

SPHERE MEETING 2014

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Volodymyr Magas

**Cascade production in antikaon reactions
on nuclei**

In collaboration with **A. Ramos, A. Feijoo Aliau**

University of Barcelona, Spain

Cascade production in antikaon reactions with protons ($K^- p \rightarrow K \Xi$)

Thesis advisors: Volodymyr Magas & Àngels Ramos.

Perturbative QCD, with *quark* and *gluon* d.o.f.,
works well at **high energies** and high momentum transfers,
but **fails** to describe **dynamics of hadrons** at **low energies**

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which is based on **effective Lagrangian** with hadron d.o.f.,
which respects the symmetries of QCD,
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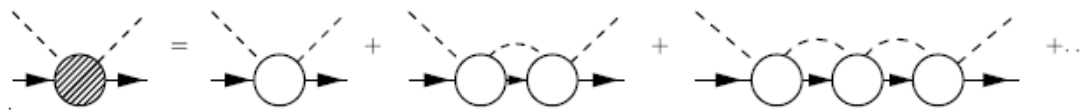
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$S = -1$ sector: $\bar{K}N$ interaction

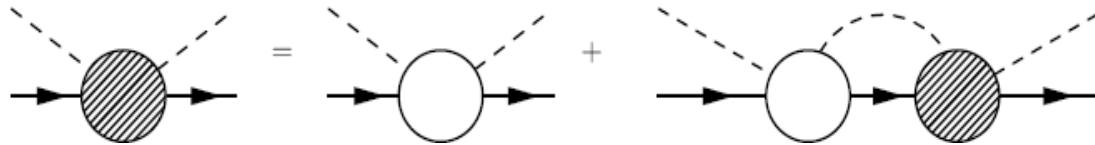
- $\bar{K}N$ scattering in the $I = 0$ channel is dominated by the presence of the $\Lambda(1405)$ resonance, located only 27 MeV below KN threshold \Rightarrow
- χPT is not applicable \Rightarrow
- **non-perturbative techniques implementing unitarization in coupled channels are mandatory!**

➡ **Unitary extension of Chiral Perturbation Theory ($U\chi PT$)**

The pioneering work -- *Kaiser, Siegel, Weise*, NP A594 (1995) 325



Lippmann-Schwinger equation



$$T_{ij} = V_{ij} + V_{il} G_l T_{lj}$$

$$T_{ij}(E; k_i, k_j) = V_{ij}(k_i, k_j) + \sum_k \int d^3 q_k V_{ik}(k_i, q_k) \tilde{G}_k(E; q_k) T_{kj}(E; q_k, k_j)$$

On shell factorization

System of the algebraic equations

$$T_{ij}(E) = V_{ij} + \sum_k V_{ik} G_k(E) T_{kj}(E), \quad \Rightarrow \quad \boxed{T = (1 - VG)^{-1}V}$$

$$G_k(E) = \int d^3 q_k \tilde{G}_k(E; q_k)$$

V_{ij} - interaction kernel to be taken from the chiral Lagrangian

Loop function

G is a diagonal matrix given by the loop function of meson and baryon propagators:

$$G_l = i \int \frac{d^4 q}{(2\pi)^4} \frac{M_l}{E_l(\vec{q})} \frac{1}{\sqrt{s} - q^0 - E_l(\vec{q}) + i\epsilon} \frac{1}{q^2 - m_l^2 + i\epsilon}$$

in which M_l and m_l are the masses of the baryons and mesons respectively.

In the dimensional regularization scheme this is given by

$$\begin{aligned} G_l &= i 2M_l \int \frac{d^4 q}{(2\pi)^4} \frac{1}{(P - q)^2 - M_l^2 + i\epsilon} \frac{1}{q^2 - m_l^2 + i\epsilon} \\ &= \frac{2M_l}{16\pi^2} \left\{ \underbrace{a_l(\mu)}_{\text{circled}} + \ln \frac{M_l^2}{\mu^2} + \frac{m_l^2 - M_l^2 + s}{2s} \ln \frac{m_l^2}{M_l^2} - 2i\pi \frac{q_l}{\sqrt{s}} \right. \\ &\quad \left. + \frac{q_l}{\sqrt{s}} \left[\ln(s - (M_l^2 - m_l^2) + 2q_l\sqrt{s}) + \ln(s + (M_l^2 - m_l^2) + 2q_l\sqrt{s}) \right. \right. \\ &\quad \left. \left. - \ln(s - (M_l^2 - m_l^2) - 2q_l\sqrt{s}) - \ln(s + (M_l^2 - m_l^2) - 2q_l\sqrt{s}) \right] \right\}, \end{aligned}$$

where μ is the scale of dimensional regularization, q_l denotes the three-momentum of the meson or baryon in the CM frame, and a_l are the subtraction constants.

Subtraction constants

$S=-1$ channel there are 10 channels \rightarrow
10 corresponding subtracting constants

$$a_{K^-p}, a_{\bar{K}^0n}, a_{\pi^0\Lambda}, a_{\pi^0\Sigma^0}, a_{\pi^+\Sigma^-}, a_{\pi^-\Sigma^+}, a_{\eta\Lambda}, a_{\eta\Sigma^0}, a_{K^+\Xi^-}, a_{K^0\Xi^0}$$

Taking into account isospin symmetry:

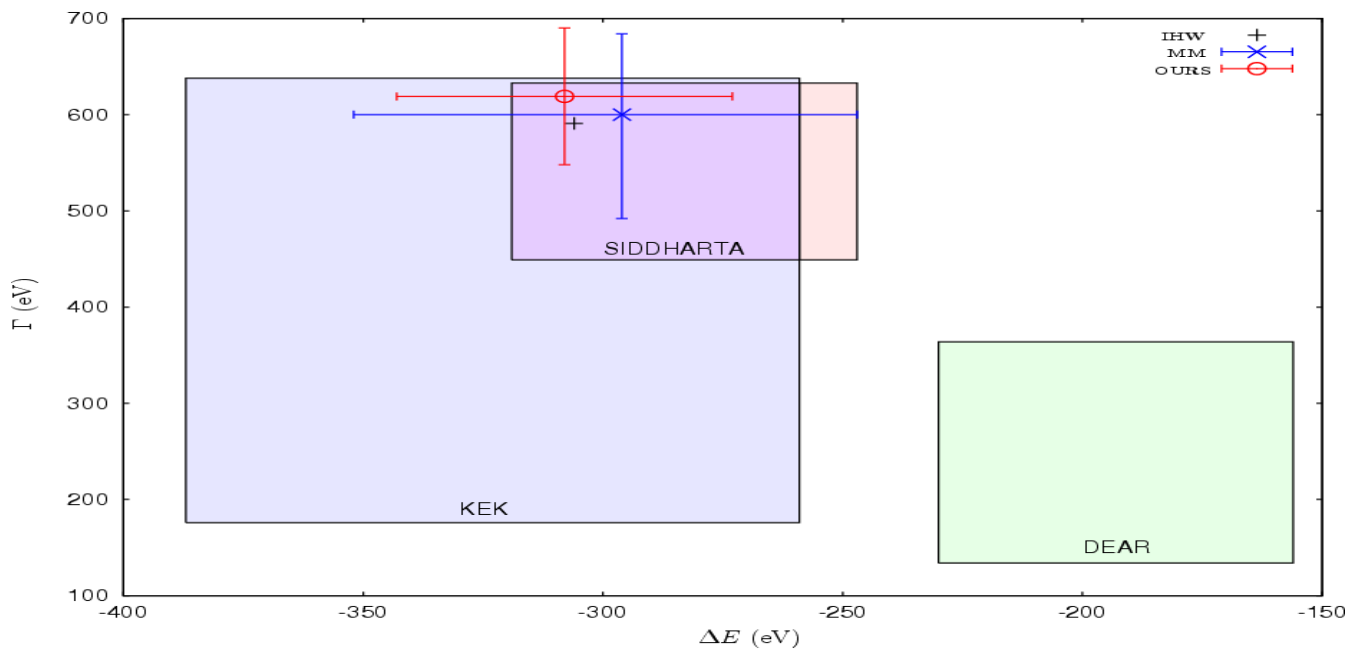
$$\left. \begin{aligned} a_{K^-p} &= a_{\bar{K}^0n} = a_{\bar{K}N} \\ a_{\pi^0\Lambda} &= a_{\pi\Lambda} \\ a_{\pi^0\Sigma^0} &= a_{\pi^+\Sigma^-} = a_{\pi^-\Sigma^+} = a_{\pi\Sigma} \\ a_{\eta\Lambda} \\ a_{\eta\Sigma^0} &= a_{\eta\Sigma} \\ a_{K^+\Xi^-} &= a_{K^0\Xi^0} = a_{K\Xi} \end{aligned} \right\} \boxed{6 \text{ PARAMETERS!}}$$

Recent experimental advances

- The **SIDDHARTA** collaboration at DAΦNE collider has determined the most precise values of shift and width of the 1s state of the kaonic hydrogen induced by the strong interaction.

[M. Bazzi et al, Phys. Lett. B704 (2011) 113]

These measurements allowed us to clarify the discrepancies between KEK and DEAR results for the kaonic hydrogen shift and width of the ground state.



Chiral meson-baryon effective Lagrangian at NLO

Recent Publications:

- B. Borasoy, R. Nißler, W. Wiese, **Eur. Phys. J. A25 (2005) 79**
- Y. Ikeda, T. Hyodo, W. Wiese, **Phys. Lett. B706 (2011) 63;**
Nucl. Phys. A881 (2012) 98
- Z.-H. Guo, J.A. Oller, **Phys. Rev. C87 (2013) 035202**
- M. Mai, U.G. Meissner, **Nucl. Phys. A900 (2013) 51**
- A. Feijoo, **Master Thesis**, U. of Barcelona (Nov 2012)
- A. Feijoo, V. Magas, A. Ramos, **arXiv:1311.5025; arXiv:1402.3971**

FORMALISM

Effective Chiral Lagrangian up to LO

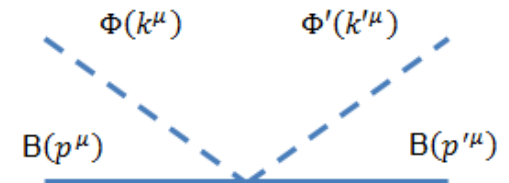
$$\mathcal{L}_{eff}(B, U) = \mathcal{L}_M(U) + \mathcal{L}_{MB}^{(1)}(B, U) \quad \longrightarrow \quad \mathcal{L}_{eff}(B, U) = \mathcal{L}_{MB}^{(1)}(B, U)$$

$$\mathcal{L}_{MB}^{(1)}(B, U) = \langle \bar{B} i \gamma^\mu \nabla_\mu B \rangle - M_B \langle \bar{B} B \rangle + \frac{1}{2} D \langle \bar{B} \gamma^\mu \gamma_5 \{u_\mu, B\} \rangle + \frac{1}{2} F \langle \bar{B} \gamma^\mu \gamma_5 [u_\mu, B] \rangle$$

$$\begin{aligned} \nabla_\mu B &= \partial_\mu B + [\Gamma_\mu, B] \\ \Gamma_\mu &= \frac{1}{2} (u^\dagger \partial_\mu u + u \partial_\mu u^\dagger) \\ U &= u^2 = \exp\left(\frac{i\sqrt{2}\Phi}{f}\right) \\ u_\mu &= i u^\dagger \partial_\mu U u^\dagger \end{aligned} \quad \Phi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta \end{pmatrix} \quad B = \begin{pmatrix} \frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & \Sigma^+ & p \\ \Sigma^- & -\frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & n \\ \Xi^- & \Xi^0 & -\frac{2}{\sqrt{6}}\Lambda \end{pmatrix}$$

- **WT, lowest order term**

$$\mathcal{L}_{MB}^{(1)}(B, U) = \langle \bar{B} i \gamma^\mu \frac{1}{4f^2} [(\Phi \partial_\mu \Phi - \partial_\mu \Phi \Phi) B - B(\Phi \partial_\mu \Phi - \partial_\mu \Phi \Phi)] \rangle$$



$$V_{ij}^{WT} = -C_{ij} \frac{1}{4f^2} \bar{u}(p) \gamma^\mu u(p) (k_\mu + k'_\mu) \quad \xrightarrow{\text{At low energies}} \quad V_{ij}^{WT} = -C_{ij} \frac{1}{4f^2} (k^0 + k'^0)$$

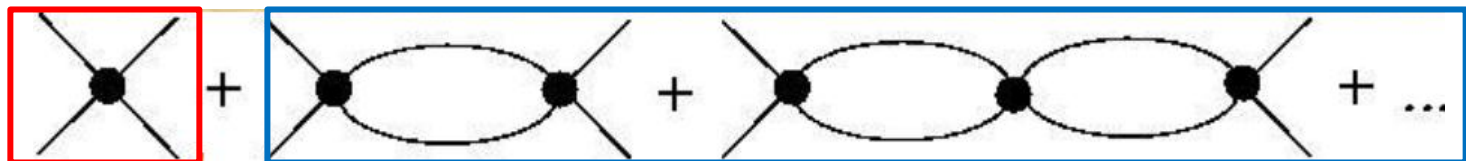
The only model parameter is **pion decay constant, f**

FORMALISM

Effective Chiral Lagrangian up to LO

C_{ij} coefficients are represented as a symmetric matrix where the indices i and j cover all the channels that conform the $S=-1$ sector.

