

## Overlapping Controllers for Uncertain Delay Continuous-Time Systems

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*Abstract:* This paper extends the Inclusion Principle to a class of linear continuous-time uncertain systems with state as well as control delays. The derived expansion-contraction relations include norm bounded arbitrarily time-varying real uncertainties and a point delay. They are easily applicable also to polytopic uncertainties. These structural conditions are further specialized on closed-loop systems with arbitrarily time-varying parameters, a point delay, and guaranteed quadratic costs. A linear matrix inequality (LMI) delay independent procedure is used for control design in the expanded space. The results are specialized on the overlapping decentralized control design. A numerical illustrative example is supplied.

*Keywords:* decentralized control; large-scale complex systems; overlapping decompositions; continuous-time systems; uncertainty; delay; LMI;

*AMS Subject Classification:* 93A14; 93A15; 93B51; 93B52; 93C41;

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