

Thermoelectric power generation-materials

what makes a good thermoelectric:

$$ZT = \frac{\alpha^2}{\rho\lambda} T$$

conflicting requirements



- α – Seebeck coefficient - large
- ρ – resistivity - small
- λ – thermal conductivity - small

- development of novel materials
- material tailoring – crystal chemistry
- composites–microstructure, nanostructure

up-to-date best bulk thermoelectrics: - $\text{Bi}_2\text{Te}_3/\text{Sb}_2\text{Te}_3$, PbTe, Si-Ge

NEW BULK MATERIALS:

Skutterudites, Heussler alloys, complex chalcogenides, oxides

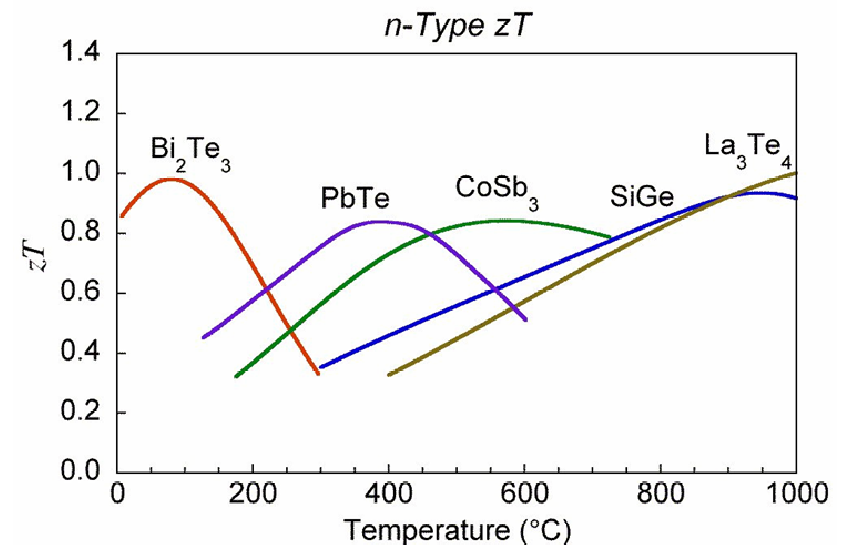
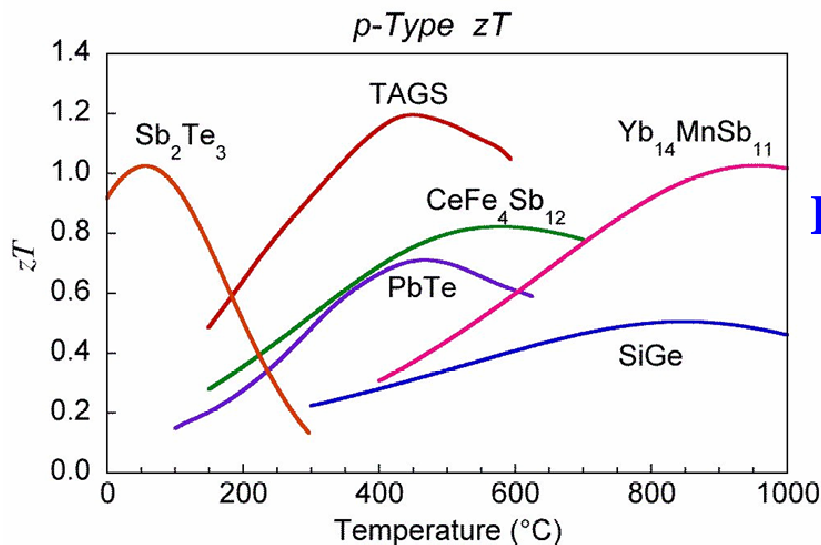


Figure of Merit

ZT

Classical guidelines for thermoelectric materials : - semiconductors, but which???

α, ρ, λ \longleftrightarrow Electronic structure, scattering mechanism, phonon spectrum,...

