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Published by

WIT Press

Ashurst Lodge, Ashurst, Southampton, SO40 7AA, UK
Tel: 44 (0) 238 029 3223; Fax: 44 (0) 238 029 2853
E-Mail: witpress@witpress.com
<http://www.witpress.com>

For USA, Canada and Mexico

Computational Mechanics Inc

25 Bridge Street, Billerica, MA 01821, USA
Tel: 978 667 5841; Fax: 978 667 7582
E-Mail: infousa@witpress.com
<http://www.witpress.com>

British Library Cataloguing-in-Publication Data

A Catalogue record for this book is available
from the British Library

ISBN: 978-1-84564-189-4
ISSN: 1746-4471 (print)
ISSN: 1743-3533 (on-line)

The texts of the papers in this volume were set individually by the authors or under their supervision. Only minor corrections to the text may have been carried out by the publisher.

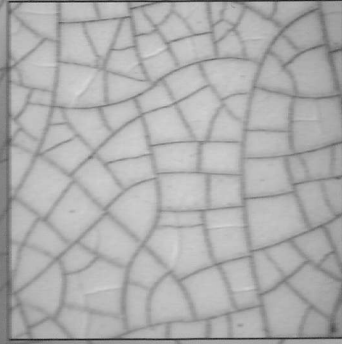
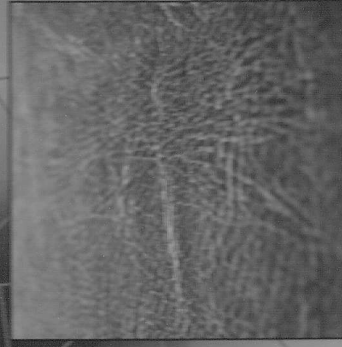
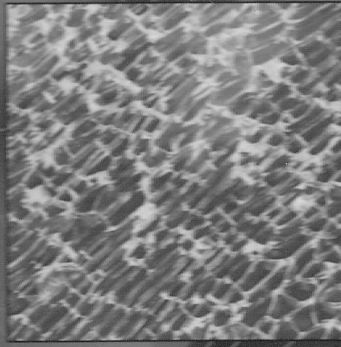
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Materials Characterisation Computational Methods and Experiments IV



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5.1 Materials and method

In each phase, 10 gr Zeolite was mixed with 40 mL HMNDA compound (N,N,N',N',N' -hexamethyl-1/9-nonanediammonium bromide, $2/72.10^{-4}$ molar) in 65 percent ethanol liquid. After 48 hours detention time in mixer, the Zeolite's colour was changed from white to grey. The remediate material must be removed via washing by water which is distilled twice and ethanol liquid (65%) for several times. Then, this Zeolite was made dry (24 hours in open air).

5.2 Results

Since groundwater resources contain arsenic, especially in the West and Northwest of Iran, the removal of arsenic ions was investigated. The results are shown in figure 8 and show that the optimized pH equals 1.5-2 and required Zeolite for removal process equals 2 gr.

6 Conclusion

Natural Zeolite can be used as a suitable material for groundwater treatment. The investigated natural Zeolite is characterized as Natrolite. It is concluded that this Zeolite has a considerable ability to remove hardness, 3 valence cations and also it is particularly appropriate to remove anions like arsenic that depends on pH and HMNDA.

Acknowledgement

This study was supported by the Sistan and Belouchestan Water and Wastewater Company (SBWWC) and National Water and Wastewater Company Iran (NWWC).

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Resonant ultrasound spectroscopy for investigation of thin surface coatings

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Abstract

In this paper, we analyze the possibility of determination of all in-plane independent elastic coefficients of an anisotropic surface coating on a known substrate by means of resonant ultrasound spectroscopy (RUS). A novel approach based on perturbation theory is presented, which enables direct determination of the elastic coefficients of the coating from the shift of resonant frequencies induced by the deposition of the layer. The reliability of the proposed concept is investigated by numerical simulations as well as verified by experiments.

