Advanced Methods for Perfusion Analysis in Echocardiography

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Summary

It has been shown that besides positron emission tomography, single photon emission computed tomography and magnetic resonance imaging; contrast echocardiography can be used for qualitative and quantitative myocardial perfusion assessment. In this review, the properties of ultrasound contrast agents, imaging techniques and acquisition methods are shortly described and the possibilities of perfusion echocardiography are summarized. The main focus is put on the description of three perfusion models: mathematical models, physical models assuming an ideal inflow and physical models including inflow measurement.

Key words

Echocardiography • Myocardial perfusion • Ultrasound contrast agent

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Introduction

The diagnostic possibilities of echocardiography have been extended with the development of ultrasound contrast agents (UCAs). These gas-filled microbubbles are administered into the blood stream and can be easily detected due to their nonlinear behavior (Hoff 2001). Over the last two decades the UCAs became a standard tool in different clinical and experimental applications, particularly in echocardiography. Several review papers have been already published on these topics, see e.g. (Mulvagh 2000, Lang and Mor-Avi 2006, Rakhit *et al.* 2007) and the reference therein.

The advantage of UCAs application has been reported to improve detection of blood-tissue interface, which enables to improve assessment of ventricular wall motion and delineation of endocardium (Hundley at al. 1998, Kornbluth et al. 2000) or some abnormalities of coronary arteries (Kaul et al. 1997). Another potential of the UCA application lies on tissue perfusion analysis. While this application field is still more experimental than clinical, first results indicate the usefulness for qualitative and quantitative perfusion assessment in simulated phantom studies (Potdevin et al. 2002, Arditi et al. 2006), in echocardiography (Wei et al. 1998, Hossack et al. 2004) and other applications like renal perfusion (Kaul et al. 2001, Forsberg et al. 2004) or cerebral perfusion (Rim et al. 2001, Eyding et al. 2002). This paper describes the principle of the perfusion methods and gives an overview of the underlying models and their applications focused on myocardial perfusion.

Contrast agents and perfusion imaging techniques

The first generation of UCAs had many disadvantages (rapid dissolving in blood and large diameter) which limited their applications predominantly to cardiac shunt detection and examination of right heart structures. Recently, UCAs have attained a prolonged persistence and smaller mean diameter, around 2 μ m, which can be achieved using a special bubble shell (lipid, polymer etc.) and filling gas (perfluoropropane,

PHYSIOLOGICAL RESEARCH • ISSN 0862-8408 (print) • ISSN 1802-9973 (online) © 2010 Institute of Physiology v.v.i., Academy of Sciences of the Czech Republic, Prague, Czech Republic Fax +420 241 062 164, e-mail: physres@biomed.cas.cz, www.biomed.cas.cz/physiolres perfuorocarbon etc.). The list of the second generation of UCAs may be found for example in (Mulvagh 2000). The images and results presented below were obtained with the SonoVue[®] contrast agent. The shell of these microbubbles consists of a flexible membrane of phospholipids with a hydrophilic surface on the outside and a hydrophobic surface on the inside. The gas in SonoVue microbubbles is sulphur hexafluoride (Greis 2004).

The UCAs are intravascular contrast agents, as the vessel wall is not permeable for microbubbles. The high echogenity of the UCAs allows tracking of the contrast bubbles in the blood and hence examining of the tissue perfusion. Two techniques have been developed for perfusion analysis on the microcapilary level.

The first imaging method, called destructionreplenishment, uses continuous (or slow) UCA bolus injection. For each imaging sequence, several destructive with high ultrasound pulses ultrasound power (mechanical index MI>1) are transmitted into imaging tissue to destroy the contrast bubbles in the imaged plane. This destruction is followed by a low power imaging phase (with low MI, around 0.1) to measure the rate of UCA replenishment (Rim et al. 2001). The time-varying image intensity *I(t)* in a specific region of interest (ROI), which corresponds to the UCA concentration, can be modeled as $I(t) = A(1-e^{-\beta t})$, where β represents the rate of the UCA replenishment and A is the steady ROI intensity. It can be shown that $A\beta$ is proportional to the blood flow through the ROI and A is proportional to the blood volume in the ROI (e.g. Rim et al. 2001).

The second imaging method uses fast UCA bolus injection followed by a flush of normal saline solution. This approach is often referred to as a *bolus kinetic* (Eyding *et al.* 2002) technique and will be described in more detail in the following sections.