Two approaches:
 ✓ Boltzman Equation of transport
 ✓ Kubo formalism...

Increase of ZT

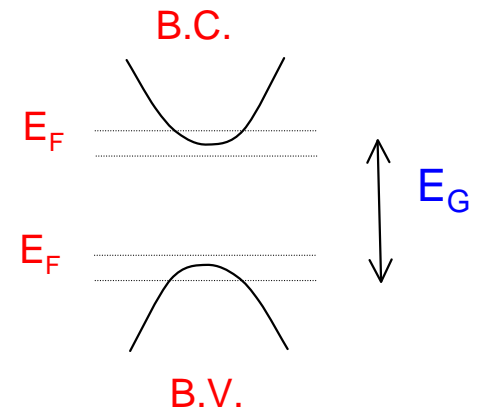
$$ZT = \frac{\alpha^2}{\rho(\lambda_{electron} + \lambda_{lattice})} T$$

➔ To adjust Fermi level E_F (optimal doping,...)

E_F should be at the edge of the band, sharp variation of DOS, $\Leftrightarrow \alpha \sim \pm 200 \mu\text{V/K}$

➔ $\frac{\mu}{\lambda_{lattice}} (m^*)^{3/2}$ highest as possible

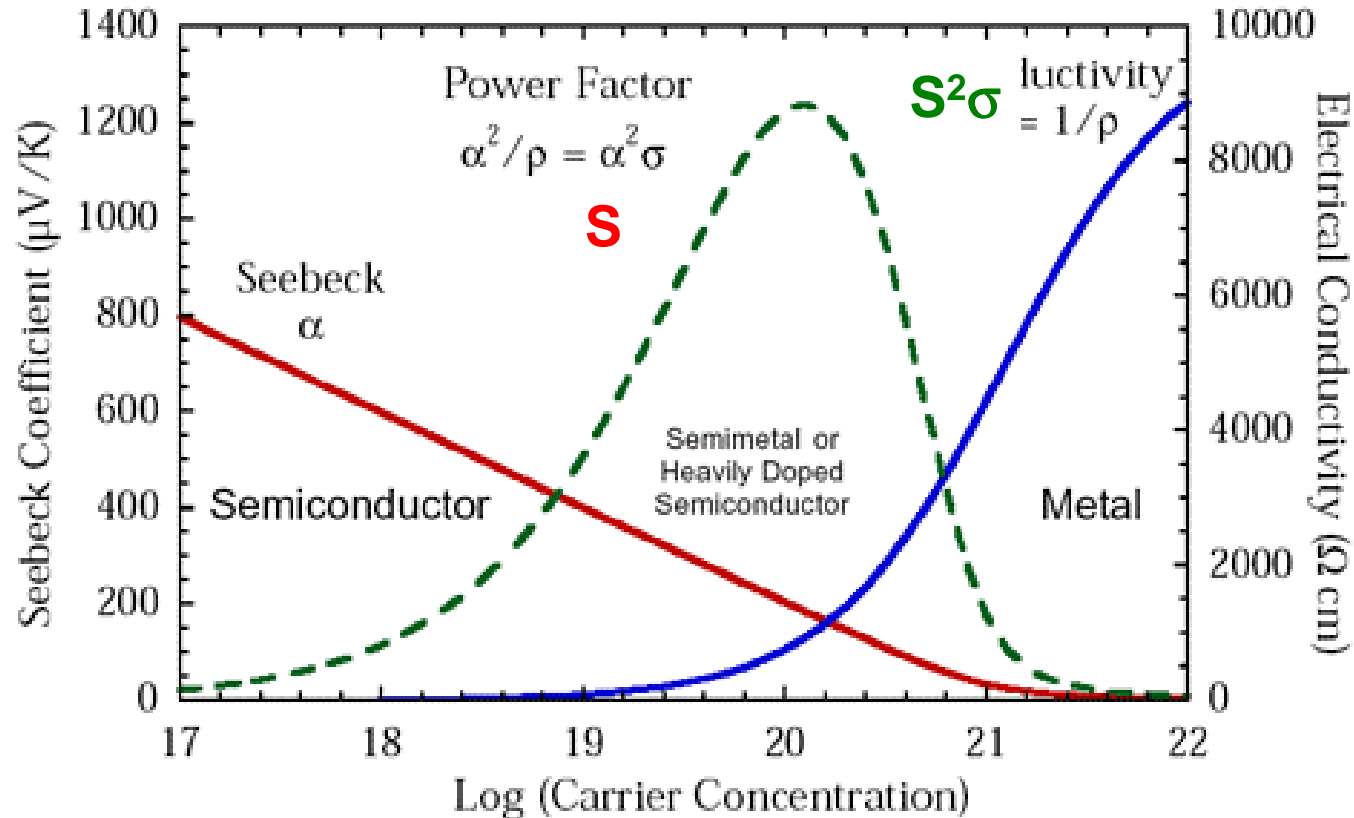
Semiconductors with a high mobility (μ), high effective mass (m^*) and low thermal conductivity of the lattice ($\lambda_{lattice}$)