	K^-p	\bar{K}^0n	$\pi^0\Lambda$	$\pi^0\Sigma^0$	$\eta\Lambda$	$\eta\Sigma^0$	$\pi^+\Sigma^-$	$\pi^-\Sigma^+$	$K^+\Xi^-$	$K^0\Xi^0$
K^-p	2	1	$\sqrt{3}/2$	$1/2$	$3/2$	$\sqrt{3}/2$	0	1	0	0
\bar{K}^0n		2	$-\sqrt{3}/2$	$1/2$	$3/2$	$-\sqrt{3}/2$	1	0	0	0
$\pi^0\Lambda$			0	0	0	0	0	0	$\sqrt{3}/2$	$-\sqrt{3}/2$
$\pi^0\Sigma^0$				0	0	0	2	2	$1/2$	$1/2$
$\eta\Lambda$					0	0	0	0	$3/2$	$3/2$
$\eta\Sigma^0$						0	0	0	$\sqrt{3}/2$	$-\sqrt{3}/2$
$\pi^+\Sigma^-$							2	0	1	0
$\pi^-\Sigma^+$								2	0	1
$K^+\Xi^-$									2	1
$K^0\Xi^0$										2



FORMALISM

Effective Chiral Lagrangian up to NLO

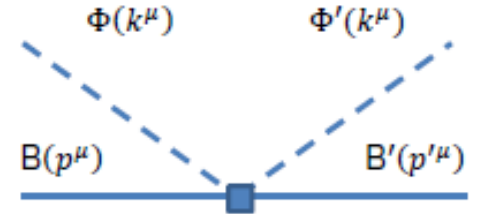
$$\mathcal{L}_{eff}(B, U) = \mathcal{L}_{MB}^{(1)}(B, U) + \mathcal{L}_{MB}^{(2)}(B, U)$$

$$\begin{aligned} \mathcal{L}_{MB}^{(2)}(B, U) = & b_D \langle \bar{B} \{ \chi_+, B \} \rangle + b_F \langle \bar{B} [\chi_+, B] \rangle + b_0 \langle \bar{B} B \rangle \langle \chi_+ \rangle + d_1 \langle \bar{B} \{ u_\mu, [u^\mu, B] \} \rangle \\ & + d_2 \langle \bar{B} [u_\mu, [u^\mu, B]] \rangle + d_3 \langle \bar{B} u_\mu \rangle \langle u^\mu B \rangle + d_4 \langle \bar{B} B \rangle \langle u^\mu u_\mu \rangle \end{aligned}$$

$$\chi = \begin{pmatrix} m_\pi^2 & 0 & 0 \\ 0 & m_\pi^2 & 0 \\ 0 & 0 & 2m_K^2 - m_\pi^2 \end{pmatrix}$$

- NLO, next - to - leading order term

$$\begin{aligned} \mathcal{L}_{MB}^{(2)}(B, U) = & -\frac{b_D}{4f^2} \langle \bar{B} (\Phi^2 \chi + 2\Phi \chi \Phi + \chi \Phi^2) B + \bar{B} B (\Phi^2 \chi + 2\Phi \chi \Phi + \chi \Phi^2) \rangle \\ & -\frac{b_F}{4f^2} \langle \bar{B} (\Phi^2 \chi + 2\Phi \chi \Phi + \chi \Phi^2) B - \bar{B} B (\Phi^2 \chi + 2\Phi \chi \Phi + \chi \Phi^2) \rangle -\frac{b_0}{4f^2} \langle \bar{B} B \rangle \langle \Phi^2 \chi + 2\Phi \chi \Phi + \chi \Phi^2 \rangle + \\ & \frac{2d_1}{f^2} \langle \bar{B} (\partial_\mu \Phi \partial^\mu \Phi B - \partial_\mu \Phi B \partial^\mu \Phi + \partial^\mu \Phi B \partial_\mu \Phi - B \partial^\mu \Phi \partial_\mu \Phi) \rangle + \\ & \frac{2d_2}{f^2} \langle \bar{B} (\partial_\mu \Phi \partial^\mu \Phi B - \partial_\mu \Phi B \partial^\mu \Phi - \partial^\mu \Phi B \partial_\mu \Phi + B \partial^\mu \Phi \partial_\mu \Phi) \rangle + \frac{2d_3}{f^2} \langle \bar{B} \partial_\mu \Phi \rangle \langle \partial^\mu \Phi B \rangle + \frac{2d_4}{f^2} \langle \bar{B} B \rangle \langle \partial^\mu \Phi \partial_\mu \Phi \rangle \end{aligned}$$



$$V_{ij}^{NLO} = \frac{1}{f^2} (D_{ij} - 2(k_\mu k'^\mu) L_{ij}) \sqrt{\frac{M_i + E_i}{2M_i}} \sqrt{\frac{M_j + E_j}{2M_j}}$$

7 new parameters to be fixed: $b_D, b_F, b_0, d_1, d_2, d_3, d_4$

FORMALISM

Effective Chiral Lagrangian up to NLO

D_{ij}

	K^-p	\bar{K}^0n	$\pi^0\Lambda$	$\pi^0\Sigma^0$	$\eta\Lambda$	$\eta\Sigma^0$	$\pi^+\Sigma^-$	$\pi^-\Sigma^+$	$K^+\Xi^-$	$K^0\Xi^0$
K^-p	$4(b_0 + b_D)m_K^2$	$2(b_D + b_F)m_K^2$	$-\frac{(b_D + 3b_F)\mu_1^2}{2\sqrt{3}}$	$\frac{(b_D - b_F)\mu_1^2}{2}$	0	$(b_D - b_F)\mu_1^2$	$\frac{(b_D + 3b_F)\mu_2^2}{6}$	$-\frac{(b_D - b_F)\mu_2^2}{2\sqrt{3}}$	0	0
\bar{K}^0n		$4(b_0 + b_D)m_K^2$	$\frac{(b_D + 3b_F)\mu_1^2}{2\sqrt{3}}$	$\frac{(b_D - b_F)\mu_1^2}{2}$	$(b_D - b_F)\mu_1^2$	0	$\frac{(b_D + 3b_F)\mu_2^2}{6}$	$\frac{(b_D - b_F)\mu_2^2}{2\sqrt{3}}$	0	0
$\pi^0\Lambda$			$\frac{4(3b_0 + b_D)m_\pi^2}{3}$	0	0	0	0	$\frac{4b_D m_\pi^2}{3}$	$-\frac{(b_D - 3b_F)\mu_1^2}{2\sqrt{3}}$	$\frac{(b_D - 3b_F)\mu_1^2}{2\sqrt{3}}$
$\pi^0\Sigma^0$				$4(b_0 + b_D)m_\pi^2$	0	0	$\frac{4b_D m_\pi^2}{3}$	0	$\frac{(b_D + b_F)\mu_1^2}{2}$	$\frac{(b_D + b_F)\mu_1^2}{2}$
$\eta\Lambda$					$4(b_0 + b_D)m_\pi^2$	0	$\frac{4b_D m_\pi^2}{3}$	$\frac{4b_F m_\pi^2}{\sqrt{3}}$	$(b_D + b_F)\mu_1^2$	0
$\eta\Sigma^0$						$4(b_0 + b_D)m_\pi^2$	$\frac{4b_D m_\pi^2}{3}$	$-\frac{4b_F m_\pi^2}{\sqrt{3}}$	0	$(b_D + b_F)\mu_1^2$
$\pi^+\Sigma^-$							$\frac{4(3b_0\mu_3^2 + b_D\mu_4^2)}{9}$	0	$\frac{(b_D - 3b_F)\mu_2^2}{6}$	$\frac{(b_D - 3b_F)\mu_2^2}{6}$
$\pi^-\Sigma^+$								$\frac{4(b_0\mu_3^2 + b_D m_\pi^2)}{3}$	$\frac{(b_D + b_F)\mu_2^2}{2\sqrt{3}}$	$\frac{(b_D + b_F)\mu_2^2}{2\sqrt{3}}$
$K^+\Xi^-$									$4(b_0 + b_D)m_K^2$	$2(b_D - b_F)m_K^2$
$K^0\Xi^0$										$4(b_0 + b_D)m_K^2$

L_{ij}

	K^-p	\bar{K}^0n	$\pi^0\Lambda$	$\pi^0\Sigma^0$	$\eta\Lambda$	$\eta\Sigma^0$	$\pi^+\Sigma^-$	$\pi^-\Sigma^+$	$K^+\Xi^-$	$K^0\Xi^0$
K^-p	$2d_2 + d_3 + 2d_4$	$d_1 + d_2 + d_3$	$-\frac{\sqrt{3}(d_1 + d_2)}{2}$	$\frac{-d_1 - d_2 + 2d_3}{2}$	$-2d_2 + d_3$	$-d_1 + d_2 + d_3$	$\frac{d_1 - 3d_2 + 2d_3}{2}$	$\frac{d_1 - 3d_2}{2\sqrt{3}}$	$-4d_2 + 2d_3$	$-2d_2 + d_3$
\bar{K}^0n		$2d_2 + d_3 + 2d_4$	$\frac{\sqrt{3}(d_1 + d_2)}{2}$	$\frac{-d_1 - d_2 + 2d_3}{2}$	$-d_1 + d_2 + d_3$	$-2d_2 + d_3$	$\frac{d_1 - 3d_2 + 2d_3}{2}$	$-\frac{(d_1 - 3d_2)}{2\sqrt{3}}$	$-2d_2 + d_3$	$-4d_2 + 2d_3$
$\pi^0\Lambda$			$2d_4$	0	0	0	0	d_3	$\frac{\sqrt{3}(d_1 - d_2)}{2}$	$-\frac{\sqrt{3}(d_1 - d_2)}{2}$
$\pi^0\Sigma^0$				$2(d_3 + d_4)$	$-2d_2 + d_3$	$-2d_2 + d_3$	d_3	0	$\frac{d_1 - d_2 + 2d_3}{2}$	$\frac{d_1 - d_2 + 2d_3}{2}$
$\eta\Lambda$					$2d_2 + d_3 + 2d_4$	$-4d_2 + 2d_3$	d_3	$\frac{2d_1}{\sqrt{3}}$	$d_1 + d_2 + d_3$	$-2d_2 + d_3$
$\eta\Sigma^0$						$2d_2 + d_3 + 2d_4$	d_3	$-\frac{2d_1}{\sqrt{3}}$	$-2d_2 + d_3$	$d_1 + d_2 + d_3$
$\pi^+\Sigma^-$							$2(d_3 + d_4)$	0	$-\frac{d_1 - 3d_2 + 2d_3}{2}$	$-\frac{d_1 - 3d_2 + 2d_3}{2}$
$\pi^-\Sigma^+$								$2d_4$	$-\frac{(d_1 + 3d_2)}{2\sqrt{3}}$	$\frac{d_1 + 3d_2}{2\sqrt{3}}$
$K^+\Xi^-$									$2d_2 + d_3 + 2d_4$	$-d_1 + d_2 + d_3$
$K^0\Xi^0$										$2d_2 + d_3 + 2d_4$

FORMALISM

Effective Chiral Lagrangian up to NLO

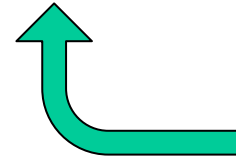
$$V_{ij} = V_{ij}^{WT} + V_{ij}^{NLO} \quad \longrightarrow \quad T = (1 - VG)^{-1}V \quad \longrightarrow \quad T_{ij}^{NLO}$$

Fitting parameters:

- Decay constant **f**
Its usual value, in real calculations, is between $1.15 - 1.2 f_{\pi}^{exp}$ in order to simulate effects of higher order corrections . ($f_{\pi}^{exp}=93.4\text{MeV}$)
- 6 subtracting constants **$a_{\bar{K}N}$, $a_{\pi\Lambda}$, $a_{\pi\Sigma}$, $a_{\eta\Lambda}$, $a_{\eta\Sigma}$, $a_{K\Xi}$**
These terms came from the regularization of the loop in LS equations.
Isospin symmetry is taken into account.
- 7 coefficients of the NLO lagrangian terms **$b_0, b_D, b_F, d_1, d_2, d_3, d_4$**

Experimental data

- Cross sections for different channels



$$\sigma_{ij} = \frac{1}{4\pi} \frac{MM'}{s} \frac{k'}{k} |\mathbf{T}_{ij}|^2$$

- Branching ratios

$$\gamma = \frac{\Gamma(K^- p \rightarrow \pi^+ \Sigma^-)}{\Gamma(K^- p \rightarrow \pi^- \Sigma^+)} = \frac{\sigma_{\pi^+ \Sigma^- \rightarrow K^- p}}{\sigma_{\pi^- \Sigma^+ \rightarrow K^- p}}$$

$$R_n = \frac{\Gamma(K^- p \rightarrow \pi^0 \Lambda)}{\Gamma(K^- p \rightarrow \text{neutral states})} = \frac{\sigma_{\pi^0 \Lambda \rightarrow K^- p}}{\sigma_{\pi^0 \Lambda \rightarrow K^- p} + \sigma_{\pi^0 \Sigma^0 \rightarrow K^- p}}$$

$$R_c = \frac{\Gamma(K^- p \rightarrow \pi^+ \Sigma^-, \pi^- \Sigma^+)}{\Gamma(K^- p \rightarrow \text{inelastic channels})} = \frac{\sigma_{\pi^+ \Sigma^- \rightarrow K^- p} + \sigma_{\pi^- \Sigma^+ \rightarrow K^- p}}{\sigma_{\pi^+ \Sigma^- \rightarrow K^- p} + \sigma_{\pi^- \Sigma^+ \rightarrow K^- p} + \sigma_{\pi^0 \Lambda \rightarrow K^- p} + \sigma_{\pi^0 \Sigma^0 \rightarrow K^- p}}$$

$K^-p \rightarrow K\Xi$ channels

These are particularly interesting for us, because

$K^-p \rightarrow K\Xi$ channels are very sensitive to
the NLO terms in the Lagrangian

Also these channels are not included in the other fits!

