

On Some Contributions to Quantum Structures by Fuzzy Sets

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Abstract: It is well known that the fuzzy sets theory can be successfully used in quantum models ([5, 26]). In this paper we give first a review of recent development in the probability theory on tribes and their generalizations – multivalued (MV)-algebras. Secondly we show some applications of the described method to develop probability theory on IF-events.

Keywords: probability; fuzzy sets; MV-algebra; IF events;

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