Keywords: *ultrasound spectroscopy, thin coatings, perturbation theory, non-destructive evaluation, in-plane anisotropy.*

1 Introduction

Reliable determination of elastic coefficients of thin surface layers and coatings is one of the most challenging topics of today's experimental mechanics. Conventional micro/nanoindentation techniques are usually neither able to distinguish clearly which part of the elastic response is inherent to the coating and which to the underlying substrate, nor suitable for determination of all independent elastic coefficients of anisotropic coatings. A promising alternative to these highly local techniques are the ultrasonic methods, which may be either the methods based on surface elastic waves (SAW), or the resonant ultrasound spectroscopy (RUS) where the sought elastic coefficients are determined from measurements of resonant spectra of free elastic vibrations of a specimen of the examined material. The latter will be discussed in this paper.

Nowadays, the RUS is one of the most widely used methods for determination of elastic coefficients of bulk anisotropic materials. This method has found its very first applications in geophysics as early as in late 1960s, where the clas-



tic coefficients of rocks and minerals were determined from resonant spectra of spherical samples (so-called *resonant sphere technique*, RST [1]) or small cubes [2] of the examined material. Later on, the method was significantly improved by Ohno and his coworkers, enabling determination of anisotropic elastic coefficients up to orthorhombic [3] and trigonal [4] symmetry class from measurements on a rectangular parallelepiped (so-called *rectangular parallelepiped resonance*, RPR). In early 1990s, Migliori et al. [5] introduced this method to solid state physics community, and applied it immediately to in-situ monitoring of elasticity changes of high temperature superconductors when undergoing transitions to the superconducting state [6]. In these pioneering works, also the more general abbreviation RUS started to be used. The measurements were further improved by scanning the surface of the resonating specimen by a laser vibrometer, thus not only the resonant frequencies but also the shapes of vibration modes became available. In 2002, Ogi et al. [7] used this improvement for reliable identification of individual modes in the obtained spectrum, which was the approach further developed by the authors in the past few years [8–12].

As far as the investigation of thin surface layers and coatings is concerned, the first attempt to modify the RUS technique for such problems can be found in Visscher's paper [13], where, among many other general shapes of the specimen, also a 'sandwich' (a specimen consisting of two parallel layers) is discussed. By decreasing the thickness of one of the layers, such 'sandwich' obviously limits to a substrate-coating system; this idea was utilized by So et al. [14], who used the concept outlined in [13] for modeling of free vibrations of a SrTiO₃ substrate coated by a thin magnetoresistant film.

Extensive experimental literature on RUS investigation of thin surface layers was published by Ogi and his coworkers. It covers a huge variety of substrate-coating systems ranging from superlattice thin films (Co/Pt multilayer in [15]) to diamond coatings deposited by CVD [16, 17]. The main improvement brought by the Ogi's group to the experimental embodiment of RUS lies in a novel experimental scheme, so-called tripod scheme (e.g. [7]). In this scheme, the investigated specimen is freely laid in a tripod of thin, rod-like piezoelectric transducers (one of them is used for generation of vibrations, the others for detection of the specimen's response). Compared to the classical scheme used in earlier works (e.g. [5]), where the specimen is clamped between two transducers, the tripod scheme ensures that the vibrations of the specimen are very close to free vibrations (the clamping force is eliminated, which is crucial particularly for thin plates or shells). For mathematical description of the vibrating substrate-coating systems, the Ogi's group uses full 3D-3D 'sandwich' models based on the concept of Visscher [13], often utilizing an interpolation method developed by Heyliger [18].

In this paper, novel theoretical and the experimental approaches will be discussed. Unlike to the 'sandwich' concept from [13], our approach reflects the multiscale character of the problem, treating the surface layer as a 2D object deposited on a 3D substrate. In the experimental part, a fully non-contact setup [11] is presented, where the vibrations of the specimen are both generated and detected by lasers. As it will be shown, these novel approaches lead to reliable, reproducible

and straightforward determination of elastic coefficients of the examined surface layer.

