, PRD1 (1970), 1267

# $\Sigma^\pm\pi^\mp$ vs $\Sigma^-p$ emission rates: comparison

PLB704 (2011), 474

## • $\Sigma^\pm\pi^\mp$ rates

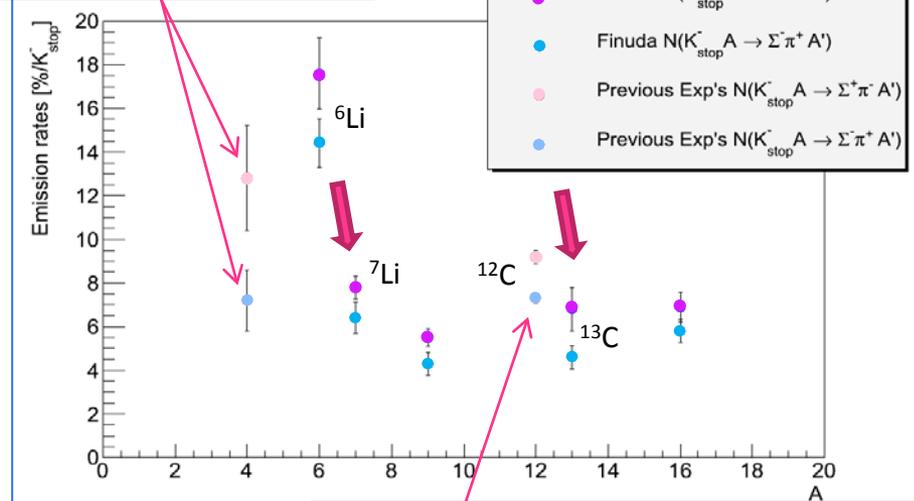
- Remarkable decrease between  ${}^6\text{Li}$ - ${}^7\text{Li}$  and  ${}^{12}\text{C}$ - ${}^{13}\text{C}$  pairs
- less K-A stop centers available for these final states

## • $\Sigma^-p$ “exclusive” rates

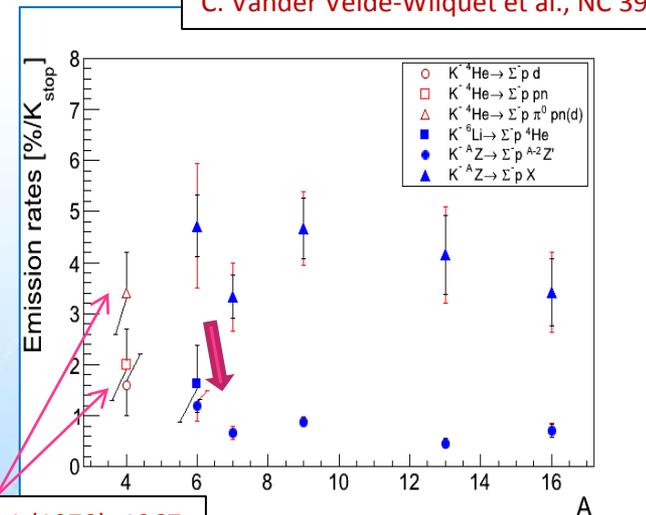
- Same behavior:  ${}^6\text{Li}$ - ${}^7\text{Li}$
- Reduced probability of 2N vs 1N absorptions

- Signature of nuclear shell structure: one more neutron in external shell
- Surface behavior of interactions: little dependence on A (except  ${}^6\text{Li}$  – cluster structure)
- $\Sigma^-p$  inclusive reaction: about 1/3 of  $\Sigma^\pm\pi^\mp$

P. Katz et al., PRD1 (1970), 1267



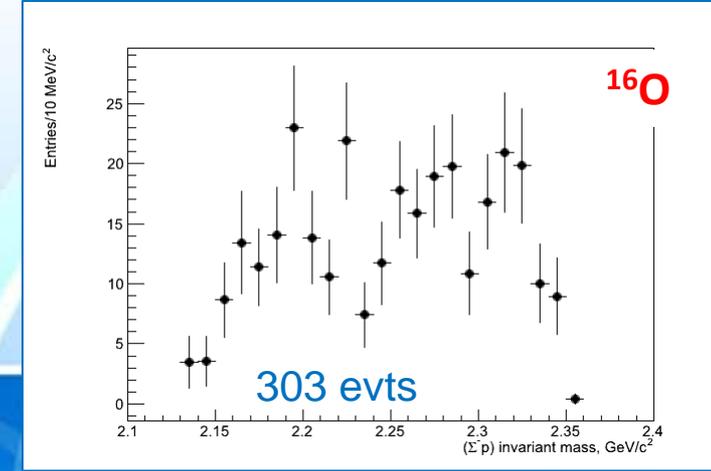
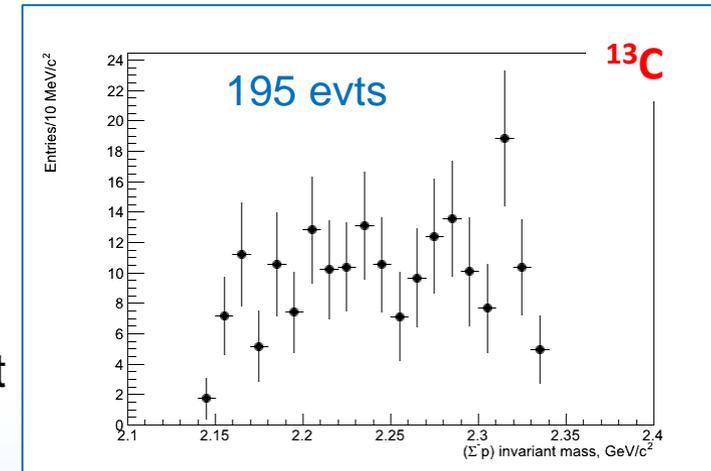
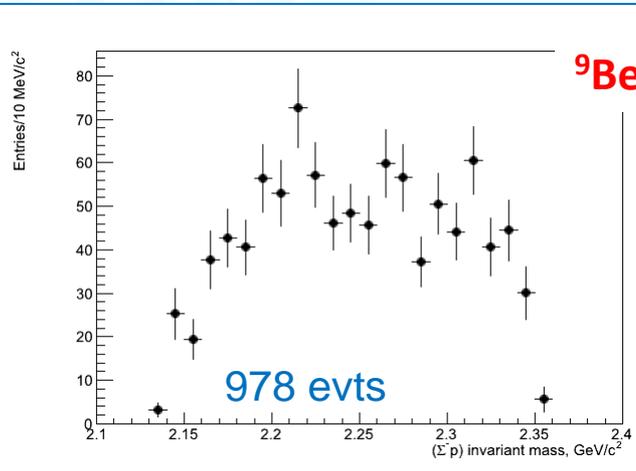
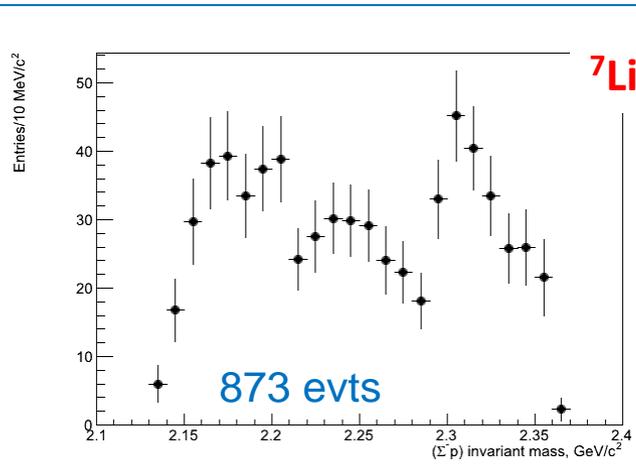
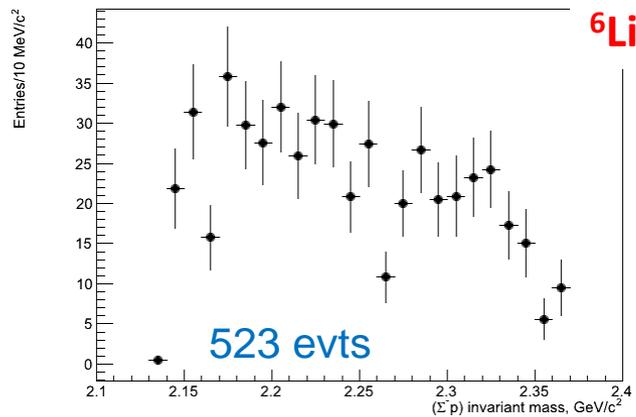
C. Vander Velde-Wilquet et al., NPA241 (1975) 511  
C. Vander Velde-Wilquet et al., NC 39A (1977) 538



