

## A Note About Operations Like $T_W$ (the Weakest $t$ -Norm) Based Addition on Fuzzy Intervals

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*Abstract:* We investigate a relation about subadditivity of functions. Based on subadditivity of functions, we consider some conditions for continuous  $t$ -norms to act as the weakest  $t$ -norm  $T_W$ -based addition. This work extends some results of Marková-Stupňanová [15], Mesiar [18].

*Keywords:* fuzzy arithmetics; fuzzy intervals; triangular norms;

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