Which materials are interesting???

– semiconductors –

Optimizing power factor \rightarrow highly doped semiconductors



For almost all typical thermoelectric materials, namely **low gap semiconductors**, if doping is increased, the electrical conductivity increases but the Seebeck coefficient is reduced.

$$P_f = \frac{\alpha^2}{\rho}$$

The Thermoelectric Figure of Merit (ZT)

Optimizing Figure of merit ZT



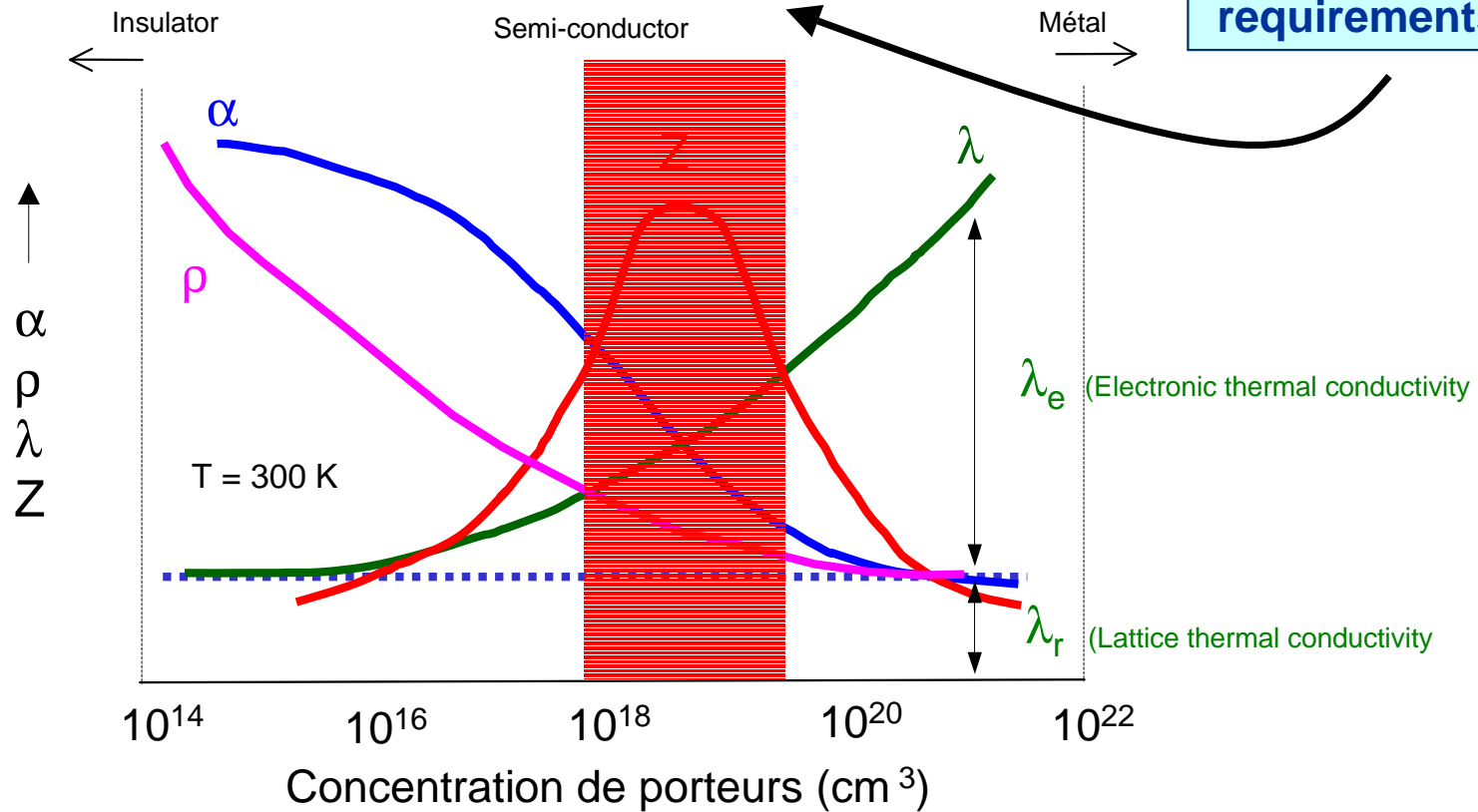
minimize the thermal conductivity

$$ZT = \frac{\alpha^2}{\rho\lambda} T$$

$$Z = \frac{\alpha^2}{\rho\lambda}$$

Ideal material : $\alpha \uparrow, \rho \downarrow, \lambda \downarrow$ but $\alpha \uparrow \Leftrightarrow \rho \uparrow$ et $\rho \downarrow \Leftrightarrow \lambda \uparrow$