P. Katz et al, PRD1 (1970), 1267

# $\Sigma^-p$ : a closer look to the data

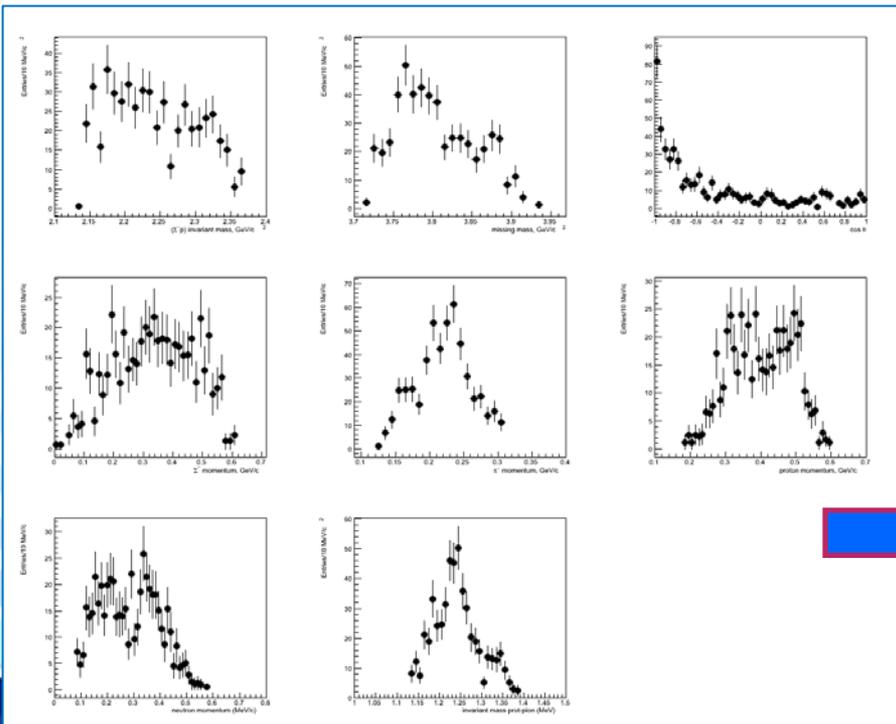
Acceptance corrected **invariant mass** spectra of the  $(n\pi^-)p$  system, selected in the  $(n\pi^-)$  mass band of the  $\Sigma^-$  (background included)



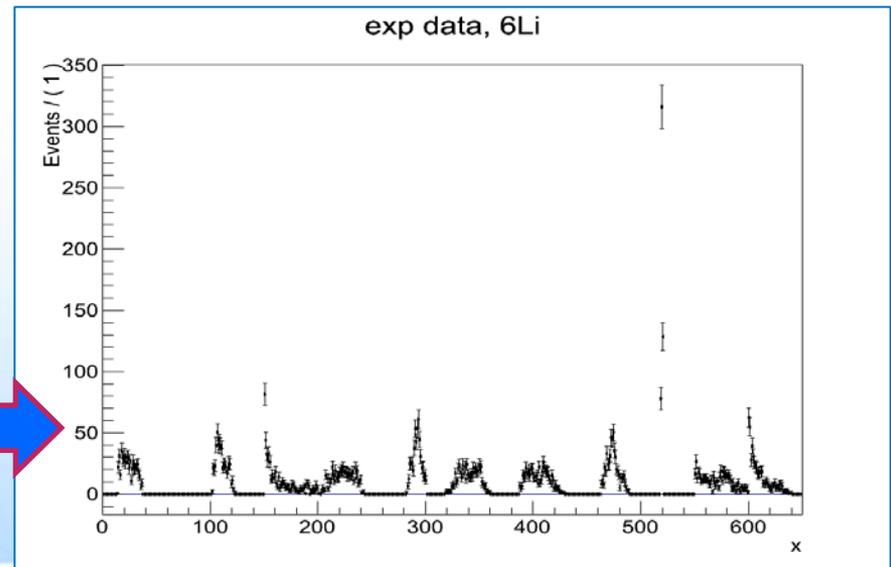
The distributions must be fitted taking into account several reactions and several other observables:  
**GLOBAL FIT**