Data acquisition and preprocessing

The image sequence used for perfusion analysis is recorded following the contrast agent administration. The aim is to record the UCA concentration development in time for particular myocardial ROIs. The physical quantity proportional to the UCA concentration is the backscattered ultrasound intensity (Bartoš *et al.* 2008), calculated as the mean intensity within the ROI. To improve the contrast between the signal backscattered from the tissue and from the UCA, second harmonic signal is utilized. This approach is based on highly nonlinear scattering of the UCA, in contrast to fairly linear scattering in the tissue. Hence, the ultrasound scanners are used in the pulse inversion, power modulation or harmonic imaging modes (Vannan 2000).

One of the major problems in perfusion analysis in echocardiography is the suppression of displacement in the successive images in the recorded sequence. This is mainly due to the movement of the patient, ultrasound probe and breathing. Alignment of displaced images (image registration) is based on searching for an optimal geometrical transformation of the sequence images with respect to one reference image from the sequence (Gardner 2004, Kolar *et al.* 2009).

Another important issue has been suppression of attenuation. This is important especially in echocardiography, where the intensity of reflected ultrasound waves from myocardium segments is influenced not only by the UCA concentration in it but also by the UCA concentration in the heart cavity between the ROI and the probe. Available solutions are not robust and automated enough yet (e.g. Mischi *et al.* 2005, Zwirn *et al.* 2009).

Perfusion models

During perfusion analysis a fast UCA bolus is administered into the blood stream and the image sequence is recorded. The ROI defines a specific myocardial tissue for perfusion analysis (see Fig. 1a). The *fast bolus* imaging method results in a perfusion curve (Fig.1b) extracted from the myocardial ROI. Processing and analysis of these perfusion curves representing the time-varying concentration lead to estimation of the parameters related to the perfusion in the ROI. Based on the model complexity, these parameters may be heuristic indices related to the perfusion state of the tissue or they can be physical quantities based on physical modeling of the perfusion process. Three quantitative parameters related to the myocardium perfusion properties on the microvascular level may be estimated:

- 1. Mean transit time (MTT) average time needed for bubbles to pass through the ROI in [s].
- Blood volume (V_b) volume of blood in the ROI per tissue weight [ml/g].
- Blood flow (F_b) blood flow [ml/min] in the ROI per tissue weight [ml/min/g].

Two additional physiological values have to be known to be able to estimate these parameters: tissue density and hematocrit correction factor, etc. (Jackson



Fig. 1. a) One image from recorded sequence with ROI. b) Time varying mean ROI intensity, which corresponds to the UCA concentration c(t). c) Measured intensity and fitted curves using Log-Normal and Erlang model, d) Measured intensity and fitted curves Gamma LDRW usina and model.

et al. 2005).

Three different approaches for qualitative or quantitative perfusion description have been reported. They will be described in the following sections. The mathematic formulas are included for comprehensiveness.

Mathematical models

These models are based on the shape similarity between the perfusion curve c(t) and a specific mathematical function used for data fitting. There is no exact physical interpretation of the model parameters. The Log-Normal distribution $f_{Log-Norm}(t)$ is a favorite fitting function in dilution techniques (e.g. Rognin 2008) and is therefore convenient in perfusion applications. It is defined as:

$$f_{Log-Norm}(t) = \frac{1}{t\sigma\sqrt{2\pi}}e^{-\frac{(\ln(t)-\mu)^2}{(2\sigma)^2}},$$
 (1)

where the parameters μ and σ define the shape of this function and must be estimated to fit the shape of the measured curve (see Fig. 1c). These parameters describe indirectly the perfusion state of the analyzed myocardium.

Physical models assuming an ideal inflow

These models are based on a physical description of the tissue perfusion and describe the

cardiovascular system between the bolus application and the tissue ROI. Furthermore, an ideal bolus (infinitely short injection, but in practice very fast bolus injection in comparison to MTT) is assumed at the input of the myocardial ROI. Two models which are used for perfusion modeling are adopted from dilution techniques: *compartment* model with an ideal input (e.g. Mischi *et al.* 2008) and the *random walk* model with an ideal input (Mischi *et al.* 2005).



Fig. 2. Single compartment with a constant blood volume V_{b_r} constant blood flow F_b and a time varying UCA concentration c(t).

