

The Stability of Parameter Estimation of Fuzzy Variables

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Abstract: Recently, the parameter estimations for normal fuzzy variables in the Nahmias' sense was studied by Cai [4]. These estimates were also studied for general T -related, but not necessarily normal fuzzy variables by Hong [10]. In this paper, we report on some properties of estimators that would appear to be desirable, including unbiasedness. We also consider asymptotic or "large-sample" properties of a particular type of estimator.

Keywords: duzy variables; parameter estimation; consistency; MSE; stability of estimation;

AMS Subject Classification: 28E10; 62L12;

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