# $\Sigma^-p$ spectra global fit – the method

- Binned maximum likelihood fit to 11 1D experimental distributions
  - Wide redundance (and correlations)
  - Independent kinematic features (momenta, angles, energy/mass spectra) taken into account in one shot
- To be fitted: one single histogram (11 histograms in a row)



Barlow, Beeston, Comp. Phys. Comm. 77 (1993), 219



# $\Sigma^-p$ spectra global fit – the method

- Fit ingredients: Monte Carlo histograms of several reactions producing  $\Sigma^- p$  or  $(n\pi^- p)$  in the final state, reconstructed through the same chain and acceptance corrected
  - Fitting several observables is crucial to take into account all the kinematic feature of each reaction
- Fit outputs:
  - fractions of each reaction
  - Goodness of fit estimators (give an indication on the quality of the hypothesis)
    - Histogram  $\chi^2$
    - Maximum (-minimum) (log) likelihood
- Minimization engine: MINUIT through TFractionFitter (or RooFit)

# $\Sigma^-p$ spectra global fit – the model

Two classes of Quasi-Free reactions are being considered:

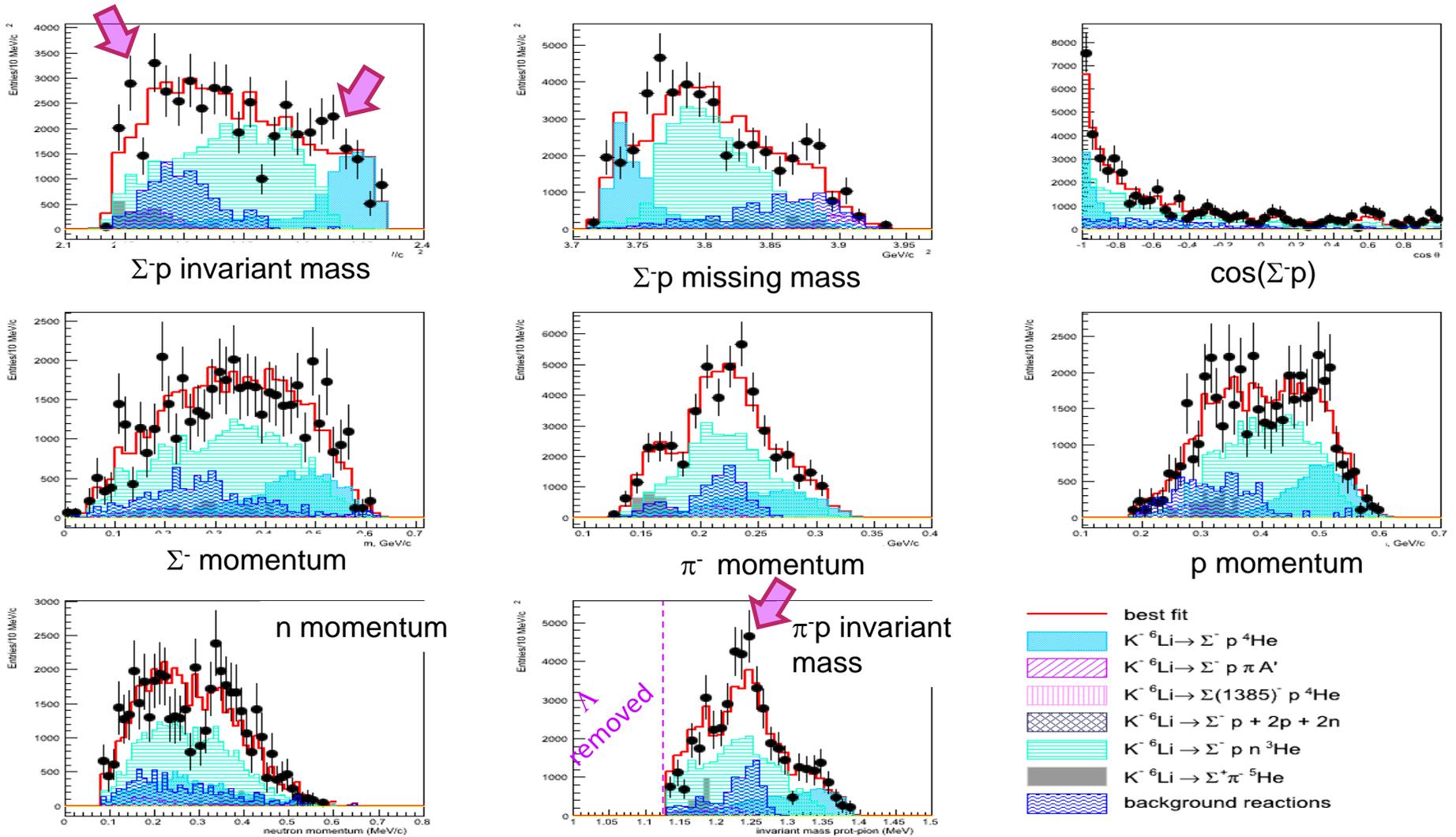
- reactions with  $(\Sigma^-p)$  pairs in the final state, recoiling against a nucleus in its *ground state (or fragmented configuration)*
  - $K^-_{\text{stop}} {}^A Z \rightarrow \Sigma^- p {}^{A-2}(Z-1)$
  - $K^-_{\text{stop}} {}^A Z \rightarrow \Sigma(1385)^- p {}^{A-2}(Z-1) \rightarrow \Sigma^- p \pi^0 {}^{A-2}(Z-1)$
  - $K^-_{\text{stop}} {}^A Z \rightarrow \Sigma^- p \pi^0 {}^{A-2}(Z-1)$
  - $K^-_{\text{stop}} {}^A Z \rightarrow \Sigma^- p \pi^+ {}^{A-2}(Z-2)$  (on pp pair)
  - $K^-_{\text{stop}} {}^A Z \rightarrow \Sigma^- p {}^{A-2}(Z-1) + p$  rescattering
  - $K^-_{\text{stop}} {}^A Z \rightarrow \Sigma^- pn {}^{A-3}(Z-2)$  (on 3N or np pair in  ${}^3\text{H}$  substructure)
- reactions leading to  $(n\pi^-p)$  in the final state, leaking through the selection criteria and entering the  $\Sigma^-$  mass window
  - $K^-_{\text{stop}} {}^Z A \rightarrow \Sigma^+ \pi^- {}^{A-1}(Z-1)$  ( $\pi^+/p$  misidentif.)
  - $K^-_{\text{stop}} {}^Z A \rightarrow \Sigma^0 \pi^0 {}^{A-1}(Z-1)$  ( $\gamma/n$  misidentif.)
  - $K^-_{\text{stop}} {}^Z A \rightarrow \Sigma^+ \pi^- n {}^{A-2}(Z-1)$  (2N absorption)
  - $K^-_{\text{stop}} {}^Z A \rightarrow \Lambda n {}^{A-2}(Z-1)$
  - $K^-_{\text{stop}} {}^Z A \rightarrow \Sigma^0 n {}^{A-2}(Z-1) \rightarrow \Lambda n \gamma {}^{A-2}(Z-1)$
  - $K^-_{\text{stop}} {}^Z A \rightarrow \Sigma^0 n {}^{A-2}(Z-1) \rightarrow \Lambda np {}^{A-3}(Z-2)$
  - $K^-_{\text{stop}} {}^Z A \rightarrow \Sigma^0 n {}^{A-2}(Z-1) \rightarrow \Lambda nn {}^{A-3}(Z-1)$
  - $K^-_{\text{stop}} {}^Z A \rightarrow \Sigma^- n {}^{A-2} Z \rightarrow \Lambda nn {}^{A-2} Z$