2 Theory and preliminary numerical tests

The main idea of RUS measurements is following: First, the resonant spectrum of vibrations of the examined specimen is measured and individual resonant frequencies are localized. Then, the elastic coefficients are determined *inversely*, which means that they are tuned such that the resonant frequencies computed for them fit the experimentally obtained spectrum in some optimal way. For such procedure, one must be able to solve the so-called *direct problem*, i.e. to evaluate the resonant frequencies of the specimen for known elastic coefficients. For homogeneous, bulk specimens of simple geometry, this can be easily achieved by finding stationary points of the Lagrangian energy of the vibrating specimen (a simple variational problem, which can be easily solved by Ritz method, see e.g. [5, 7, 10, 12]). In the following section, the direct problem will be posed and solved for a substrate-coating system.

2.1 Perturbation model of a vibrating substrate-coating system

Consider now a vibrating substrate (a rectangular parallelepiped with edges aligned to cartesian coordinates x_1 , x_2 and x_3) on which a thin coating is deposited (on a face normal to the x_3 axis). The kinetic and potential energy of the substrate are

$$E_k = \frac{1}{2} \int_{V_s} \rho_s \dot{u}_i \dot{u}_i dV_s \quad \text{and} \quad E_p = \frac{1}{2} \int_{V_s} C_{ijkl}^{(s)} \frac{\partial u_i}{\partial x_j} \frac{\partial u_k}{\partial x_l} dV_s, \quad (1)$$

where, \mathbf{u} is the displacement field, ρ_s is the density, $C_{ijkl}^{(s)}$ are the elastic coefficients and $V_s = \langle -d_1/2; d_1/2 \rangle \times \langle -d_2/2; d_2/2 \rangle \times \langle -d_3/2; d_3/2 \rangle$ is the volume of the substrate. By taking polynomial approximation of the displacement field

$$u_i = \sum_{k=1}^N \alpha_k^{(i)} \psi_k(x_1, x_2, x_3) \cos(\omega t) \quad (2)$$

(where ω is the angular frequency of harmonic vibrations and the basis ψ_k can be advantageously chosen as orthonormal Legendre polynomials), it can be easily shown (e.g. [5]) that the problem of finding stationary points of the Lagrangian of the substrate $L = E_k - E_p$ can be rewritten as a generalized eigenvalue problem of the following form:

$$\mathbb{K}\bar{\alpha} - \omega^2 \mathbb{M}\bar{\alpha} = \bar{0}, \quad (3)$$

where $\bar{\alpha}$ is a vector of coefficients from approximation (2) and the matrices \mathbb{K} and \mathbb{M} are given by the geometry, density and elastic coefficients of the substrate [5, 7, 10, 12].

tensor $(\varepsilon_{11}, \varepsilon_{22}$ and $\varepsilon_{12})$, i.e. $[\sigma_{11}, \sigma_{22}, \sigma_{12}]^T = \mathbb{Q}[\varepsilon_{11}, \varepsilon_{22}, 2\varepsilon_{12}]^T$. It can be easily shown that

$$\mathbb{Q} = \begin{pmatrix} (C^{-1})_{1111}^{(c)} & (C^{-1})_{1122}^{(c)} & (C^{-1})_{1112}^{(c)} \\ (C^{-1})_{1111}^{(c)} & (C^{-1})_{2222}^{(c)} & (C^{-1})_{2212}^{(c)} \\ \text{symm.} & & (C^{-1})_{1212}^{(c)} \end{pmatrix}^{-1}, \quad (8)$$

where $(C^{-1})_{ijkl}^{(c)}$ is a compliance tensor. Further in this text, we will use this matrix \mathbb{Q} for characterization of in-plane elastic coefficients of the coatings, i.e. of those elastic coefficients of the coatings theoretically obtainable from RUS measurements on the substrate-coating system.