B. Borasoy, R. Nißler, W. Wiese, **Eur. Phys. J. A**25 (2005) 79

Y. Ikeda, T. Hyodo, W. Wiese, **Phys. Lett. B**706 (2011) 63; **Nucl. Phys. A**881 (2012) 98

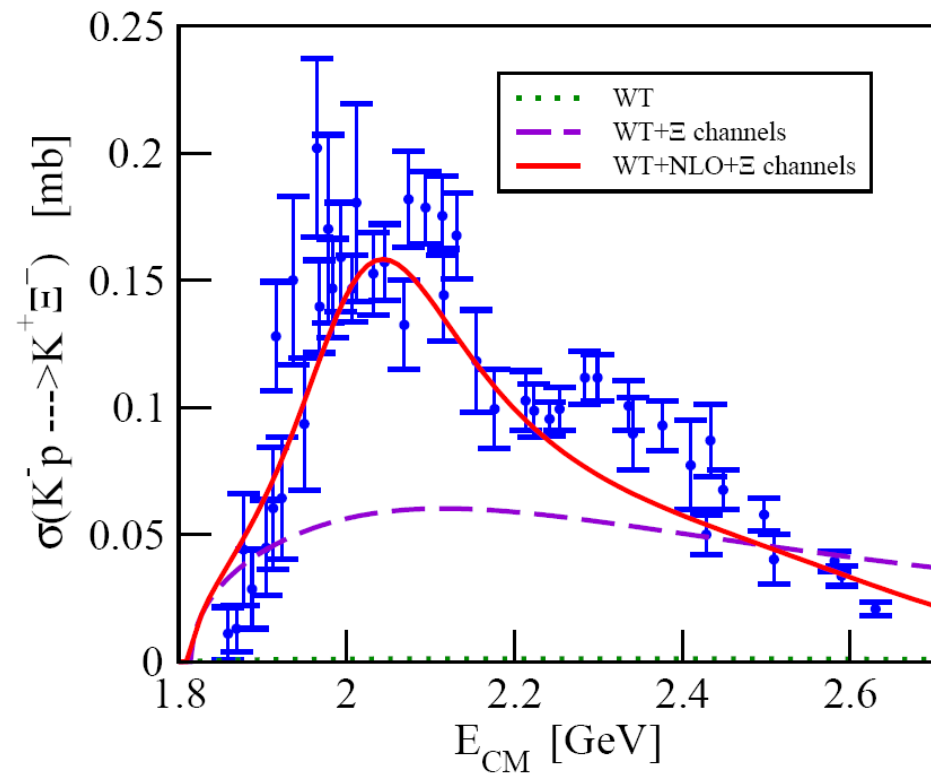
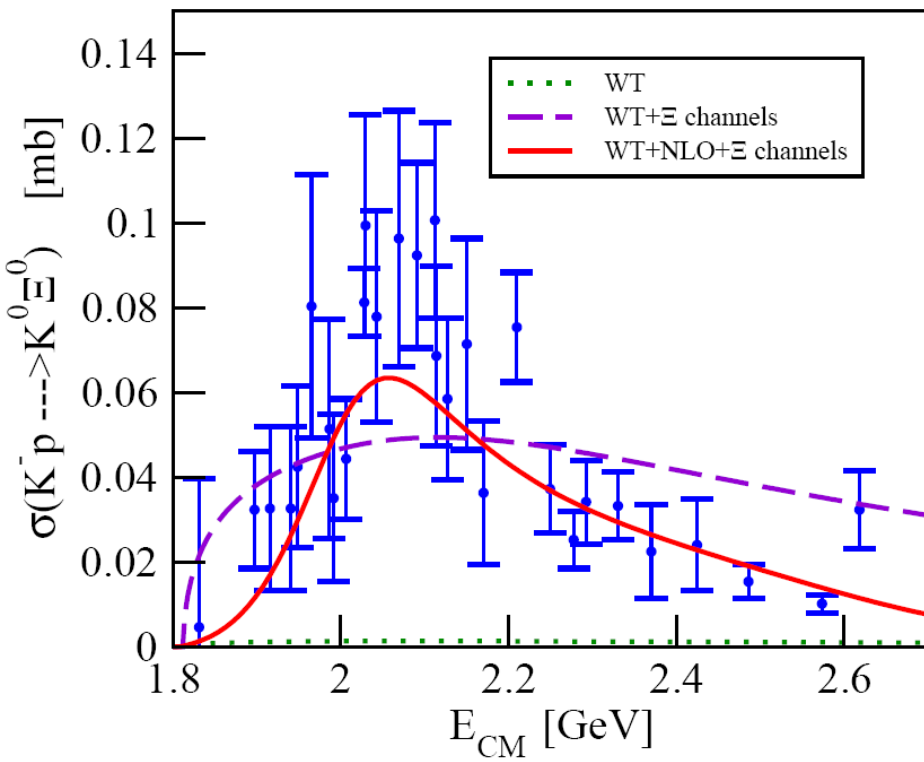
Z.-H. Guo, J.A. Oller, **Phys. Rev. C**87 (2013) 035202

M. Mai, U.G. Meissner, **Nucl. Phys. A**900 (2013) 51

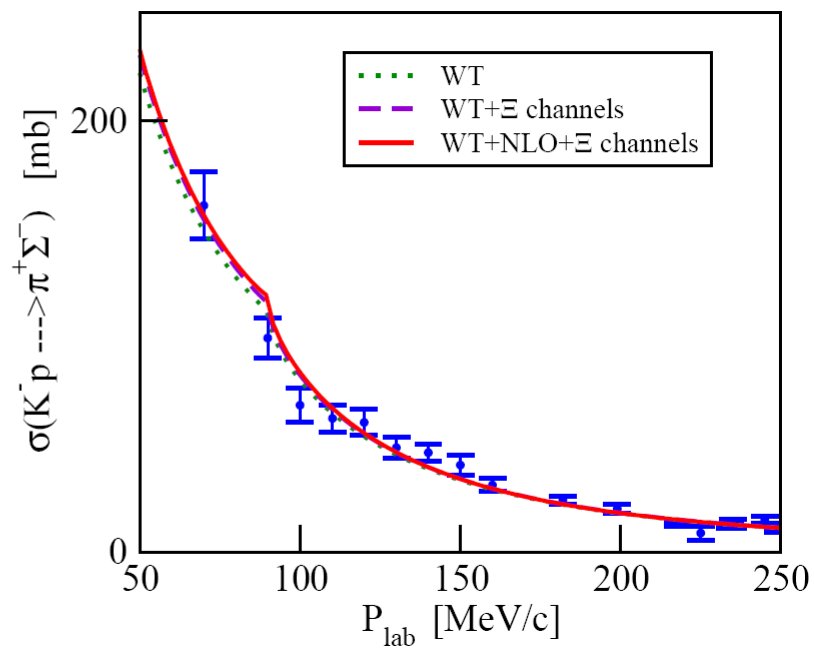
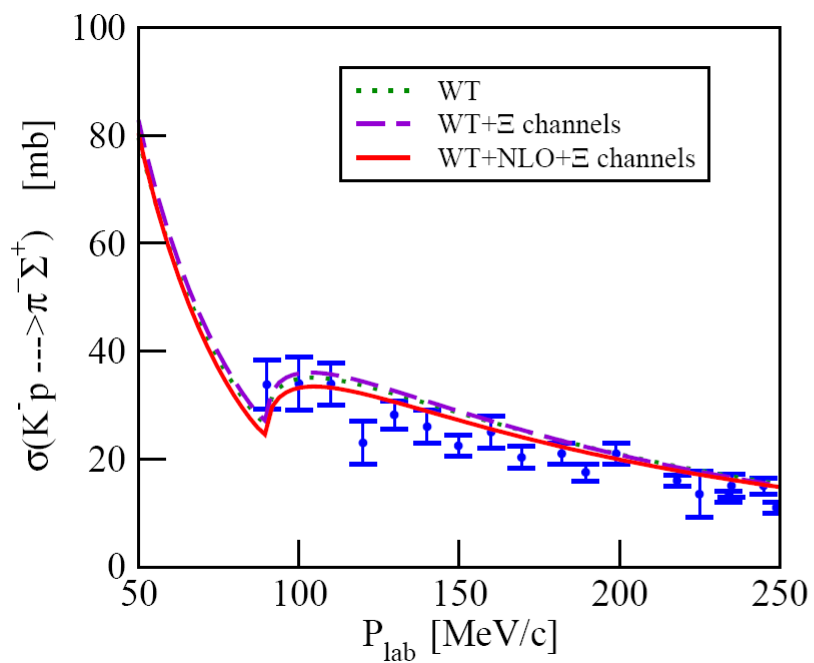
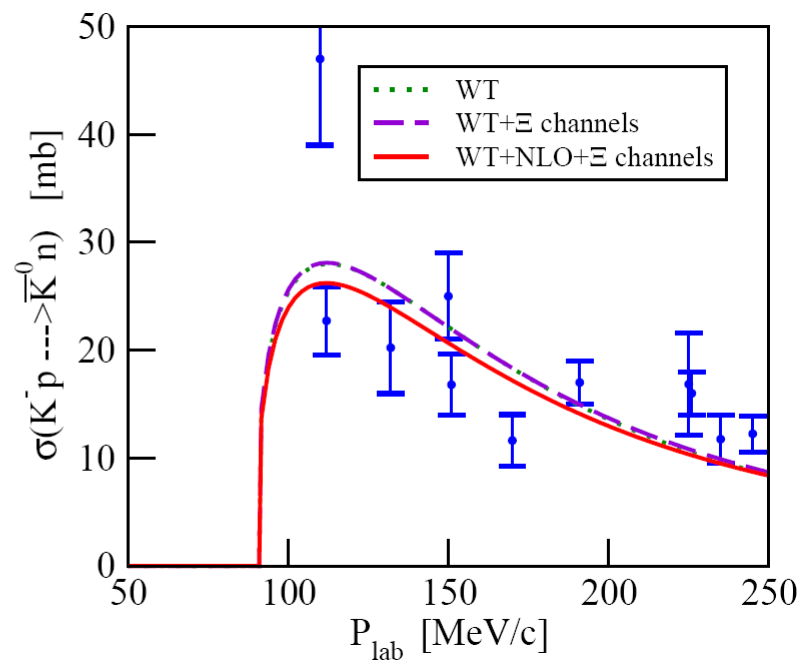
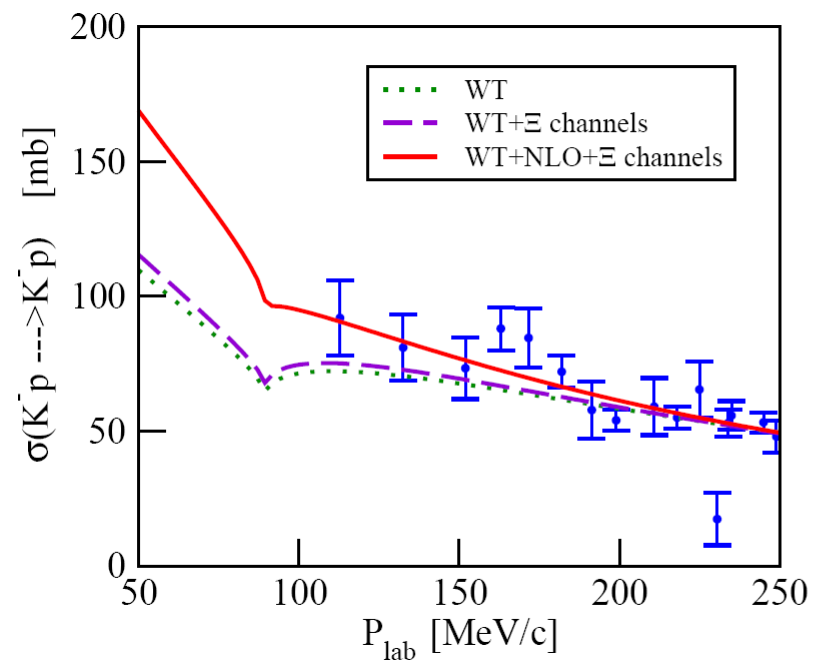
But studied in phenomenological model of

D. A. Sharov, V. L. Korotkikh, D. E. Lanskoy, **Eur. Phys. J. A**47 (2011) 109

$K^-p \rightarrow K\Xi$ channels



Results 1



Results 1

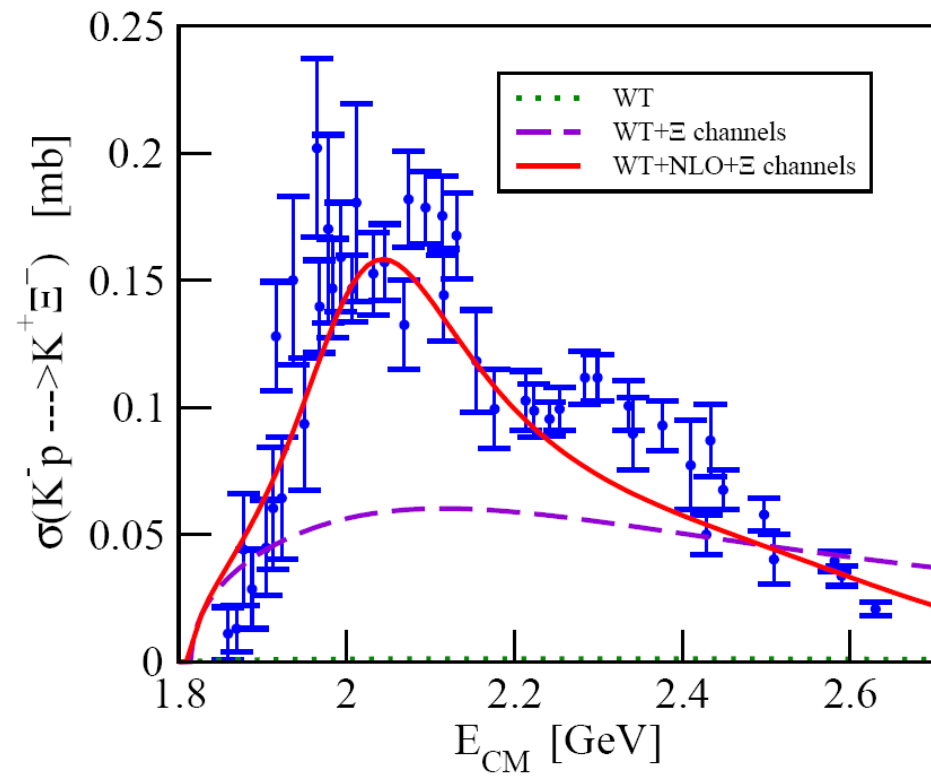
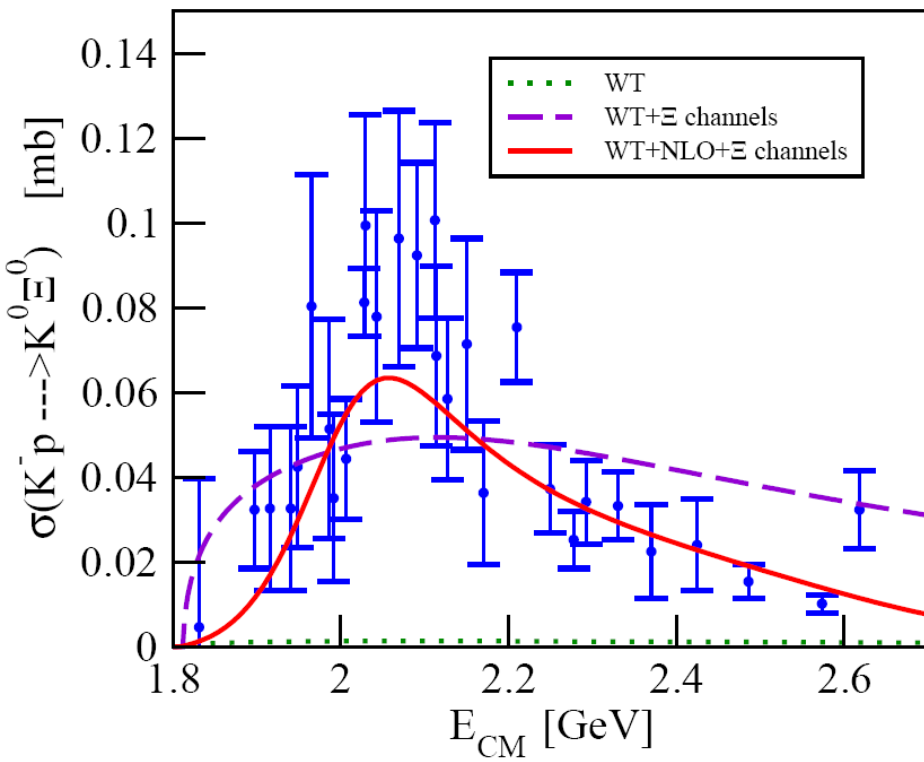
- Branching ratios*