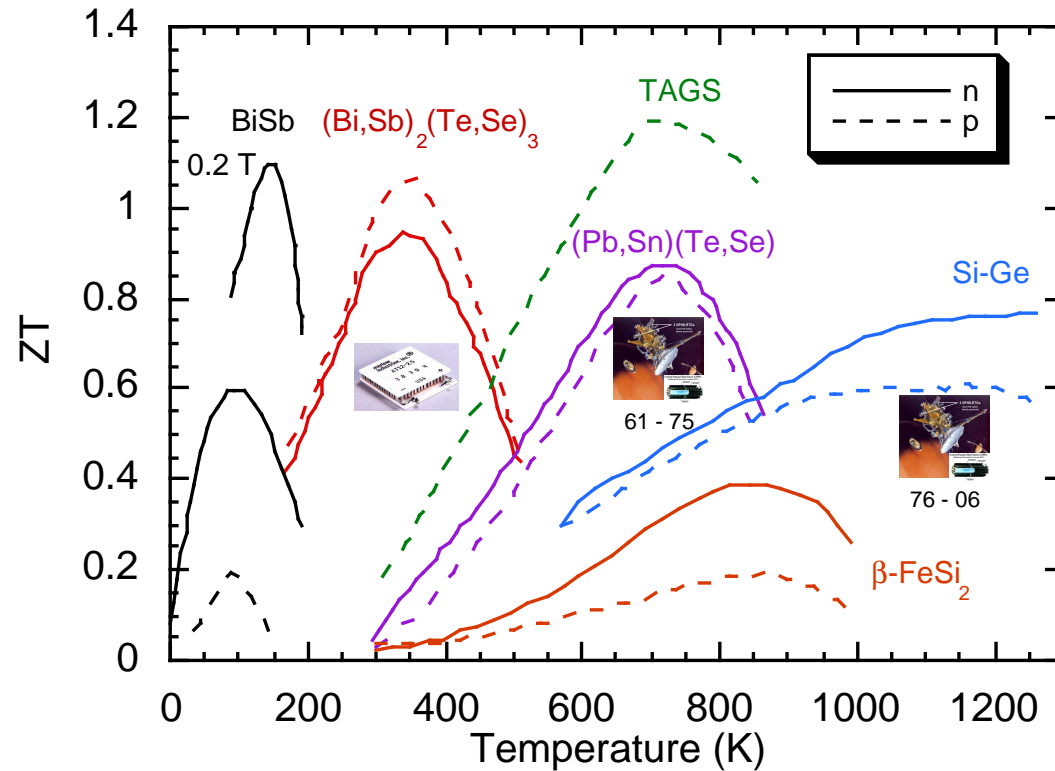
conflicting requirements



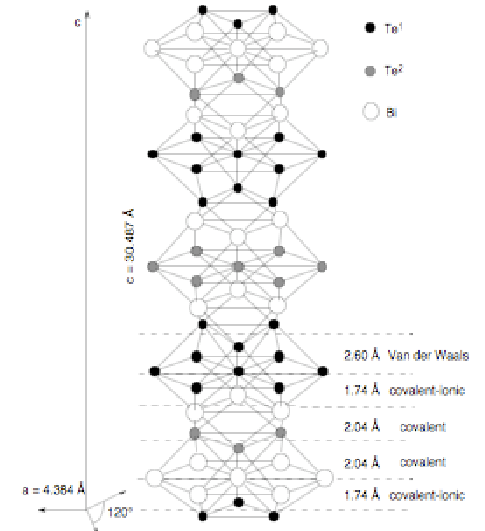
Best compromise → still highly doped semiconductors ($\lambda = \lambda_e + \lambda_r$)

1930 - 1995 : Classical materials...

Limits in ZT (~ 1) ...Limits in temperature ($T < 250$ °C)



TAGS : $(\text{AgSbTe}_2)_{1-x}(\text{GeTe})_x$



- SC low gap + heavy elements
- ZT optimized only for narrow temperature window
- At $T \sim 300$ K used solutions based on Te, namely (Bi_2Te_3)