2.2 Numerical comparison to a full 3D-3D model

The above proposed perturbation model can be expected to work properly for $h \ll d_3$. Indeed, both the perturbations of the energetic quantities, δE_k and δE_p , are linearly proportional to the thickness of the coating, so limiting $h \rightarrow 0$ increases the validity of our assumptions. A natural question arises, how thin the coating must be to justify the use of the perturbation model, i.e. to ensure that this model provides the frequency shifts with some satisfying accuracy. To investigate this, and in order to verify the correctness of our model, we made the following preliminary numerical tests prior to applying the perturbation model to real experimental data:

1. We considered a homogeneous specimen (a $4\text{mm} \times 5\text{mm} \times 1\text{mm}$ single crystal of silicon cut along the principal directions) with the smallest dimension slightly increasing, and analyzed whether the changes of the resonant frequencies due to the thickening (evaluated by solving the eigenvalue problem (3) for different d_3) can be captured by the perturbation model. In other words, we analyzed a substrate-coating system, where the coating had exactly the same elastic properties as the substrate.
2. We assumed a full 3D-3D 'sandwich' model (similar to [13] but using an orthogonal basis) as a reference and compared the frequency shifts predicted by this model to those evaluated by relation (7). The analyzed system in this case was a CVD deposited diamond coating on the same substrate as in the first example.

For both these systems, shifts of the first thirty resonant frequencies of the substrate were evaluated. The results are shown in Fig. 1. In the upper row, the frequency shifts are shown for two chosen modes (the 1st and the 12th mode in the spectrum; circles denote the full 3D-3D models, solid lines are the shifts determined by relation (7)), in the lower row, the difference between the shifts predicted by the both models for all analyzed thirty modes is plotted versus the thickness and the mode number. The results are shown for the thickness of the coating ranging from 10nm to $100\ \mu\text{m}$.

Obviously, there is a significant difference between the two analyzed systems. Except of three or four modes, the perturbation model sufficiently approximates

Let us now incorporate the presence of the coating in this model. The kinetic and potential energy of the coating (understood here as small perturbations δE_k and δE_p) are considered now as fully given by the displacement field \mathbf{u} at the surface of the substrate where the coating is deposited. For h standing for the thickness of the coating, a possible assumption is to take this displacement field (denoted here as $\mathbf{v}(x_1, x_2, t)$) as an extrapolation of displacement field \mathbf{u} in the midplane of the coating (e.g. in distance $h/2$ above the surface of the substrate) (in this simplification, we neglect the fact that the derivatives of \mathbf{u} can be discontinuous over the substrate-coating interface) which reads

$$v_i(x_1, x_2, t) = u_i(x_1, x_2, x_3 = d_3/2, t) + \frac{h}{2} \frac{\partial u_i}{\partial x_3}(x_1, x_2, x_3 = d_3/2, t) \quad (4)$$

for $i = 1, 2, 3$. This leads to the following simplified expressions

$$\delta E_k = \frac{h}{2} \int_{S_c} \rho_c \dot{v}_i \dot{v}_i dS_c \quad \text{and} \quad \delta E_p = \frac{h}{2} \int_{S_c} C_{ijkl}^{(c)} \frac{\partial v_k}{\partial x_j} \frac{\partial v_l}{\partial x_i} dS_c, \quad (5)$$

for the kinetic and elastic energy of the coating respectively, where the subscripts c and superscripts (c) denote the quantities related to the coating. Using the approximation (2) again, a *perturbed eigenvalue problem* can be arrived, relating the perturbation of matrices \mathbb{K} and \mathbb{M} to the small changes in the angular frequencies $\delta\omega^2$ as

$$(\mathbb{K} + \delta\mathbb{K})(\vec{\alpha} + \delta\vec{\alpha}) - (\omega^2 + \delta\omega^2)(\mathbb{M} + \delta\mathbb{M})(\vec{\alpha} + \delta\vec{\alpha}) = \vec{0}. \quad (6)$$