MODEL	γ	R_n	R_c
WT	2.34	0.185	0.665
WT+ Ξ channels	2.30	0.185	0.665
WT+ NLO+ Ξ channels	2.31	0.186	0.660
Experimental	2.36 ± 0.04	0.189 ± 0.015	0.664 ± 0.011

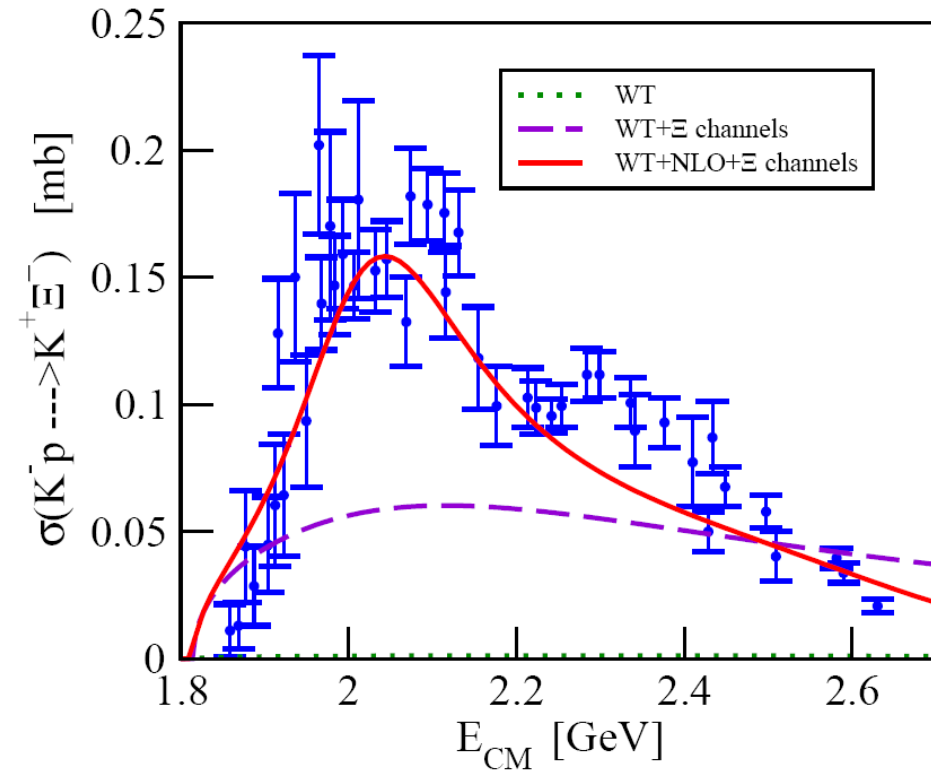
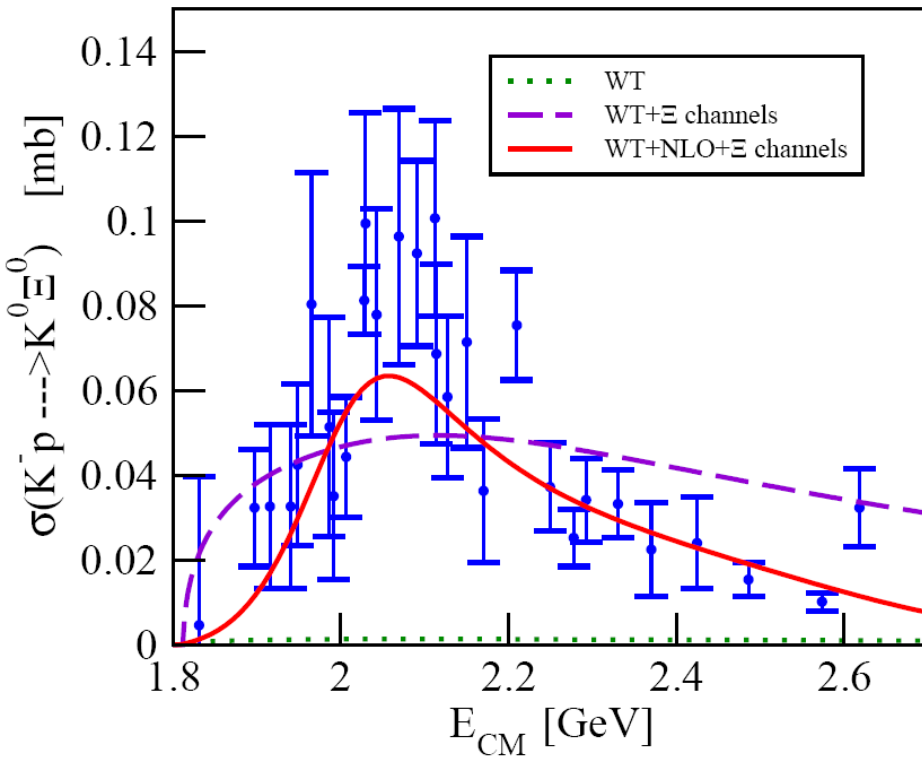
Fitting parameters 1

	WT	WT+ Ξ channels	WT+ NLO+ Ξ channels
$a_{\bar{K}N}$ (10^{-3})	-1.79	-1.95	4.13
$a_{\pi\Lambda}$ (10^{-3})	-39.83	-222.69	26.03
$a_{\pi\Sigma}$ (10^{-3})	0.06	0.40	0.37
$a_{\eta\Lambda}$ (10^{-3})	1.18	1.49	4.50
$a_{\eta\Sigma}$ (10^{-3})	38.04	247.17	-16.00
$a_{K\Xi}$ (10^{-3})	239.0	32.26	51.60
f (MeV)	$1.21f_\pi$	$1.21f_\pi$	$1.21f_\pi$
b_0 (GeV^{-1})	—	—	-0.58
b_D (GeV^{-1})	—	—	0.28
b_F (GeV^{-1})	—	—	0.39
d_1 (GeV^{-1})	—	—	0.36
d_2 (GeV^{-1})	—	—	0.49
d_3 (GeV^{-1})	—	—	0.95
d_4 (GeV^{-1})	—	—	-0.68
$\chi^2_{d.o.f.}$	1.23 (no Ξ !)	3.56	1.79

$K^-p \rightarrow K\Xi$ channels

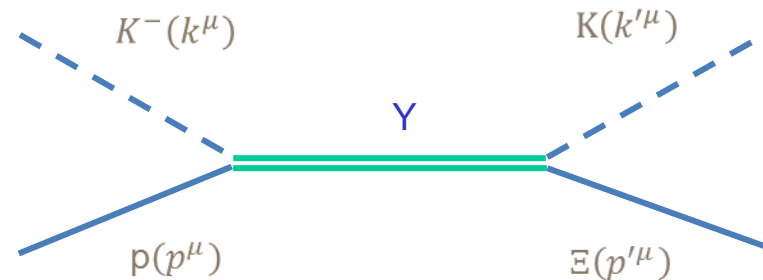


$K^- p \rightarrow K \Xi$ channels



- Missing contribution from the heavy high spin resonances

$$K^- p \rightarrow Y \rightarrow K \Xi$$



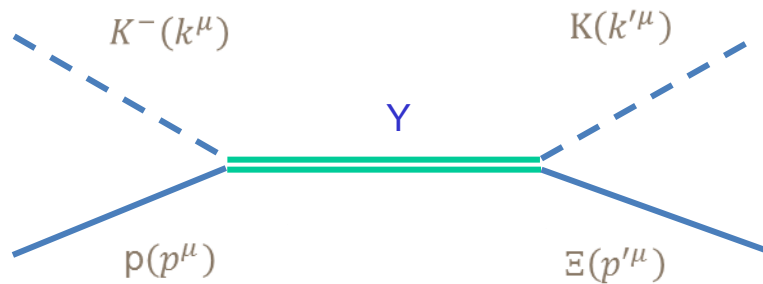
$K^-p \rightarrow K\Xi$ channels

Resonancia	$I(J^P)$	Mass (MeV)	Γ (MeV)	Fraction ($\Gamma_{K\Xi}/\Gamma$)
$\Lambda(1890)$	$0\left(\frac{3^+}{2}\right)$	1850 – 1910	60 – 200	–
$\Lambda(2100)$	$0\left(\frac{7^-}{2}\right)$	2090 – 2110	100 – 250	< 3%
$\Lambda(2110)$	$0\left(\frac{5^+}{2}\right)$	2090 – 2140	150 – 250	–
$\Lambda(2350)$	$0\left(\frac{9^+}{2}\right)$	2340 – 2370	100 – 250	–
$\Sigma(1915)$	$1\left(\frac{5^+}{2}\right)$	1900 – 1935	80 – 160	–
$\Sigma(1940)$	$1\left(\frac{3^-}{2}\right)$	1900 – 1950	150 – 300	–
$\Sigma(2030)$	$1\left(\frac{7^+}{2}\right)$	2025 – 2040	150 – 200	< 2%
$\Sigma(2250)$	$1\left(\frac{5^-}{2}\right)$	2210 – 2280	60 – 150	–

Sharov, Korotkikh, Lanskoj, EPJ A47 (11) 109:

trying different combinations, the author conclude that $\Sigma(2030)$ and $\Sigma(2250)$ give the better fit to the data

Inclusion of hyperonic resonances in $K^-p \rightarrow K\Xi$ channels



K. Nakayama, Y. Oh, H. Habertzettl, Phys. Rev. C74, 035205 (2006)
K. Shing Man, Y. Oh, K. Nakayama, Phys. Rev. C83, 055201 (2011)

$$Y = \Sigma(2030), \Sigma(2250)$$

$$\Sigma(2030), J^P = \frac{7}{2}^+, T^{7/2^+}$$

$$\mathcal{L}_{BYK}^{7/2^\pm}(q) = -\frac{g_{BY_{7/2}K}}{m_K^3} \bar{B} \Gamma^{(\mp)} Y_{7/2}^{\mu\nu\alpha} \partial_\mu \partial_\nu \partial_\alpha K + H.c.$$

$$v_{BYK}^{7/2^\pm} = -\frac{g_{BY_{7/2}K}}{m_K^3} k_\mu k_\nu k_\sigma \Gamma^{(\mp)}$$

$$S_{7/2}(q) = \frac{i}{\not{q} - M_{Y_{7/2}} + i\Gamma_{7/2}/2} \Delta_{\alpha_1\alpha_2\alpha_3}^{\beta_1\beta_2\beta_3}$$

$$\Sigma(2250), J^P = \frac{5}{2}^-, T^{5/2^-}$$

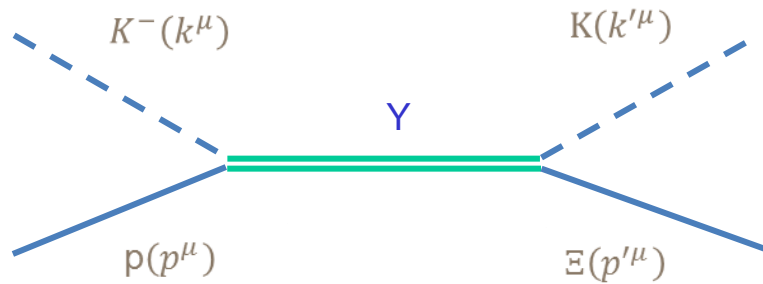
$$\mathcal{L}_{BYK}^{5/2^\pm}(q) = i\frac{g_{BY_{5/2}K}}{m_K^2} \bar{B} \Gamma^{(\pm)} Y_{5/2}^{\mu\nu} \partial_\mu \partial_\nu K + H.c.$$

$$v_{BYK}^{5/2^\pm} = i\frac{g_{BY_{5/2}K}}{m_K^2} k_\mu k_\nu \Gamma^{(\pm)}$$

$$S_{5/2}(q) = \frac{i}{\not{q} - M_{Y_{5/2}} + i\Gamma_{5/2}/2} \Delta_{\alpha_1\alpha_2}^{\beta_1\beta_2}$$

$$\Gamma^{(\pm)} = \begin{pmatrix} \gamma_5 \\ 1 \end{pmatrix}$$

Inclusion of hyperonic resonances in $K^-p \rightarrow K\Xi$ channels



K. Nakayama, Y. Oh, H. Habertzettl, Phys. Rev. C74, 035205 (2006)
K. Shing Man, Y. Oh, K. Nakayama,, Phys. Rev. C83, 055201 (2011)

$$Y = \Sigma(2030), \Sigma(2250)$$

$$\Sigma(2030), J^P = \frac{7}{2}^+, T^{7/2^+}$$

$$S_{5/2}(p) = \frac{i}{\not{p} - m_R + i\Gamma/2} \Delta_{\alpha_1 \alpha_2}^{\beta_1 \beta_2},$$