}  $\Sigma \Lambda$  conv. react.

# $\Sigma^-p$ spectra global fit – study of backgrounds

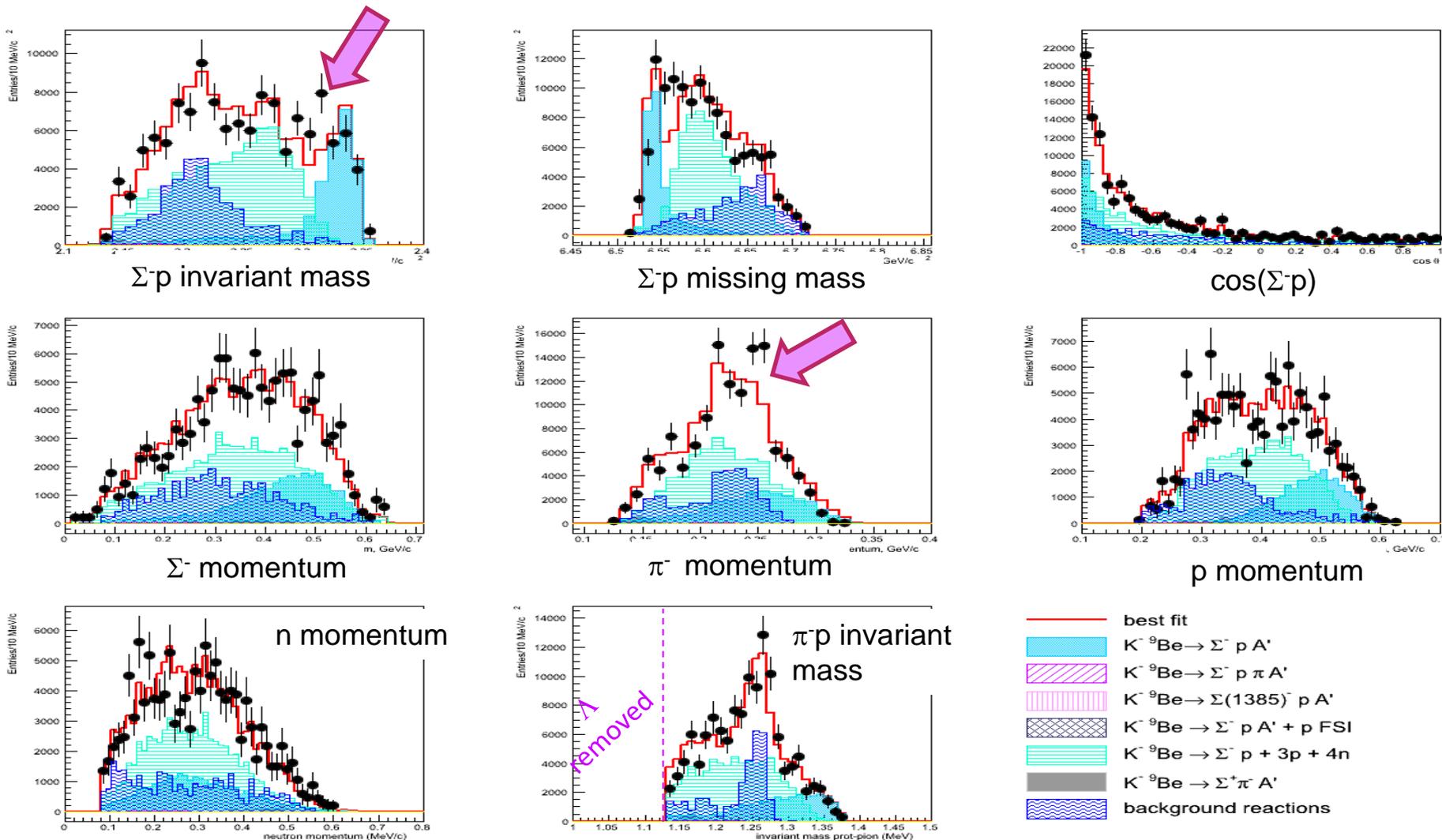
- Large systematic errors expected
  - Larger background contamination due to  $n/\pi^0/\gamma$  misidentification
    - Similar detection+reconstruction efficiency for all neutrals:
      - $\varepsilon_n = 3.5 \times 10^{-2}$
      - $\varepsilon_{\pi^0} = (2.16 \pm 0.01) \times 10^{-2}$
      - $\varepsilon_\gamma = (2.33 \pm 0.01) \times 10^{-2}$
  - Kinematic cuts reduce the contamination of each background reaction to the level of  $10^{-7}/K_{\text{stop}}^-$
  - The only sizeable contribution from  $(np\pi^-)$  background reactions given by one-nucleon absorption:  $K_{\text{stop}}^- {}^Z\text{A} \rightarrow \Sigma^+\pi^- {}^{A-1}(\text{Z}-1)$
  - No inverse  $\Lambda\Sigma$  conversion taken into account (suppressed)
  - Incoherent background component: mixture of QF reactions + conversion and/or rescattering not leading to  $\Sigma^-p$  in the final state