- ZT ~ 1 standard

Since 1995 - ... : New orientations

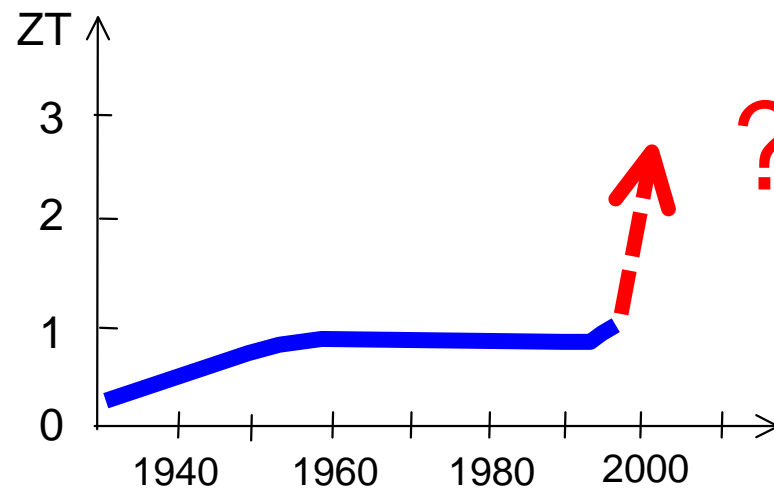
Environmental problems (Kyoto...), energy, waste heat, etc → New interest in thermoelectricity (USA, Japon, Europe is still on the tail....)

Proposal of new concepts to target new materials, need systems with $ZT > 1$

Thermoelectrics based on lowered dimensionality, nanostructuring, ...

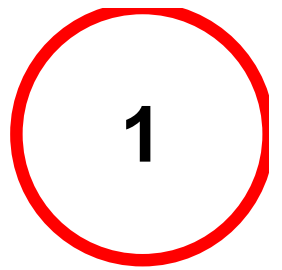
Identification of new bulk materials....