$$\Sigma(2250), J^P = \frac{5}{2}^-, T^{5/2^-}$$

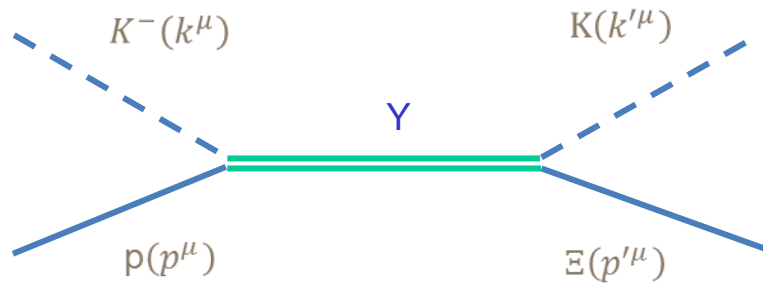
$$S_{7/2}(p) = \frac{i}{\not{p} - m_R + i\Gamma/2} \Delta_{\alpha_1 \alpha_2 \alpha_3}^{\beta_1 \beta_2 \beta_3}$$

$$\Delta_{\alpha_1 \alpha_2}^{\beta_1 \beta_2}(\frac{5}{2}) = \frac{1}{2} \left(\theta_{\alpha_1}^{\beta_1} \theta_{\alpha_2}^{\beta_2} + \theta_{\alpha_1}^{\beta_2} \theta_{\alpha_2}^{\beta_1} \right) - \frac{1}{5} \theta_{\alpha_1 \alpha_2} \theta^{\beta_1 \beta_2} - \frac{1}{10} \left(\bar{\gamma}_{\alpha_1} \bar{\gamma}^{\beta_1} \theta_{\alpha_2}^{\beta_2} + \bar{\gamma}_{\alpha_1} \bar{\gamma}^{\beta_2} \theta_{\alpha_2}^{\beta_1} + \bar{\gamma}_{\alpha_2} \bar{\gamma}^{\beta_1} \theta_{\alpha_1}^{\beta_2} + \bar{\gamma}_{\alpha_2} \bar{\gamma}^{\beta_2} \theta_{\alpha_1}^{\beta_1} \right)$$

$$\Delta_{\alpha_1 \alpha_2 \alpha_3}^{\beta_1 \beta_2 \beta_3}(\frac{7}{2}) = \frac{1}{36} \sum_{P(\alpha), P(\beta)} \left\{ \theta_{\alpha_1}^{\beta_1} \theta_{\alpha_2}^{\beta_2} \theta_{\alpha_3}^{\beta_3} - \frac{3}{7} \theta_{\alpha_1}^{\beta_1} \theta_{\alpha_2 \alpha_3} \theta^{\beta_2 \beta_3} - \frac{3}{7} \bar{\gamma}_{\alpha_1} \bar{\gamma}^{\beta_1} \theta_{\alpha_2}^{\beta_2} \theta_{\alpha_3}^{\beta_3} + \frac{3}{35} \bar{\gamma}_{\alpha_1} \bar{\gamma}^{\beta_1} \theta_{\alpha_2 \alpha_3} \theta^{\beta_2 \beta_3} \right\},$$

$$\theta_\mu^\nu = g_\mu^\nu - \frac{p_\mu p^\nu}{M^2}, \quad \bar{\gamma}_\mu = \gamma_\mu - \frac{p_\mu \not{p}}{M^2}$$

Inclusion of hyperonic resonances in $K^-p \rightarrow K\Xi$ channels



$$Y = \Sigma(2030), \Sigma(2250)$$

Finally, the scattering amplitudes related to the resonances can be obtained in the following way :

$$T^{5/2^-}(s', s) = \frac{g_{\Xi Y_{5/2} K} g_{N Y_{5/2} \bar{K}}}{m_K^4} \bar{u}_{\Xi}'(p') \frac{k'_{\beta_1} k'_{\beta_2} \Delta_{\alpha_1 \alpha_2}^{\beta_1 \beta_2} k^{\alpha_1} k^{\alpha_2}}{\not{q} - M_{Y_{5/2}} + i\Gamma_{5/2}/2} u_N^s(p) \exp\left(-\vec{k}^2 / \Lambda_{5/2}^2\right) \exp\left(-\vec{k}'^2 / \Lambda_{5/2}^2\right)$$

$$T^{7/2^+}(s', s) = \frac{g_{\Xi Y_{7/2} K} g_{N Y_{7/2} \bar{K}}}{m_K^6} \bar{u}_{\Xi}'(p') \frac{k'_{\beta_1} k'_{\beta_2} k'_{\beta_3} \Delta_{\alpha_1 \alpha_2 \alpha_3}^{\beta_1 \beta_2 \beta_3} k^{\alpha_1} k^{\alpha_2} k^{\alpha_3}}{\not{q} - M_{Y_{7/2}} + i\Gamma_{7/2}/2} u_N^s(p) \exp\left(-\vec{k}^2 / \Lambda_{7/2}^2\right) \exp\left(-\vec{k}'^2 / \Lambda_{7/2}^2\right)$$

Note that a form factor has been included in each vertex of the diagram, we chose exponential form factor due to the high dependence in momentum of the scattering amplitudes.

Inclusion of hyperonic resonances in $K^-p \rightarrow K\Xi$ channels

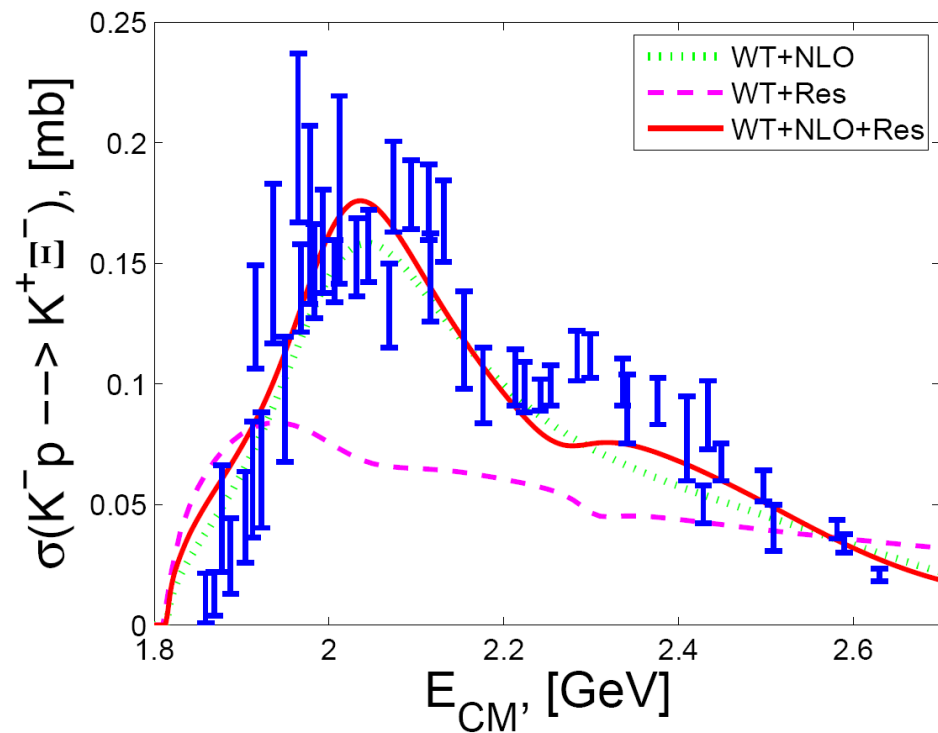
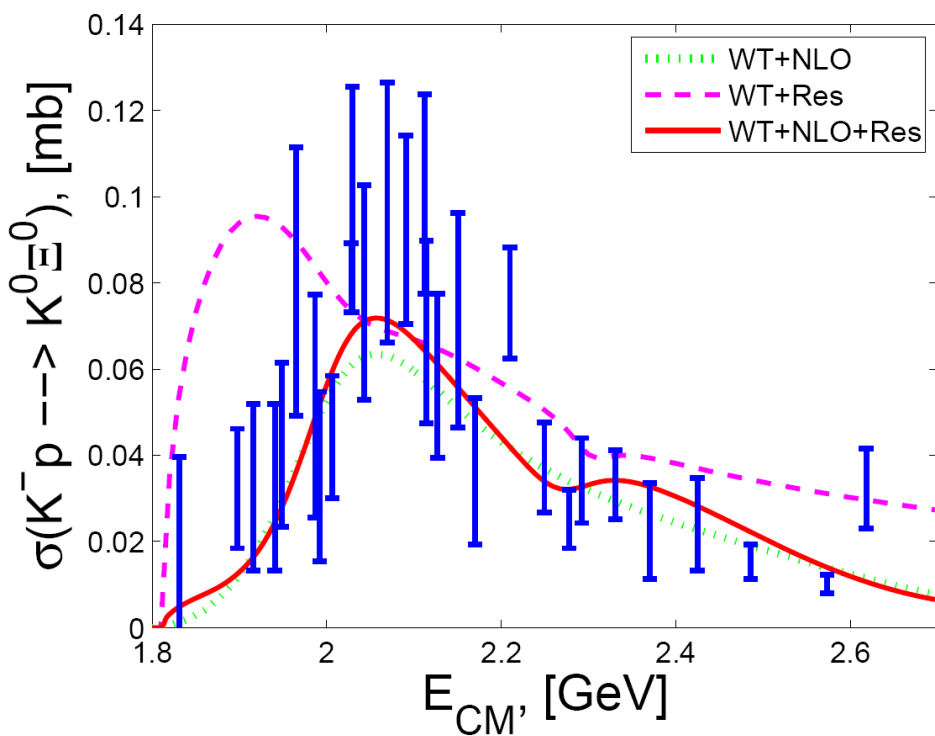
Taking into account the scattering amplitude given by LS equations for a NLO Chiral Lagrangian and the phenomenological contributions from the resonances, the total scattering amplitude for the $\bar{K}N \rightarrow K\Xi$ reaction should be written as:

$$T_{ij,s,s'}^{tot} = T_{ij,s,s'}^{LS} + T_{s,s'}^{5/2^-} + T_{s,s'}^{7/2^+}$$

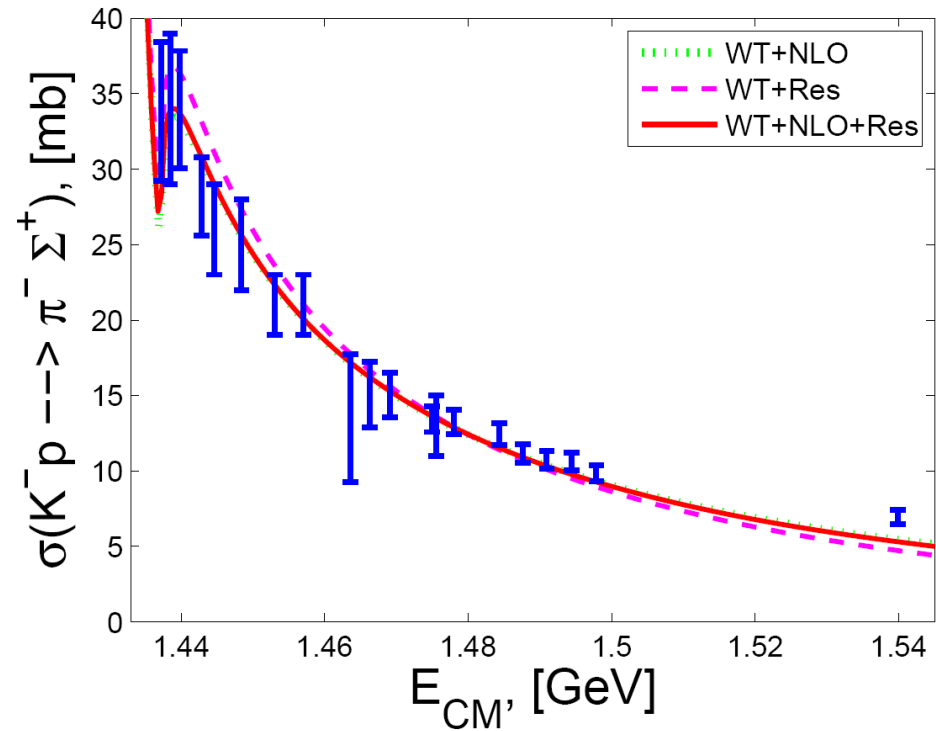
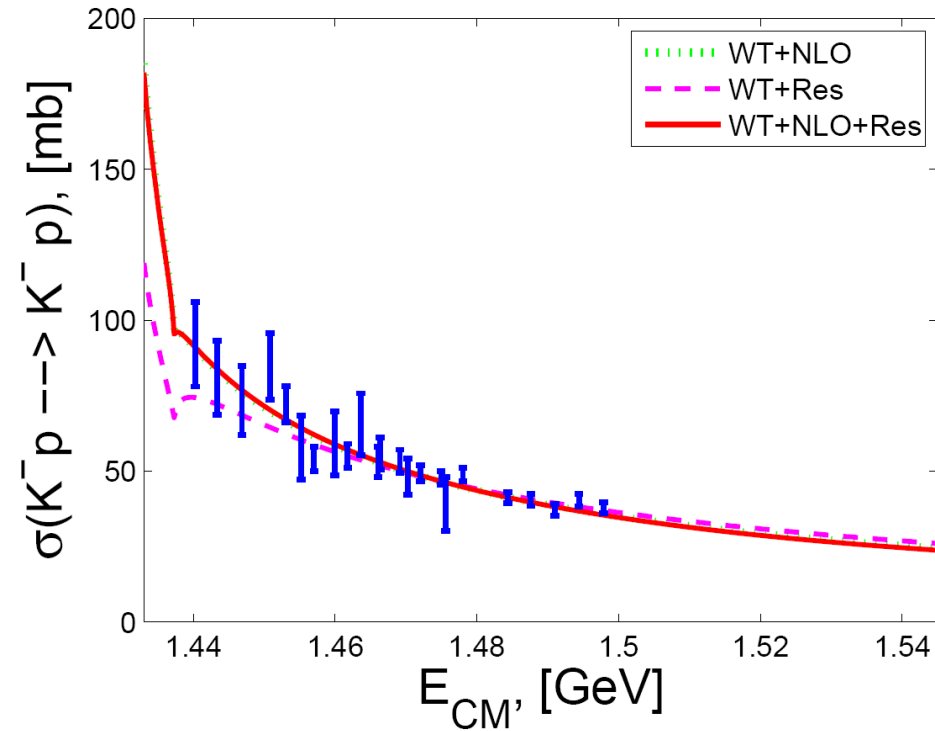
Fitting parameters:

- Decay constant f
Its usual value, in real calculations, is between $1.15 - 1.2 f_{\pi}^{exp}$ in order to simulate effects of higher order corrections . ($f_{\pi}^{exp}=93.4\text{MeV}$)
- Subtracting constants $a_{\bar{K}N}$, $a_{\pi\Lambda}$, $a_{\pi\Sigma}$, $a_{\eta\Lambda}$, $a_{\eta\Sigma}$, $a_{K\Xi}$
These terms came from the regularization of the loop in LS equations.
Isospin symmetry is taken into account.
- Coefficients of the NLO lagrangian terms $b_0, b_D, b_F, d_1, d_2, d_3, d_4$
- Masses and width of the resonances $M_{Y_{5/2}}, M_{Y_{7/2}}, \Gamma_{5/2}, \Gamma_{7/2}$
Not free at all, their values are constrained according to PDG summary
- Cutoff parameters from the form factor $\Lambda_{5/2}, \Lambda_{7/2}$
- Product of the coupling constants (one for each vertex) for both resonances
 $g_{\Xi Y_{5/2} K} \cdot g_{N Y_{5/2} \bar{K}} , g_{\Xi Y_{7/2} K} \cdot g_{N Y_{7/2} \bar{K}}$

Results 2



Results 2



• Branching ratios

MODEL	γ	R_n	R_c
WT +RES	2.48	0.202	0.667
WT+ NLO	2.31	0.186	0.660
WT+NLO+RES	2.50	0.188	0.664
Experimental	2.36 ± 0.04	0.189 ± 0.015	0.664 ± 0.011

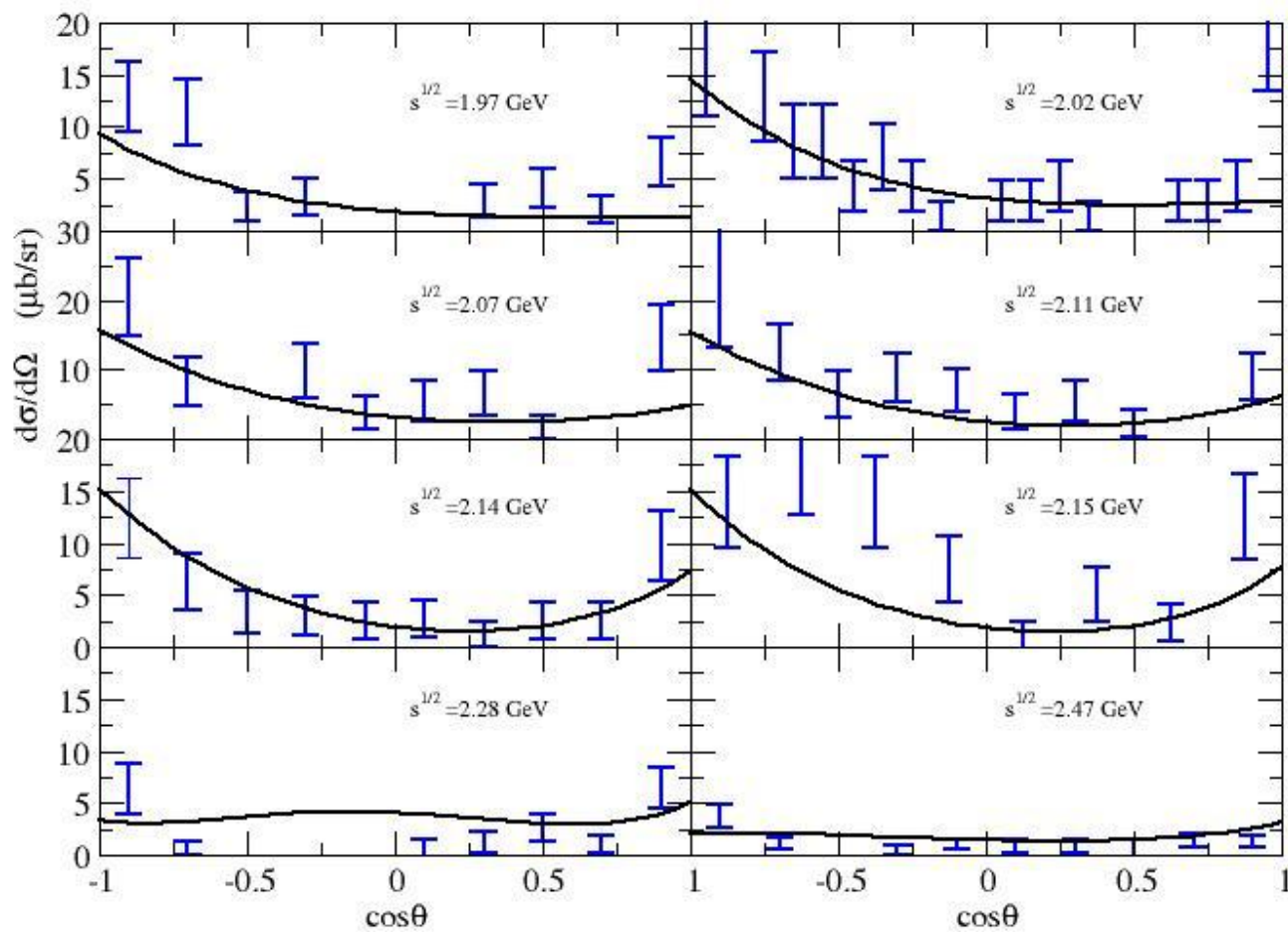
Fitting parameters 2

	WT+RES	WT+ NLO	WT+ NLO +RES
$a_{\bar{K}N} \text{ (} 10^{-3} \text{)}$	-1.87	4.13	4.03
$a_{\pi\Lambda} \text{ (} 10^{-3} \text{)}$	-202.56	26.03	26.89
$a_{\pi\Sigma} \text{ (} 10^{-3} \text{)}$	0.29	0.37	0.16
$a_{\eta\Lambda} \text{ (} 10^{-3} \text{)}$	1.42	4.50	5.10
$a_{\eta\Sigma} \text{ (} 10^{-3} \text{)}$	224.53	-16.00	-37.03
$a_{K\Xi} \text{ (} 10^{-3} \text{)}$	36.05	51.60	58.397
$f \text{ (MeV)}$	$1.20f_\pi$	$1.21f_\pi$	$1.21f_\pi$
$b_0 \text{ (GeV}^{-1} \text{)}$	-	-0.58	-0.52
$b_D \text{ (GeV}^{-1} \text{)}$	-	0.28	0.26
$b_F \text{ (GeV}^{-1} \text{)}$	-	0.39	0.43
$d_1 \text{ (GeV}^{-1} \text{)}$	-	0.36	0.41
$d_2 \text{ (GeV}^{-1} \text{)}$	-	0.49	0.45
$d_3 \text{ (GeV}^{-1} \text{)}$	-	0.95	0.85
$d_4 \text{ (GeV}^{-1} \text{)}$	-	-0.68	-0.59
$g_{\Xi Y_{5/2}K} \cdot g_{NY_{5/2}\bar{K}}$	-6.0	-	3.65
$g_{\Xi Y_{7/2}K} \cdot g_{NY_{7/2}\bar{K}}$	-6.59	-	0.12
$\Lambda_{5/2} \text{ (MeV)}$	506.50	-	578.94
$\Lambda_{7/2} \text{ (MeV)}$	484.05	-	862.25
$M_{Y_{5/2}} \text{ (MeV)}$	2300.0	-	2275.2
$M_{Y_{7/2}} \text{ (MeV)}$	2025.0	-	2040.0
$\Gamma_{5/2} \text{ (MeV)}$	60.0	-	130.71
$\Gamma_{7/2} \text{ (MeV)}$	200.0	-	200.00
$\chi^2_{d.o.f.}$	3.19	1.79	1.34

Variations
within 10-20%

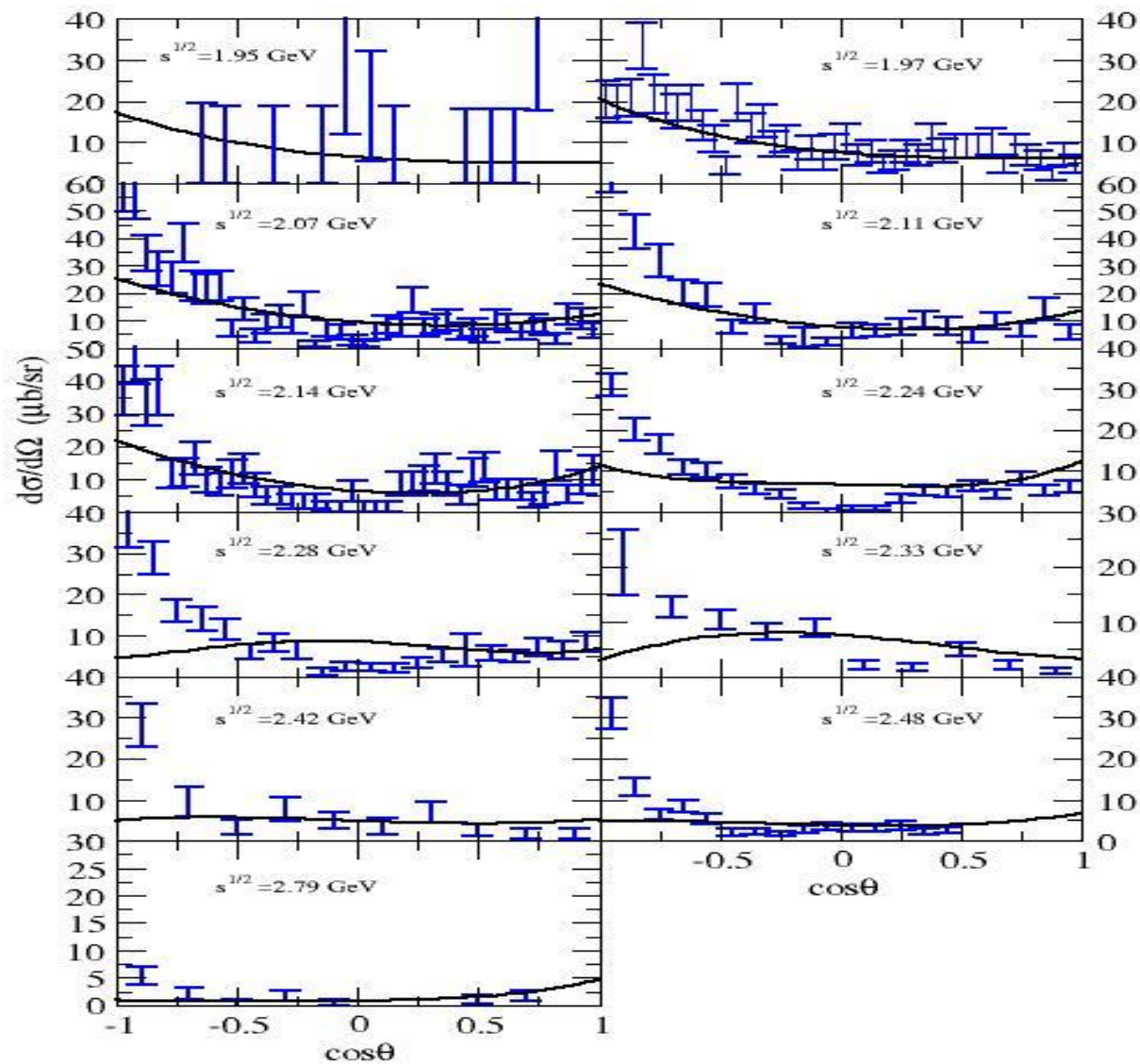
Results 2

$$K^- p \rightarrow K^0 \Xi^0$$



Results 2

$$K^- p \rightarrow K^+ \Xi^-$$



Production of Ξ in nuclei: (K^-, K^+) reaction on nuclear targets

- These reaction may inform us about the size of the Ξ optical potential in the nucleus
- They are employed to produce Ξ hypernuclei and double Λ hypernuclei

Production of Ξ in nuclei: (K^-, K^+) reaction on nuclear targets

$$K^-(p_{lab}) + A \Rightarrow K^+(p') + A'_{\Xi^-}$$

K^- is absorbed by the nucleon with momenta randomly chosen within the local Fermi sea

$$\sigma_{A_{\Xi}} = \int d^3r \rho_p(r) \sigma_{\Xi}(p_{lab}, k) = 2 \int d^3r \int \frac{d^3k}{(2\pi)^3} \Theta(k_F(r) - k) \sigma_{\Xi}(p_{lab}, k)$$

$$K^-(p_{lab}) + p(k) \Rightarrow K^+(p') + \Xi^-(k')$$

$$d\sigma_{\Xi}(p_{lab}, k) = \frac{(2\pi)^4}{4m_p p_{lab}} |T|^2 \frac{d^3p'}{(2\pi)^3 E_K} \frac{d^3k'}{(2\pi)^3 E_{\Xi}} \delta(p_{lab} + k - p' - k')$$

where $T \equiv T_{K^- p \rightarrow K^+ \Xi^-}^{tot}$

$$E_{\Xi} = \sqrt{M_{\Xi}^2 + k'^2} - V_{\Xi}(r), \quad V_{\Xi} = -V_0 \frac{\rho(r)}{\rho_0}, \quad \text{with} \quad V_0 \approx -15 - 20 \text{ MeV}$$