In this first, linear approximation, is $\vec{\alpha} \perp \mathbb{M}\delta\vec{\alpha}$ and thus, after some additional algebra, the perturbation of the resonant frequency of the i -th mode ($\delta\omega_i^2$) can be expressed as

$$\delta\omega_i^2 = \frac{\vec{\alpha}_i^T (\delta\mathbb{K} - \omega_i^2 \delta\mathbb{M}) \vec{\alpha}_i}{\vec{\alpha}_i^T \mathbb{M} \vec{\alpha}_i}. \quad (7)$$

This formula directly relates the shifts of the resonant frequencies to the elastic coefficients, the density and the thickness of the coating (embodied here by the perturbations $\delta\mathbb{K}$ and $\delta\mathbb{M}$). In other words, it enables $C_{ijkl}^{(c)}$ to be determined directly from the shifts $\delta\omega_i^2$, without solving the full eigenvalue problem (6) within every step of the inverse procedure. This makes the use of the perturbation model not only enormously less computation-time-consuming than the classical approaches, but more lucid for further theoretical analysis (e.g. estimation of the experimental errors).

It is more than obvious that the shifts $\delta\omega_i^2$ cannot contain sufficient information on all the elastic coefficients $C_{ijkl}^{(c)}$. In the potential energy δE_p , all the products $C_{ijkl}^{(c)} \varepsilon_{ij} \varepsilon_{kl} = \sigma_{kl}^{(c)} \varepsilon_{kl}$ give zero whenever k or l equals to 3 (plane stress conditions in the coating), which decreases the number of the involved elastic coefficients from 21 down to 6. These coefficients can be arranged into a symmetric 3×3 matrix \mathbb{Q} , which represents a linear relation between the non-zero components of the stress tensor (σ_{11} , σ_{22} and σ_{12} only) to the in-plane components of the strain

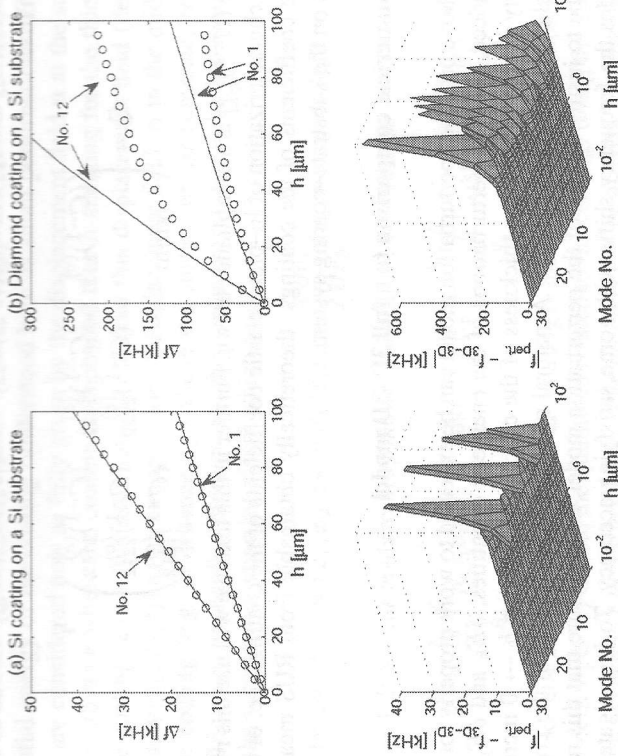


Figure 1: Comparison of the perturbation method to a full 3D-3D model. Upper row: Frequency shifts for the 1st and the 12th mode depending on the thickness of the coating h . (Circles denote the full 3D-3D models, solid lines the perturbation method). Lower row: Differences between the two discussed models for the first 30 modes.