# ${}^6\text{Li}$ : fit with QF reactions only, $A_{\text{g.s.}}$ $\chi_R^2 = 1.42$



- 4 main reactions describe most of the spectra – incoherent background at 15-20% level
- Not sensitive enough to separate  $\Sigma^- p \pi^0$ ,  $\Sigma(1385)^- p$  and  $\Sigma^- p \pi^-$  contributions
- Sizeable contribution from  $\Sigma^- p n$  final state – **imperfect fit at 2150 and 2300 MeV/c<sup>2</sup>**

# ${}^9\text{Be}$ : fit with QF reactions, $A_{\text{g.s.}}$ $\chi_R^2 = 1.56$

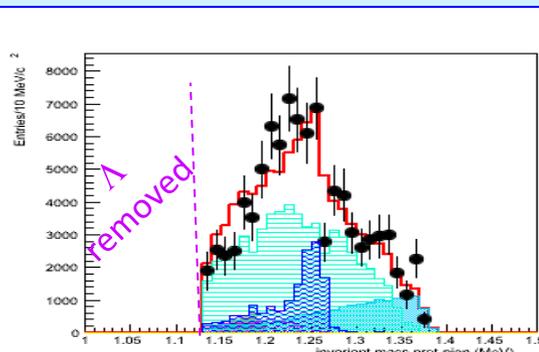
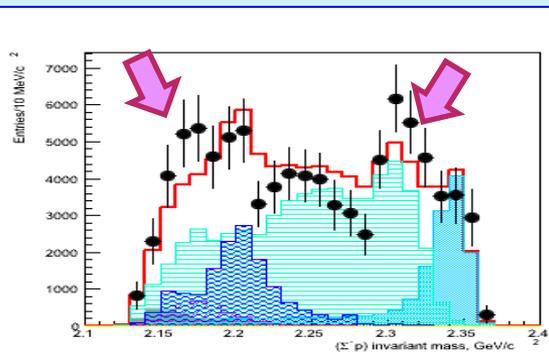


- 3 main reactions describe most of the spectra – incoherent background at 20% level
- pion momentum fit not satisfactory
- Sizeable contribution from  $\Sigma^- pn$  final state - **Missing strength at 2300 MeV/c<sup>2</sup>**

# ${}^7\text{Li}$ , ${}^{13}\text{C}$ , ${}^{16}\text{O}$ : fit with QF reactions only, $A_{g.s.}$

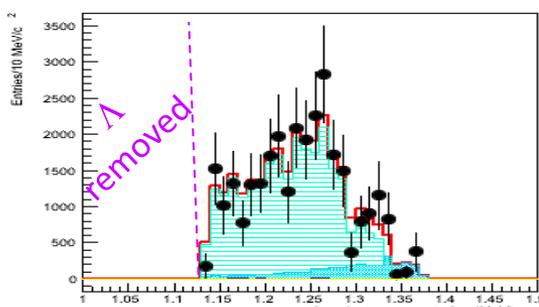
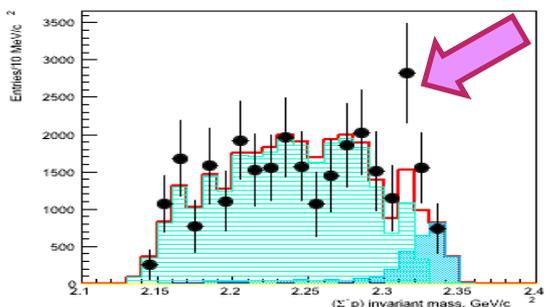
$\Sigma^-p$  invariant mass

$\pi^-p$  invariant mass



${}^7\text{Li}$

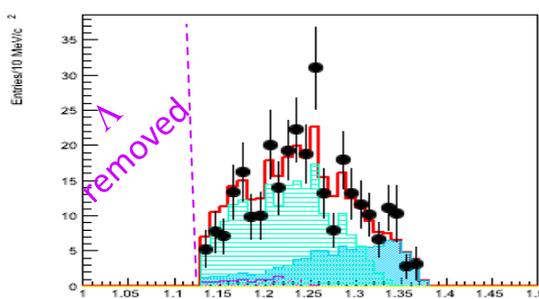
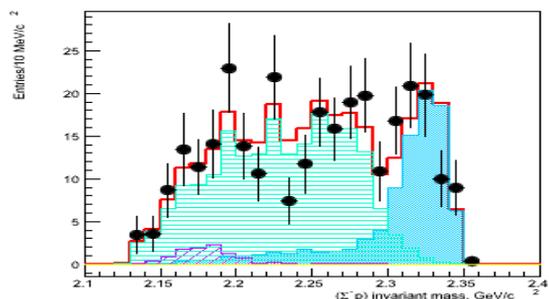
- 4 main reactions describe most of the spectra – incoherent background at 15-20% level
- Sizeable contribution from  $\Sigma^-pn$  final state - Missing strength at 2150 and 2300 MeV/c<sup>2</sup>
- $\chi_R^2 = 1.24$



${}^{13}\text{C}$

Low statistics

- 2 main reactions describe most of the spectra
- Sizeable contribution from  $\Sigma^-pn$  final state - Missing strength at ~2320 MeV/c<sup>2</sup>
- $\chi_R^2 = 0.61$



${}^{16}\text{O}$

Low statistics

- 3 main reactions describe most of the spectra
- Sizeable contribution from  $\Sigma^-pn$  final state -
- $\chi_R^2 = 0.83$

# Add-on #1: QF reactions with recoiling fragmented nucleus

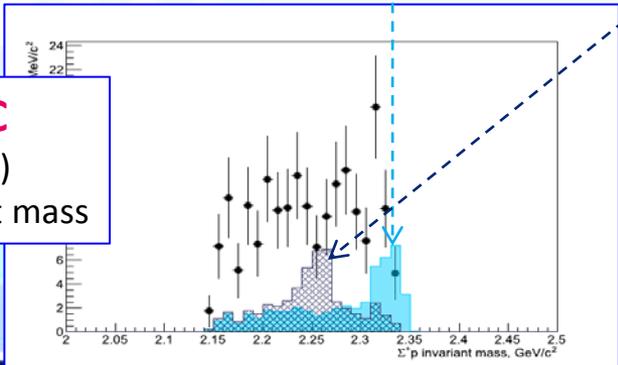
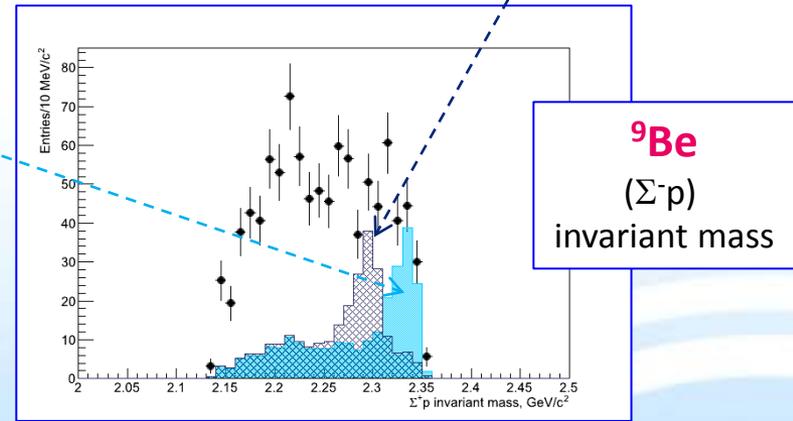
1<sup>st</sup> test: add components with a maximally fragmented system produced in  $\Sigma^-p$  QF