Production of Ξ in nuclei: (K^-, K^+) reaction on nuclear targets

Exp. Data of **T.Iijima et al. Nucl.Phys. A546 (1992) 588**

$$K^- A \rightarrow K^+ \Xi^- A' \quad p_{K^-} = 1.65 \text{ GeV}$$

$$\text{Forward reaction: } 1.7^\circ < \Theta_{K^+} \Big|_{lab} < 13.6^\circ$$

ISI - eikonal approximation

$$e^{-\int_{-\infty}^z \sigma_{K^-N}(p_{lab}) \rho(\sqrt{b^2 + z'^2}) dz'} \quad \sigma_{K^-N} = \frac{1}{2} (\sigma_{K^-p}^{tot} + \sigma_{K^-n}^{tot})$$

FSI - eikonal approximation

$$e^{-\int_z^\infty \sigma_{K^+N}(p') \rho(r') dl} \quad \text{where} \quad \vec{r}' = \vec{r} + l \frac{\vec{p}'}{p'} \quad \sigma_{K^+N} = \frac{1}{2} (\sigma_{K^+p}^{tot} + \sigma_{K^+n}^{tot})$$

Production of Ξ in nuclei: (K^-, K^+) reaction on nuclear targets

Exp. Data of **T.Iijima et al. Nucl.Phys. A546 (1992) 588**

$$K^- A \rightarrow K^+ \Xi^- A' \quad p_{K^-} = 1.65 \text{ GeV}$$

Forward reaction: $1.7^\circ < \Theta_{K^+} \Big|_{lab} < 13.6^\circ$

$$T_{K^- p \rightarrow K^+ \Xi^-}^{tot} \Rightarrow \left(\frac{d\sigma}{d\Omega} \right)_{lab}^{forward} \approx 35 mb$$

Practically constant

$$|\vec{p}| \leq k_F(\rho_0)$$

ISI: $\sigma_{K^- N} \approx 29 mb$

Practically constant

FSI: $\sigma_{K^+ N} \approx 18.4 mb$

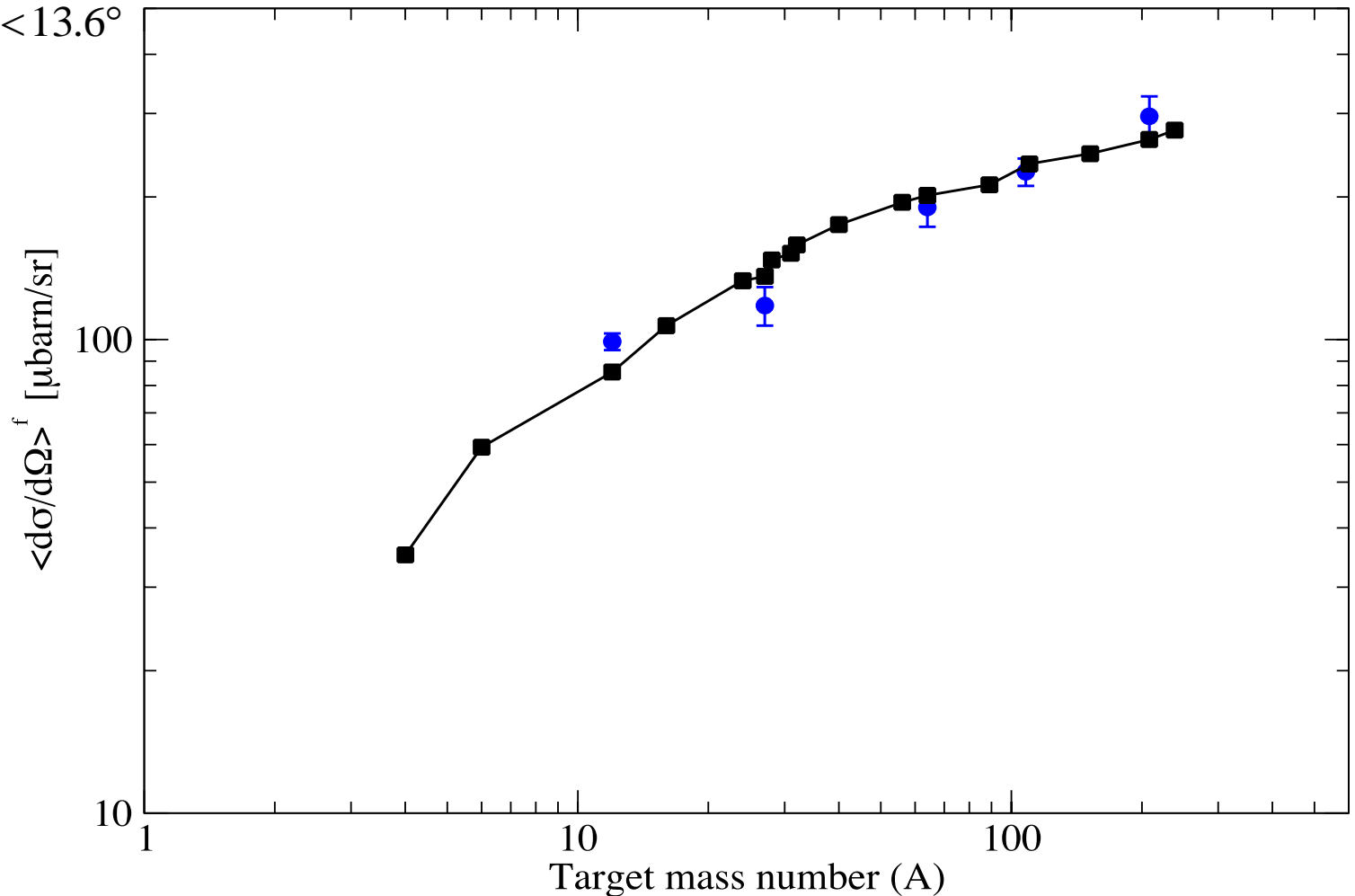
Exp. Data of T.Iijima et al. Nucl.Phys. A546 (1992) 588

$$K^- A \rightarrow K^+ \Xi^- A'$$

$$p_{K^-} = 1.65 \text{ GeV}$$

$$0.95 < p_{K^+} < 1.30 \text{ GeV/c}$$

$$1.7^\circ < \Theta_{K^+}|_{lab} < 13.6^\circ$$



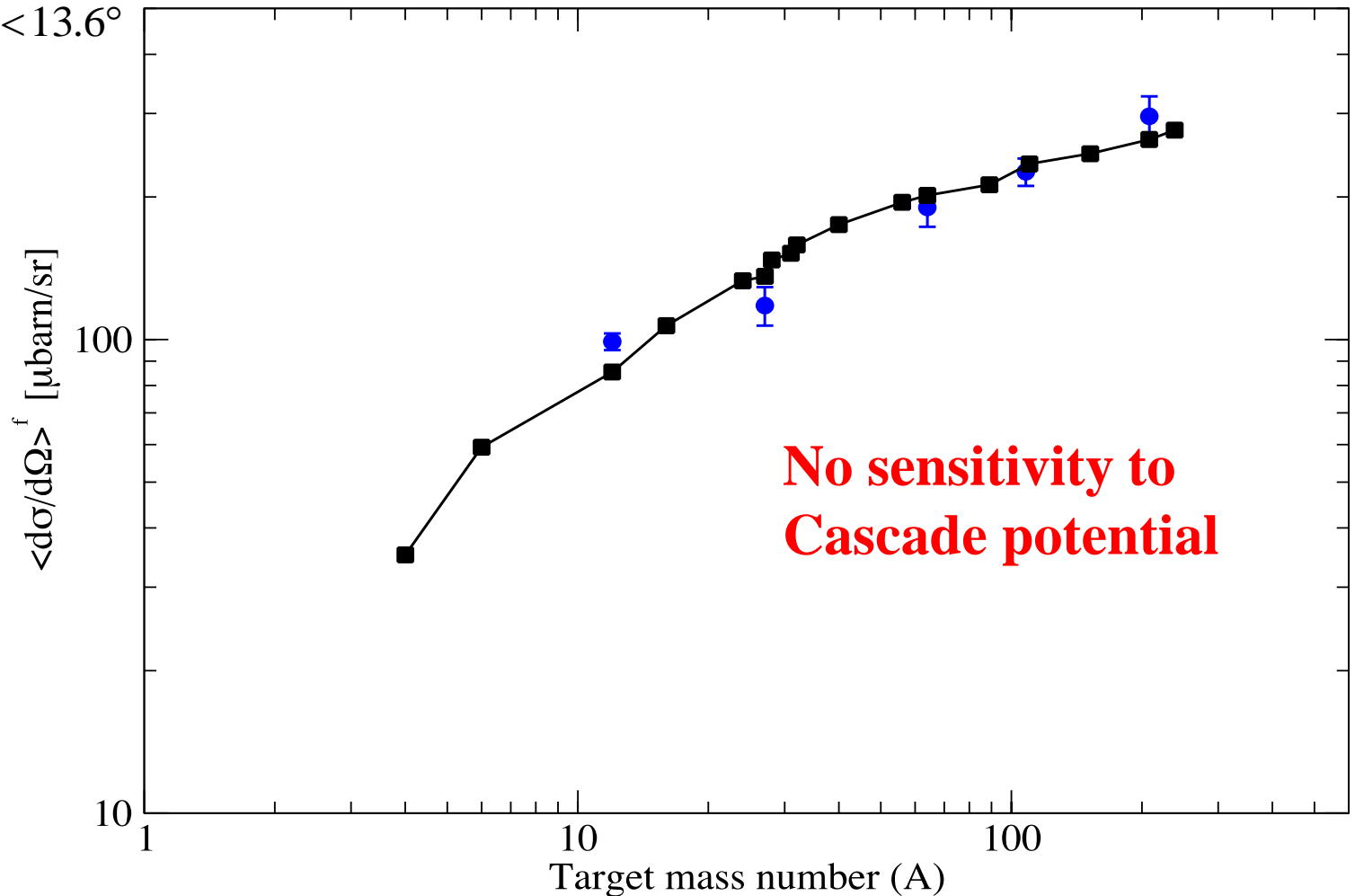
Exp. Data of T.Iijima et al. Nucl.Phys. A546 (1992) 588



$$p_{K^-} = 1.65 \text{ GeV}$$

$$0.95 < p_{K^+} < 1.30 \text{ GeV/c}$$

$$1.7^\circ < \Theta_{K^+}|_{lab} < 13.6^\circ$$



Ξ -hypernuclei production

We add the condition: $E_{\text{ext}} < 0$

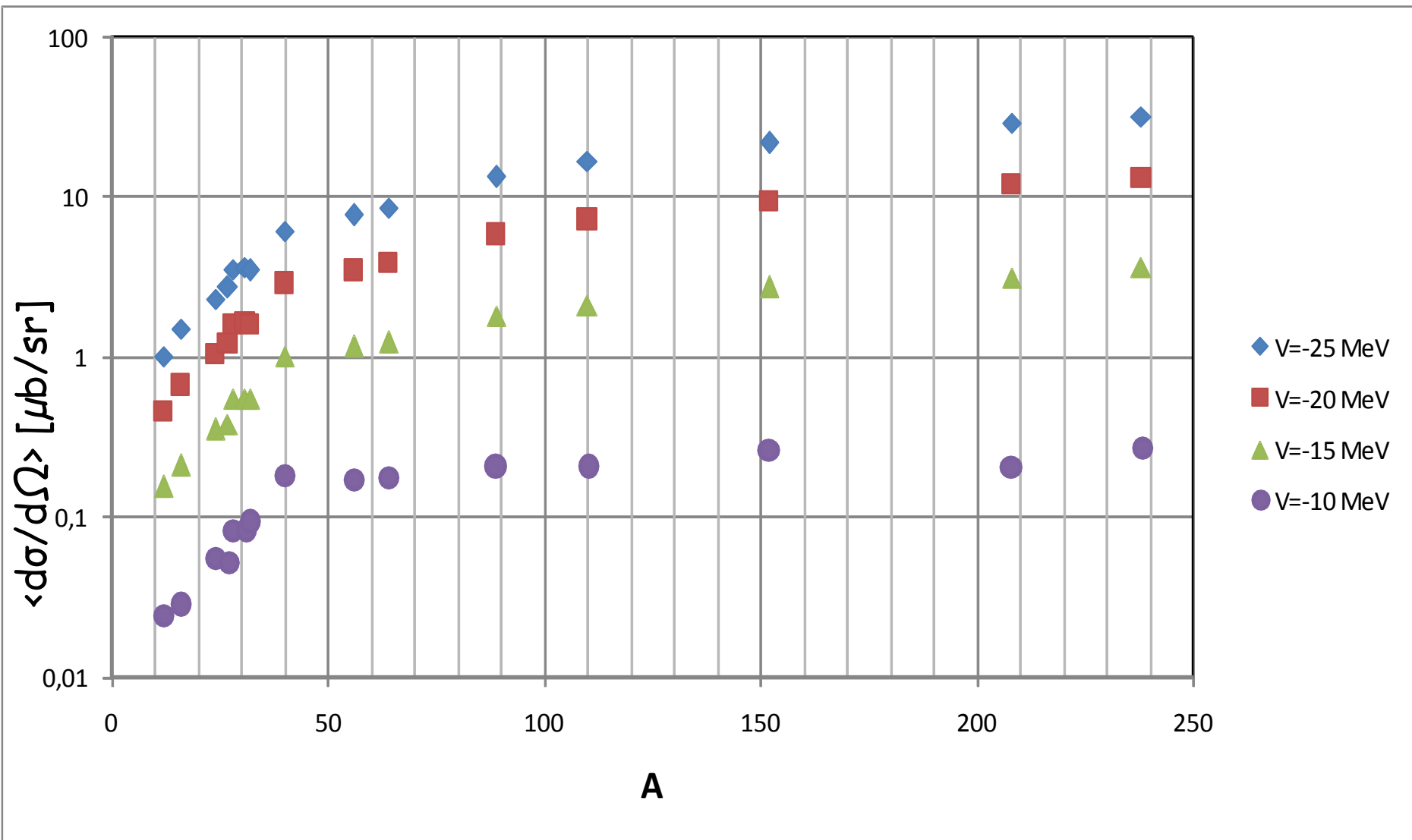
$$E_{\text{ext}} = E_x - M_{gs}^{A'} - M_{\Xi^-} = \left[E_{K^-} + M_{gs}^A - E_{K^+} \right] - M_{gs}^{A'} - M_{\Xi^-}$$