the frequency shifts for the silicon substrate with changing thickness up to $h = 100 \mu\text{m}$, whereas the silicon-diamond system is reasonably described by the perturbation model for $h \leq 10 \mu\text{m}$ only. The reason may be found in the disproportion between the elastic properties of silicon and of the deposited diamond. The cubic crystal of silicon has $c_{11} = 166 \text{ GPa}$, $c_{12} = 64 \text{ GPa}$ and $c_{44} = 80 \text{ GPa}$; for the isotropic diamond coating (polycrystal aggregate), the bulk coefficients $c_{11} = 1143 \text{ GPa}$ and $c_{44} = 530 \text{ GPa}$ were taken from [7]. Thus the diamond is nearly seven times 'tougher' in tension than the silicon substrate itself. That is the reason why the potential energy of a $100 \mu\text{m}$ thick diamond coating cannot be ever taken as a small perturbation of the potential energy of the 1 mm thick silicon substrate, and the perturbation approach fails. We can conclude that any estimation of limiting thickness h for which the perturbation approach reliably works is impossible without taking the ratio between elastic moduli of the substrate and the coating into account.

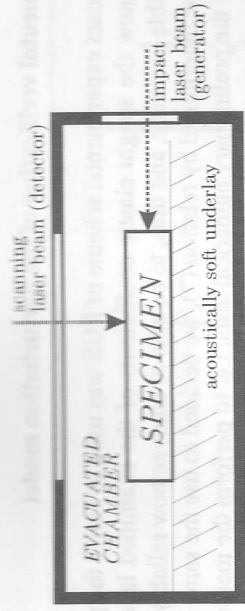


Figure 2: Outline of the non-contact experimental scheme of RUS.

3 Experiment

In this final section, the above outlined approach will be verified experimentally. The experiment (the setup and instrumentation) will be briefly described, and the results for two testing materials will be presented and discussed.

3.1 Experimental setup

For the RUS measurements described in this paper, a fully non-contact scheme [11] was used. In this scheme, the specimen is excited by an impact of a focused laser pulse (so-called thermoacoustic source) and the vibrations are detected by laser-Doppler interferometer scanning the surface of the excited specimen. The specimen itself is laid of an underlay which must be extremely acoustically soft (i.e. its acoustic impedance must be incomparably smaller than the impedance of the specimen) to ensure a good approximation of the free-surface boundary conditions. To minimize the damping of the specimen, the whole measurement is performed in an evacuated chamber with two silica-glass windows, one for each of the used laser beams (see Fig. 2 for an outline). The used instrumentation was following: The elastic vibrations in the specimen were excited by sequences of pulses of a focused infrared laser beam (pulse duration 8 ns , energy 25 mJ , Quantel ULTRA Nd:YAG Laser system, equipped by fiber optic – FOLA options). The displacement response was detected in a mesh of points on the sample surface by Polytec Micro System Analyzer MSA-500 (using the OFV-5000 controller and the sensor head OFV-551).

This scheme was inspired by measurements by Zadler [19], who used lasers to excite specimens hanging on thin silica wires. However, the use of the acoustically soft underlay proposed by the authors seems to provide adequately good approximation of the free-surface conditions, but with much easier specimen mounting and replacement. This experimental concept was already successfully applied to determine elastic coefficients of various bulk materials [11, 12], and was shown to be especially suitable for quantitative measurements of ultrasound attenuation [20].

3.2 Experimental verification of the perturbation model

The non-contact experimental scheme of RUS was used to verify the perturbation model. To know the sought elastic coefficients of the examined layers with the highest possible accuracy, and thus, to be able to analyze how reliably these coefficients can be determined by relation (7), we decided to use the same approach as in the first of the preliminary numerical tests, i.e. to perform the measurements on homogeneous specimens where the presence (or absence) of the surface coating is represented by a change in thickness.

Two different materials were used for such experiments. The first was a single crystal of silicon (a 2.1 mm × 3.6 mm × 3.1 mm rectangular parallelepiped cut along the principal crystallographic axes) and the second a reaction-bonded silicon carbide Si-SiC (1.8 mm × 2.5 mm × 2.8 mm rectangular parallelepiped). These specimens were taken as substrates *with* surface layers; the resonant spectra of these specimens were measured (covering always about the first thirty modes) and individual modes of vibration within the spectra were identified. After that, the considered surface layers were removed by polishing: 32 μm thick layer was polished out from the single crystal of silicon, 8 μm thick layer from the specimen of the reaction-bonded silicon carbide. This approach simulated the issue of determination of elastic properties of a 32 μm thick cubic surface coating and a 8 μm thick isotropic surface coating. The resonant spectra of the specimens *without* the 'coatings' were measured and the frequency shifts $\delta\omega^2$ for particular modes were identified (in this point, the identification of the modes from scanning laser-Doppler interferometry is obviously crucial, as the original order of the resonances can be shuffled when the layer is deposited/removed).