<b><sup>6</sup>Li</b>	A - [np]	<sup>4</sup> He	<sup>3</sup> He + n	d + d	2p + 2n
	Mass(MeV/c <sup>2</sup> )	3727.38	3747.95	3751.23	3755.67

<b><sup>7</sup>Li</b>	A - [np]	<sup>5</sup> He	<sup>4</sup> He + n	t+d	<sup>4</sup> H + p	<sup>3</sup> He + 2n	2p+3n
	Mass(MeV/c <sup>2</sup> )	4667.83	4666.95	4684.55	4689.64	4687.52	4695.24

<b><sup>9</sup>Be</b>	A - [np]	<sup>7</sup> Li	<sup>6</sup> Li + n	<sup>5</sup> Li + 2n	<sup>4</sup> Li + 3n	...	3d+n	3p+4n
	Mass(MeV/c <sup>2</sup> )	6533.83	6541.09	6546.75	6568.46	...	6566.40	6573.08

<b><sup>13</sup>C</b>	A - [np]	<sup>11</sup> B	...	3p + 4n
	Mass(MeV/c <sup>2</sup> )	10252.55		10328.75



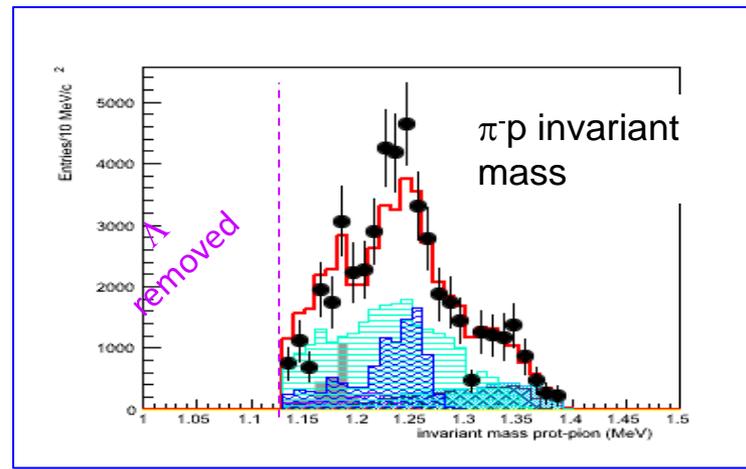
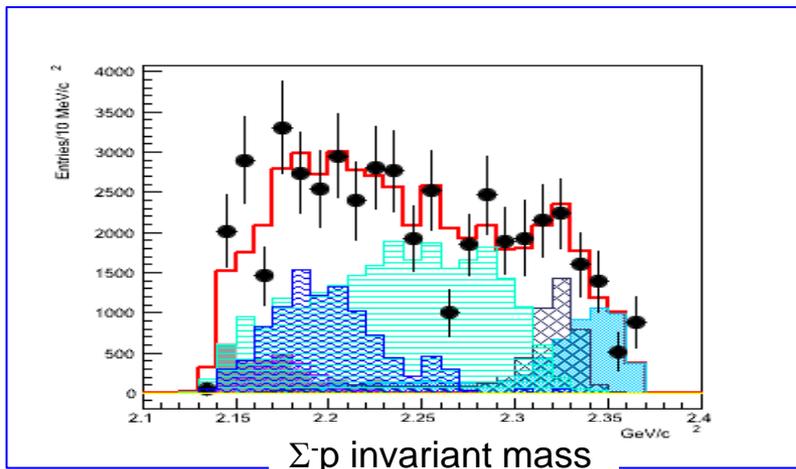
Arbitrary normalizations

Arbitrary normalizations

<b><sup>16</sup>O</b>	A - [np]	<sup>14</sup> C	...	7p + 7n
	Mass(MeV/c <sup>2</sup> )	13040.87		13144.86

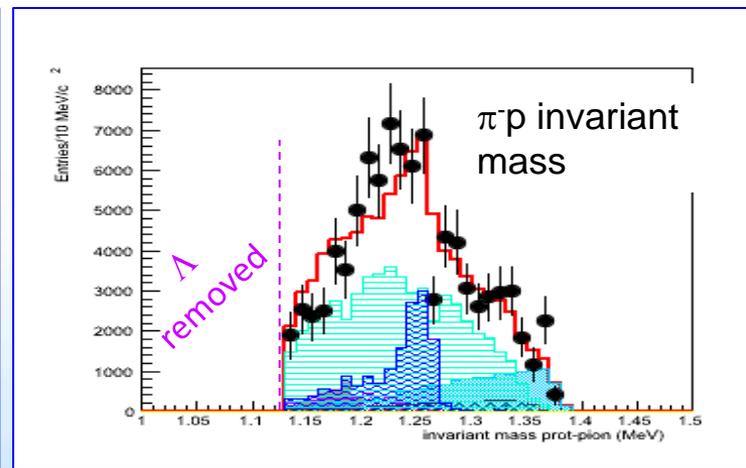
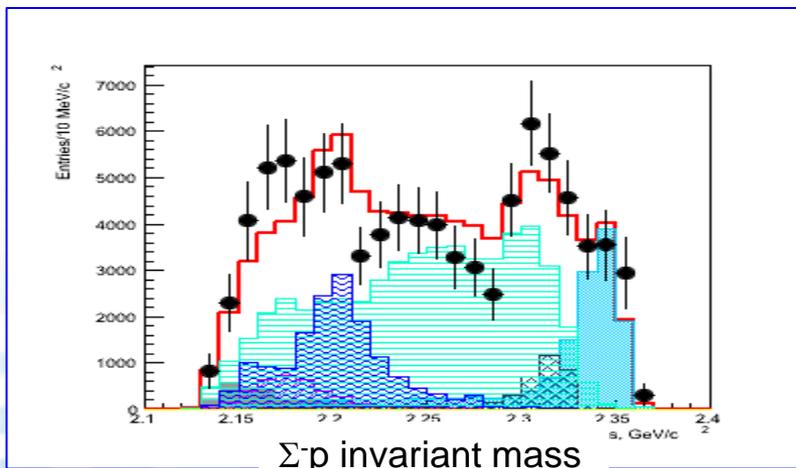
# ${}^6\text{Li}$ , ${}^7\text{Li}$ : fit with QF + recoiling fragmented configuration