Compartment modeling is based on a mathematical description of a small ideal *mixing chamber* with a unidirectional UCA washout and with a constant flow rate F_b (Fig. 2). Each part of the cardiovascular system can be considered as one compartment, e.g. left ventricle, a part of some artery or a perfused myocardium region. The modeled UCA concentration $f_c(t)$ in one compartment after applying an ideal bolus can be

mathematically described as an exponentially decreasing function:

$$f_c(t) = c_0 e^{-\frac{t}{\tau}}, \qquad (2)$$

where τ is a time constant depending on the blood flow rate (i.e. perfusion) and the compartment volume as $\tau = V_b/F_b$ and c_0 is the UCA concentration at time t=0 (the beginning of the measurement). This simplest model of one compartment can be extended to a more complex *multi-compartment* model. This leads to Erlang distribution (Mischi *et al.* 2008):

$$f_{Erlang}(t) = c_0 \frac{e^{-\frac{t}{\tau}} \left(\frac{t}{\tau}\right)^{(k-1)}}{(k-1)!},$$
(3)

where the new parameter k defines the number of compartments. An example of perfusion curve fitting using this model is shown in Figure 1c.

Generalization (for non-integer k) of this model is also used and is called Gamma distribution (Mischi *et al.* 2008):

$$f_{Gamma}(t) = c_0 \frac{e^{-\frac{t}{\tau}} \left(\frac{t}{\tau}\right)^{(k-1)}}{\Gamma(k)}, \qquad (4)$$

where $\Gamma(k)$ represents a special type of a mathematical function, called Gamma function (Rektorys 1994). An example of perfusion curve fitting using this generalized model is shown in Figure 1d.

The *local density random walk* (LDRW) model has been introduced by Sheppard and Savage (Sheppard and Savage 1951) and adopted for estimation of the ejection fraction using UCA by Mischi (Mischi *et al.* 2005). This LDRW model can be used also for perfusion analysis where it describes an ideal injection of the UCA bolus and its behavior in a straight infinitely-long tube. Due to a constant blood velocity and Brownian motion of the UCA bubbles, the time-varying concentration can be described as (Mischi *et al.* 2005):

$$f_{LDRW}(t) = \frac{1}{\mu} e^{\lambda} \sqrt{\frac{\lambda\mu}{2\pi t}} e^{-\frac{\lambda}{2} \left(\frac{t}{\mu} + \frac{\mu}{t}\right)}, \qquad (5)$$

where μ is the mean transit time through the modeled tube and λ determines the type of the UCA behavior in the blood stream. Both parameters are related to the ROI perfusion. An example of curve fitting using this model is shown in Figure 1d.

Physical models including inflow measurement

This approach has been extensively used in perfusion imaging using positron emission tomography (PET) (Akinboboye et al. 2001), electron beam computed tomography (EBCT) (Mohlenkamp et al. 2003) and magnetic resonance imaging (Ostergaard 2005), but so far, surprisingly, very little in ultrasonography (Quaia 2005). It is also partly based on the compartment theory. However, compared to the above described physical models, these models describe the UCA kinetics directly for the ROI. The effect of the cardiovascular system between the bolus-administration location and the ROI and the non-ideal bolus administration are included in the arterial input function (AIF). In myocardial perfusion applications the AIF(t) is usually measured as the perfusion curve in the left ventricle (LV), because blood from LV (from the aorta, respectively) directly fills the coronary arteries. The change of the AIF between the measurement location and the ROI location is neglected.

Myocardial ROI can be considered either as a homogenous compartment or, more generally, as a complicated microvasculature region. The latter model is based on a concept of the tissue residue function R(t)(Ostergaard 2005), which can be considered as the normalized UCA concentration curve that would be measured in the ROI in case of an ideal AIF.

Having AIF(t) measured in the left ventricle and c(t) in the analyzed myocardium, three quantitative perfusion parameters can be estimated (blood volume, blood flow and mean transit time) from the following equations. Blood volume V_b can be estimated directly from the measured curves c(t) and AIF(t) and the assumed tissue density ρ :

$$V_{b} = \frac{1}{\rho} \frac{\int c(t)dt}{\int AIF(t)dt},$$
(6)

where the symbol \int denotes the area under the respective measured curve. Blood flow F_b can be estimated from:

$$c(t) = \rho F_b R(t) * AIF(t), \qquad (7)$$

using appropriate mathematic operations, including deconvolution and assuming that R(t=0)=1 (Ostergaard 2005). The third perfusion parameter is the mean transit time described above. It is related to the blood flow and

blood volume as (Ostergaard 2005):

$$MTT = \frac{V_b}{F_b} \,. \tag{8}$$

Results and discussion

Three examples related to the myocardium perfusion analysis are given in this section. The presented results are based on our experiments with GE VingMed System 5 ultrasound scanner and SonoVue contrast agent. The analyzed contrast sequences were acquired after UCA bolus administration of 2.5 mg, followed by a saline flush bolus. The recordings were triggered by ECG and only end-systolic and end-diastolic images were recorded from each cardiac cycle to decrease the probability of bubble destruction.