To verify the reproducibility of the measurements, the spectra of the specimens before the layers were polished out were measured repeatedly under slightly different conditions (the impacting laser was focused on different places of the specimen, the specimen was removed from the chamber and put back again etc.). In Fig. 3, the spectra obtained by two different measurements of the specimen before polishing (solid lines) are compared to the spectrum of the specimen without the examined layer. Obviously, the reproducibility of the measurements is extremely good and all the shifts of individual peaks in the spectrum can be reliably ascribed to the presence/absence of the surface layer.

Our aim was to determine the elastic coefficients of the removed layers Q_{ij} by inverting the perturbation formula (7). This was done in two different ways:

1. The symmetry class of the examined material was considered as known, i.e. only three independent coefficients for cubic silicon were sought (Q_{11} , Q_{12} and Q_{33}) and two (Q_{11} and Q_{33}) for the isotropic silicon carbide.
2. Full elastic anisotropy of the layer was considered, which means six independent elastic coefficients Q_{ij} . However, as all the modes of vibration of the examined layer were forced by free vibrations of the specimen, the layers were loaded only in modes having the same symmetry as the substrates (i.e. in modes symmetric or antisymmetric with respect to symmetry planes of the substrates). This obviously precludes reliable determination of the coef-

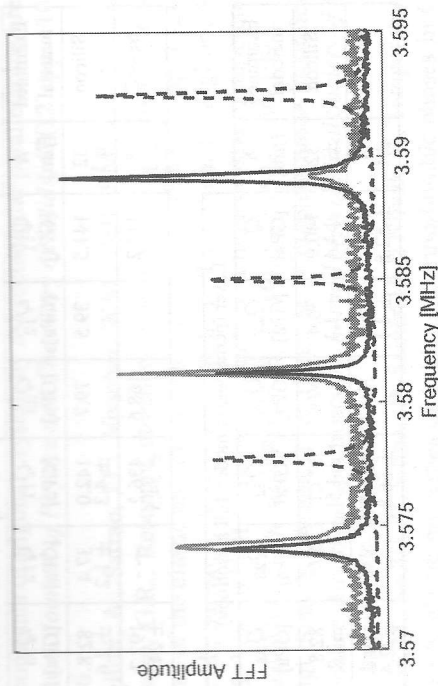


Figure 3: A selected part of the obtained spectrum (Si-SiC specimen) illustrating the reproducibility of the non-contact RUS measurements and the shifts induced by the absence of the surface layer. Solid lines (black and gray) correspond to two independent measurements of the original specimen, the dashed line shows how the resonant frequencies change after a 8 μm thick surface layer was removed.

ficients Q_{13} and Q_{23} , so only Q_{11} , Q_{22} , Q_{12} and Q_{33} were sought. (The coefficients Q_{13} and Q_{23} could be, however, determined by measurements on less symmetric substrates.)

In both cases, the sought coefficients Q_{ij} were calculated by numerical inversion of relation (7), where to the measured shifts of resonant frequencies were fitted in the least-square sense. In Tab. 1, the results are listed and compared to coefficients $Q_{ij}^{(s)}$ determined from the elastic coefficients of the substrate $C_{ijkl}^{(s)}$ by formula (8). The experimental errors displayed in Tab. 1 result from the accuracy of measurements of the removed layer, which was estimated to be about 1 μm.