(meaningful contributions for lighter targets – heavier: too displaced)



${}^6\text{Li}$

$$\chi^2_{\text{NDF}} = 1.39$$



${}^7\text{Li}$

$$\chi^2_{\text{NDF}} = 1.26$$

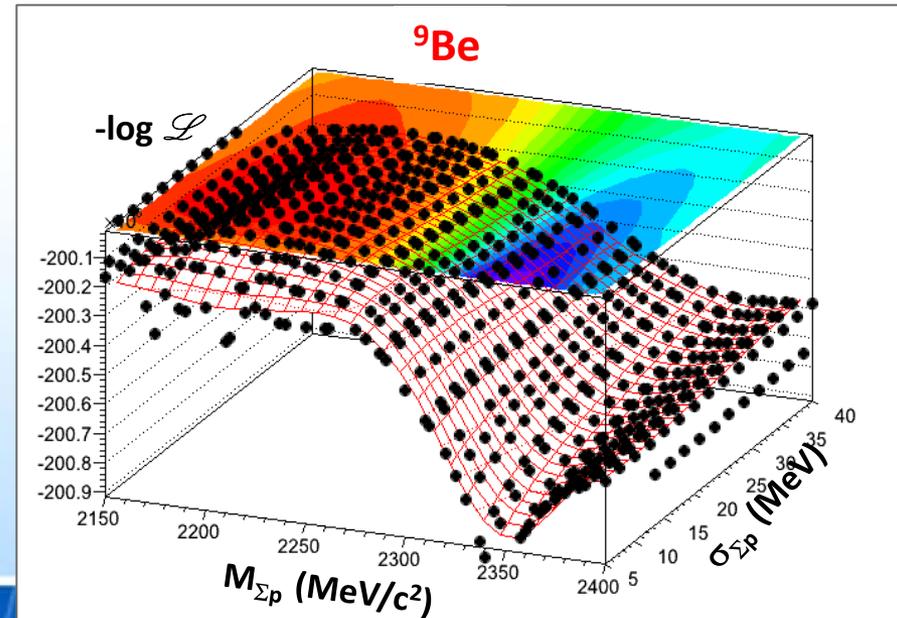
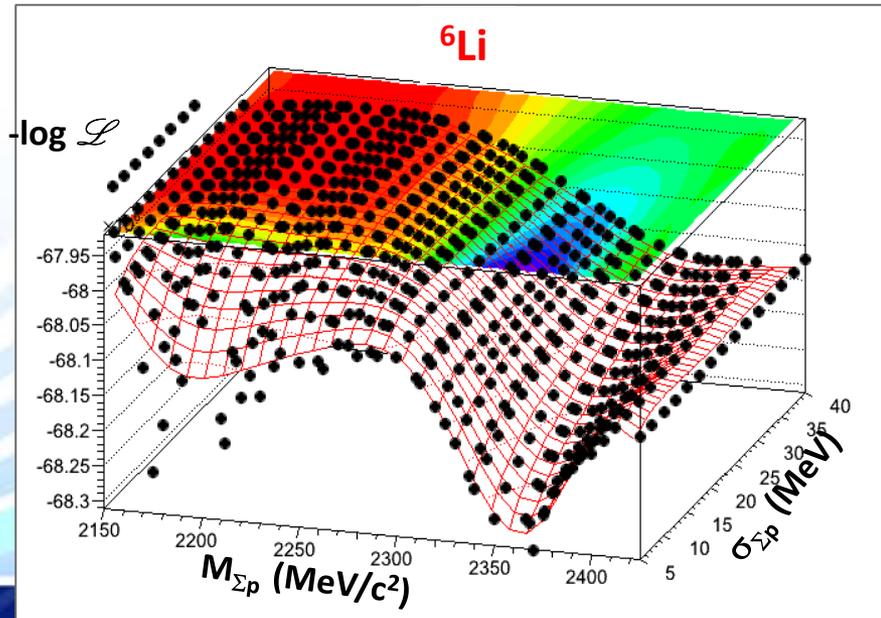
- ${}^6\text{Li}$ : QF reaction recoiling against a totally fragmented system  $\sim 10\%$ , g.s.:  $13\%$
- ${}^7\text{Li}$ : QF reaction recoiling against a totally fragmented system  $\sim 5\%$ , g.s.:  $15\%$
- Clear improvement of the  $(\Sigma$ -p) mass region at  $2320 \text{ MeV}/c^2$ , still imperfect for  $(\pi$ -p)

# Add-on #2: extra component needed?

- Purpose: cusp effect at threshold? More exotic component?
- Additional hypothesis: a  $[K^-pn]$  resonant state decaying into  $\Sigma^-p$
- Parameterized through a Breit-Wigner distribution, with mass  $m_{\Sigma^-p}$  and width  $\Gamma_{\Sigma^-p}$  as floating parameters
- Two approaches:
  - Best fit search over a discrete 2D grid over  $m_{\Sigma^-p}$  and width  $\Gamma_{\Sigma^-p}$ 
    - For each  $(m_{\Sigma^-p}, \Gamma_{\Sigma^-p})$  hypothesis a dedicated simulation must be performed
    - Very time consuming
  - modeling of phase space  $(n\pi^-p)$  events imposing proper kinematic constraints
    - $(n\pi^-) \rightarrow \Sigma^-$
    - Back-to-back  $\Sigma^-p$  angle
    - Missing mass in the proper range
    - $(\Sigma^-p) \rightarrow$  Breit-Wigner with given mass and width, floating on a discrete grid
    - Fast localization of relative and absolute likelihood minima to have a rough indication of the region to be finer-tuned