Ξ -hypernuclei production

$$p_{K^-} = 1.65 \text{ GeV}$$

$$\mathbf{E}_{\text{ext}} < 0$$

$$1.7^\circ < \Theta_{K^+}|_{\text{lab}} < 13.6^\circ$$

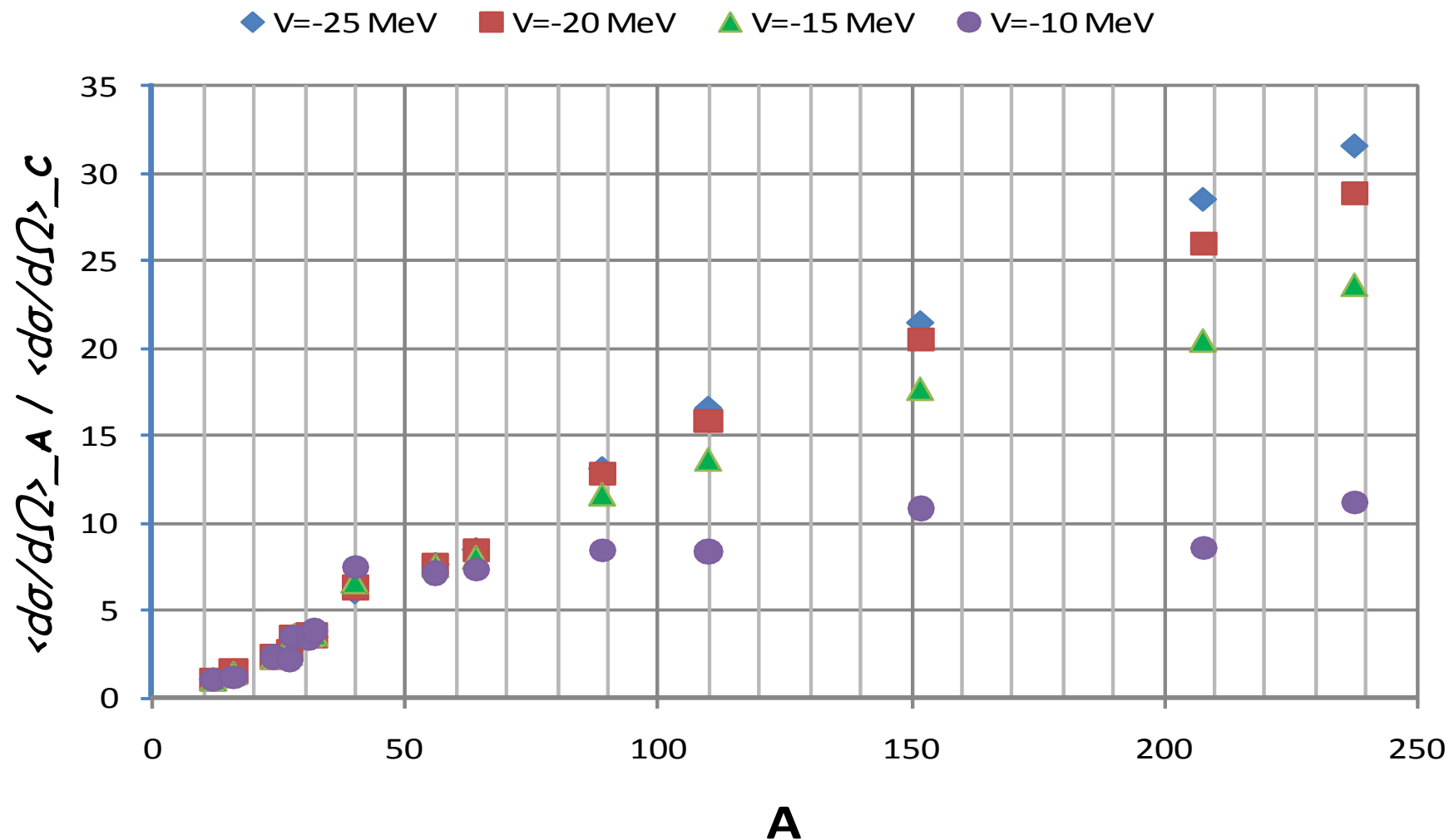


Ξ -hypernuclei production

$$p_{K^-} = 1.65 \text{ GeV}$$

$$E_{\text{ext}} < 0$$

$$1.7^\circ < \Theta_{K^+}|_{\text{lab}} < 13.6^\circ$$



Conclusions

Chiral Perturbation Theory with unitarization in coupled channels is a very powerful technique to describe low energy hadron dynamics

Next - to - leading order calculations are now possible

*NLO terms in the Lagrangian do improve
agreement with data*

*$K^-p \rightarrow K\Xi$ channels are very interesting and important
for fitting NLO parameters*

Our results can be useful to study Ξ -hypernuclei production

Work in progress...

BACKUP SLIDES

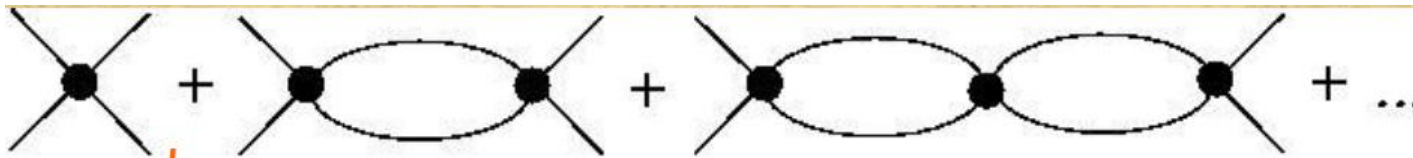
$\Lambda(1405)$ as a dynamically generated resonance

Jones, Dalitz and Horgan, Nucl. Phys. B129 (1977) 45 –

$\Lambda(1405)$ is dynamical generated

Boost in unitary extensions of chiral perturbation theory ($U\chi PT$)

1995-2003: Kaiser, Oset, Ramos, Oller, Meissner, Jido,
Hosaka, Garcia-Recio, Vicente Vacas



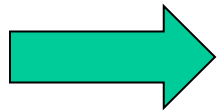
$\Lambda(1405)$ as a dynamically generated resonance

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$\Lambda(1405)$ is dynamical generated

Boost in unitary extensions of chiral perturbation theory ($U\chi PT$)

1995-2003: Kaiser, Oset, Ramos, Oller, Meissner, Jido,
Hosaka, Garcia-Recio, Vicente Vacas



Surprisingly there are **two poles** in the neighborhood of the $\Lambda(1405)$ both contributing to the final experimental invariant mass distribution

$\pi\Sigma$

Mass ~ 1390 MeV
Width ~ 130 MeV

$\bar{K}N$

Mass ~ 1425 MeV
Width ~ 30 MeV

$\Lambda(1405)$ as a dynamically generated resonance

The observed shapes are in good agreement with corresponding chiral unitarity model calculations:

$$K^- p \rightarrow \pi^0 \pi^0 \Sigma^0$$

⇒ Magas, Oset, Ramos,
Phys. Rev. Lett. 95 (05) 052301

$$\pi^- p \rightarrow K^0 \pi \Sigma$$

⇒ Thomas et al.,
Nucl. Phys. B56 (1973) 15

This combined study gives the first **experimental evidence** of the two-pole nature of the $\Lambda(1405)$

Crystall Ball Collaboration data from
versus

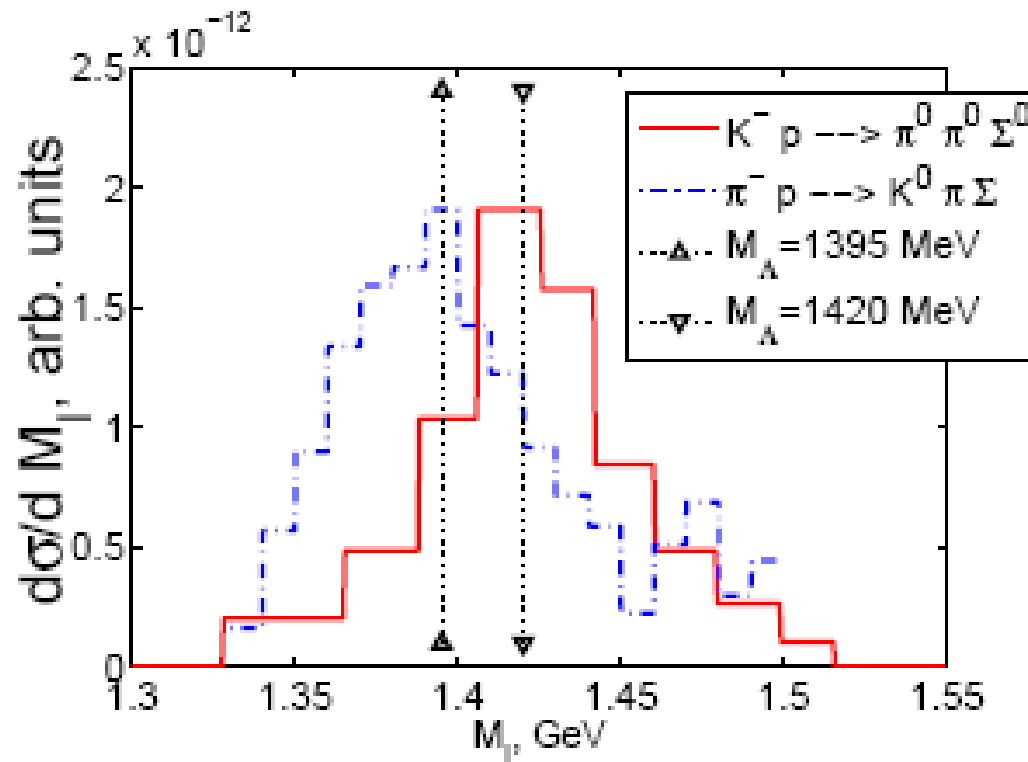
$$K^- p \rightarrow \pi^0 \pi^0 \Sigma^0$$

(Width ~ 38 MeV)

Thomas et al., NP B 56 (1973) 15

$$\pi^- p \rightarrow K^0 \pi \Sigma$$

(Width ~ 60 MeV)



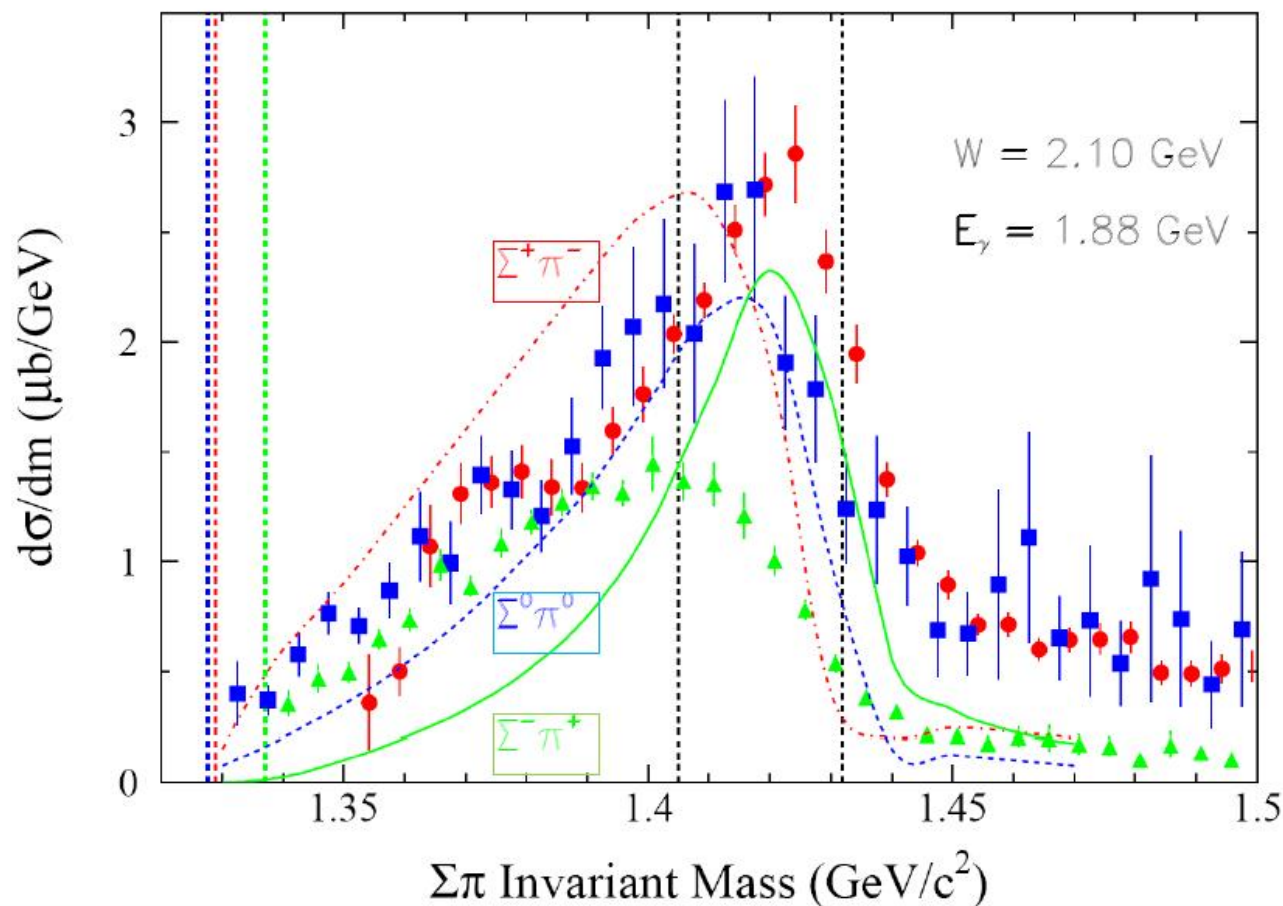
Magas, Oset, Ramos,
PRL 95 (2005) 052301

FIG. 5: Two experimental shapes of $\Lambda(1405)$ resonance. See text for more details.

Fine-tuning of the model

Large $I=1$ effects have been detected in the photoproduction experiment at CLAS, Moriya *et al.*, *Phys.Rev.C87,035206 (2013)*

$$\gamma p \rightarrow K^+ \pi \Sigma$$



Line Curves, Nacher et al.
Better reproduction for $\pi^0 \Sigma^0$ But not for the charged modes with $I=1$