In the case of the single crystal of silicon, this table shows how powerful tool the perturbation model can be. Not only that all the elastic coefficient for the known class of symmetry were determined with satisfying accuracy (especially when the uncertainty given by the thickness of the layer is taken into account), but also the cubic symmetry can be reliably identified: For cubic silicon, the constants Q_{11} and Q_{22} differ by less than 2%. For silicon carbide, the results are less satisfying. Although for the given symmetry class, the results are quite good, the isotropy requires $Q_{11} = Q_{22} = Q_{12} + 2Q_{33}$, which is here not fulfilled (difference larger than 10%). This may be ascribed to heterogeneity or porosity of the material or to the fact that for $h = 8 \mu\text{m}$, the uncertainty in the thickness (and plan-parallelism) of the removed layer is more significant.

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Examined material	h [μm]	Bulk material			Layer (perturbation model)		
		Q ₁₁ ⁽ⁿ⁾ [GPa]	Q ₁₂ ⁽ⁿ⁾ [GPa]	Q ₃₃ ⁽ⁿ⁾ [GPa]	Q ₁₁ [GPa]	Q ₁₂ [GPa]	Q ₃₃ [GPa]
Silicon	32 ± 1	141.5	39.5	79.7	142.0 ± 4.3	37.4 ± 1.2	82.8 ± 2.6
Si-SiC	8 ± 1	412.2	---	168.6	436.2 ± 54.5	---	192.7 ± 24.1

Examined material	h [μm]	Layer (perturbation model, full anisotropy)					
		Q ₁₁ [GPa]	Q ₁₂ [GPa]	Q ₁₃ [GPa]	Q ₂₂ [GPa]	Q ₂₃ [GPa]	Q ₃₃ [GPa]
Silicon	32 ± 1	140.9 ± 4.4	36.4 ± 1.1	N/A	143.1 ± 4.5	N/A	82.8 ± 2.2
Si-SiC	8 ± 1	422.4 ± 52.8	32.6 ± 4.1	N/A	454.4 ± 56.8	N/A	179.0 ± 22.4

Table 1: Comparison of in-plane elastic coefficients Q_{ij} determined by RUS on bulk specimens and by the perturbation model.

4 Conclusion

By introducing the perturbation theory into the RUS of thin surface coatings, the in-plane elastic coefficients of isotropic and cubic coatings can be easily and reliably determined. In future, the authors would like to focus on the effect of the disproportion between the elastic properties of the substrate and the coating (see paragraph 2.2) and the the analysis of the experimental errors of the obtained coefficients in dependence on various factors, such as symmetry of the substrate, etc.

Acknowledgements

This work was financially supported by the Czech Science Foundation (project No.202/09/P164), the Grant Agency of ASCR (project No. A200100627), the Czech Ministry of Education (project No. 1M06031) and the institutional project of IT ASCR CEZ: AV0Z20760514.

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The effect of cerium solutions on 316L stainless steel

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Abstract

Surface passivation is a technique for improving the corrosion resistance of stainless steel. In this work, we studied the effect of cerium treatment on 316L SS. Characterization techniques such as anodic polarization test, electrochemical impedance spectroscopy, and X-ray photoelectron spectroscopy were employed to correlate the corrosion behavior to surface treatments. Results showed that cerium passivation treatment increase corrosion protection of alloy due to the formation of amorphous oxidation that leads to diffusion control. This improvement is attributed to a more uniform and compact layer which is composed of oxide particles with higher oxygen and chromium concentrations.

Keywords: passive layer, 316L stainless steel, cerium, chemical treatment, electrochemical, SEM, XPS.

1 Introduction

Resistance of passive layer of stainless steel depends on the alloy composition and conditions in which it is generated. Chemical treatment on steel parts could improve passive layer [1]. Well-known method of surface modification involves the use of dichromate, a substance which is now recognized as both highly toxic and carcinogenic. The search for more environmentally acceptable alternatives has led to the identification of rare-earth metal species as possible replacements for the chromium [6].

The anodic dissolution behavior of active-passive metals in the presence of oxidizers is illustrated in figure 1, which shows a typical active-passive metal M