# $\Sigma^-p$ fits with additional resonant amplitude

- Once the correct minimum region has been spotted, a complete simulation may be performed to look after the effective best fit solution
- General observations:
  - for all targets the fits are **poorly sensitive to the width** of the resonant signal: narrow widths are preferred, all of them within the experimental resolution
  - Two minima: one below 2200 MeV/c<sup>2</sup>, the second (absolute) around 2350 MeV/c<sup>2</sup>

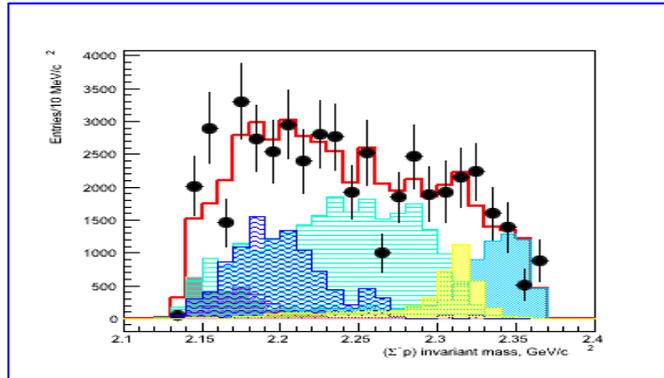


# Fits with QF (g.s. recoil) + [K<sup>-</sup>pn] resonant state

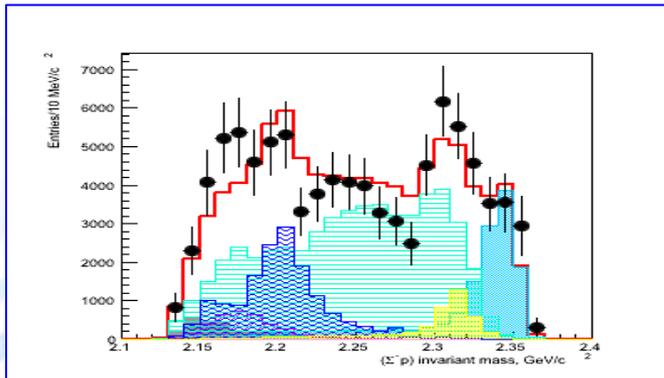
Rather marginal improvements

Statistical significance of  $< 3\sigma$

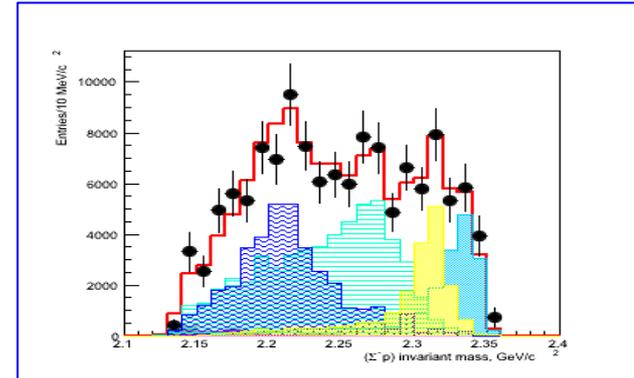
Better for heavier targets



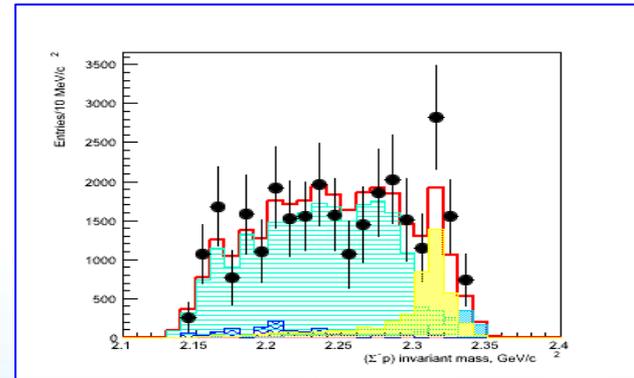
**<sup>6</sup>Li**  
 $\chi^2 = 1.43$   
 Fraction: 8%



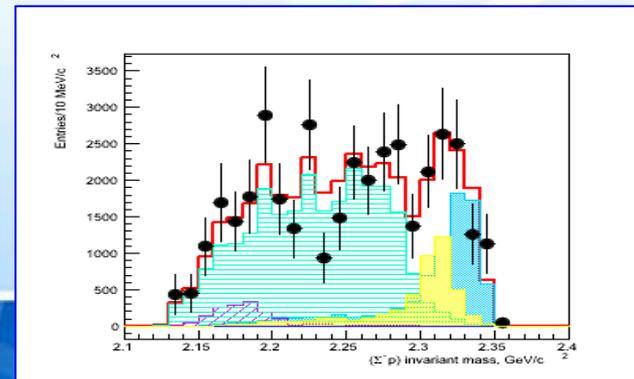
**<sup>7</sup>Li**  
 $\chi^2 = 1.27$   
 Fraction: 5%



**<sup>9</sup>Be**  
 $\chi^2 = 1.56$   
 Fract.: 14%



**<sup>13</sup>C**  
 $\chi^2 = 0.72$   
 Fract.: 14%



**<sup>16</sup>O**  
 $\chi^2 = 0.86$   
 Frac.: 12%

• Best fit (average):

- $m_{\Sigma^-p} = 2320 \pm 5_{st} \pm 10_{sys} \text{ MeV}/c^2$
- $\Gamma_{\Sigma^-p} = 12 \pm 11_{st} \pm 10_{sys} \text{ MeV}/c^2$

# Summary and outlook

- Progress in the study of spectral composition in two-nucleon kaon absorptions on some p-shell nuclei: study of  $\Sigma^-$  emission
- **$K^-[pn] \rightarrow \Sigma^-p$  in several targets**
  - Capture rate evaluations (useful for background estimations)
  - Detailed study of QF contributions to experimental spectra: *global fits* with QF reactions
  - Imperfect fits: several tests for add-on's done and planned
    - Fragmentation/excited recoiling nucleus effect? YES, needed!
      - 3N absorption quite sizeable: try to include 4N ( $\alpha$ ) absorption
    - Resonance in the ( $\Sigma^-p$ ) system? significance  $< 3\sigma$  (not promising)
    - Cusp effect at  $\Sigma N$  and/or  $\Sigma N\pi$  threshold?
    - More complex  $\Sigma/p/\pi$  rescatterings?
- New and interesting information on  $K^-(np)$  absorption dynamics in nuclei