Experiment 1

As mentioned above, one of the main difficulties is the time dependent attenuation caused by time varying UCA concentration in the LV. Therefore, the attenuation coefficient has to be estimated before perfusion analysis in order to obtain reliable results. This can be done by employing the exponential-decay model (Zwirn et al. 2009) and rough manual LV segmentation. An example of the attenuation coefficient estimation is depicted in Figure 3a for the end-diastolic sequence. These numbers correlate with the attenuation values estimated in perfusion analysis of experimental animals (Mule et al. 2008) and in vitro phantom studies (Chen et al. 2002). The curve shape follows the increasing and decreasing UCA concentration during dilution process of the bubbles in the left ventricle. Figure 3b shows how this attenuation coefficient influences the perfusion curve from defined myocardium ROI. The perfusion curve before the correction lacks the typical dilution peak, but after attenuation compensation the curve follows the expected shape.

Experiment 2

In this experiment, perfusion was examined in the apical, mid and basal segments of the myocardial septum in the end-systolic phase (Fig. 4a). Three ROIs were manually placed in the corresponding segments and perfusion curves were extracted from the recorded sequence. The analysis was based on curve-fitting using the LDRW model (Fig. 4 b, c, d), where the perfusion



Fig. 3. a) The estimation of the time-varying attenuation coefficient. **b)** The perfusion curves before (dashed line) and after attenuation compensation (solid line).

parameter *MTT* is directly represented by model parameter μ (see equation 5). The results of this estimation are: $MTT_{basal} = 6.3$ s, MTTmid = 9.6 s and $MTT_{apical} = 10.3$ s, which correlates with findings in (Malm *et al.* 2005), where destruction-replenishment approach has been used.

Experiment 3

The intensity curves AIF(t) (Fig. 5, left) and c(t) (Fig. 5, right) were measured in the left ventricle and the mid posterior segment of the myocardium, respectively (healthy volunteer recording). Before processing, the curves were smoothed by averaging using a 7-sample window. The tissue residue function (Fig. 5, middle) was estimated by a method of parametric deconvolution assuming a compartment model of the ROI. Figure 5, right, shows the correspondence of the measured



perfusion curve c(t) and its approximation by the convolution of AIF(t) and R(t). The above perfusion parameter estimation results in $F_b = 41$ ml/min/100g, $V_b = 5$ ml/100g, MTT = 8 s, which is in the range reported for myocardium using other perfusion analysis methods (e.g. Mohlenkamp *et al.* 2003).

Conclusion

This review has described the possibilities and problems of perfusion analysis in echocardiography. There are two main approaches: destructionreplenishment method and bolus-kinetic method. Here, the main focus has been put on the bolus kinetic approach and its mathematical description, because it is still in a research stage and might be of high diagnostic potential. The principal advantage of this method is that the bolus injection is cheaper and easier to perform than the destruction-replenishment method, where automatic injection equipment and a higher UCA dose is needed to obtain reliable results.

Dynamic contrast-enhanced echocardiography is



Fig. 4. a) The rough position of three analyzed myocardial regions; **b**, **c**, **d)** Three measured and fitted perfusion curves obtained from ROIs in the apical septum segment (b), mid septum segment (c) and basal septum segment (d). The corresponding values of the *MTT* are shown in respective curves.

a promising tool for a less invasive assessment of myocardial perfusion in comparison to the well accepted standard represented by positron (or single photon) emission computed tomography. The main problems of fully automatic perfusion analysis in echocardiography in clinical practice are moving artifacts, ultrasound attenuation due to tissue and due to time-varying UCA concentration and also segmentation of the blood pool and myocardium. The choice of the underlying pharmacokinetic model and the parameter-estimation procedure remains an open question. Also the acquisition protocols have not been standardized yet. The choice of the acquisition parameters is based on physician's experience. This concerns mainly the UCA dosage (UCA volume and concentration) and the ultrasound scanner setting (mainly the used frequency, mechanical index and imaging mode).



Fig. 5. Example curves used in deconvolution-based perfusion analysis. Left: AIF(t) measured in the left ventricle. Middle: Tissue residue function estimated by deconvolution. Right: Measured and approximated perfusion curve c(t).

Conflict of Interest

There is no conflict of interest.

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