1



2

Motivation for Nanotechnology in Thermoelectricity



(2D quantum wells, 1D nanowires, 0D quantum dots)

$$ZT = \frac{S^2 \sigma T}{\kappa}$$

Seebeck Coefficient S , Conductivity σ , Temperature T , Thermal Conductivity κ

$ZT \sim 3$ for desired goal

Difficulties in increasing ZT in bulk materials:

$$S \uparrow \iff \sigma \downarrow$$

$$\sigma \uparrow \iff S \downarrow \text{ and } \kappa \uparrow$$

\Rightarrow A limit to Z is rapidly obtained in conventional materials

\Rightarrow So far, best bulk material ($\text{Bi}_{0.5}\text{Sb}_{1.5}\text{Te}_3$) has $ZT \sim 1$ at 300 K

Low dimensional physics gives additional control:

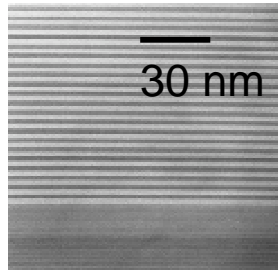
- Enhanced density of states due to quantum confinement effects
 \Rightarrow Increase S without reducing σ
- Boundary scattering at interfaces can reduce κ more than σ
- Possibility of materials engineering to further improve ZT

Low dimensionality- impact on thermopower, thermal conductivity

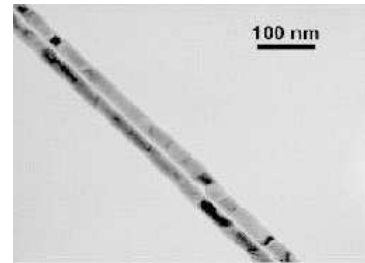
1



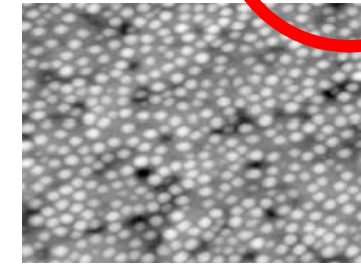
3 D



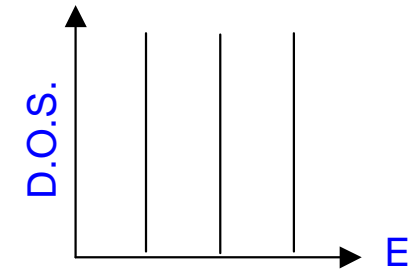
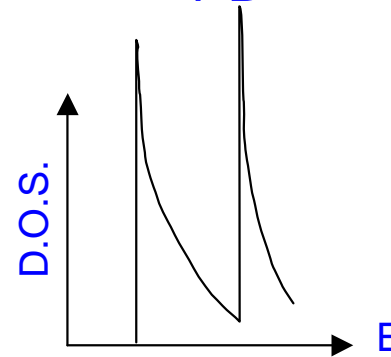
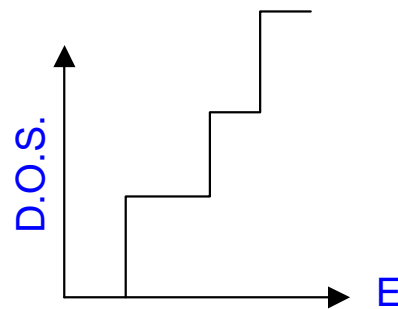
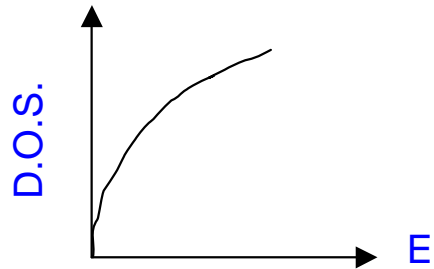
2 D



1 D



0 D

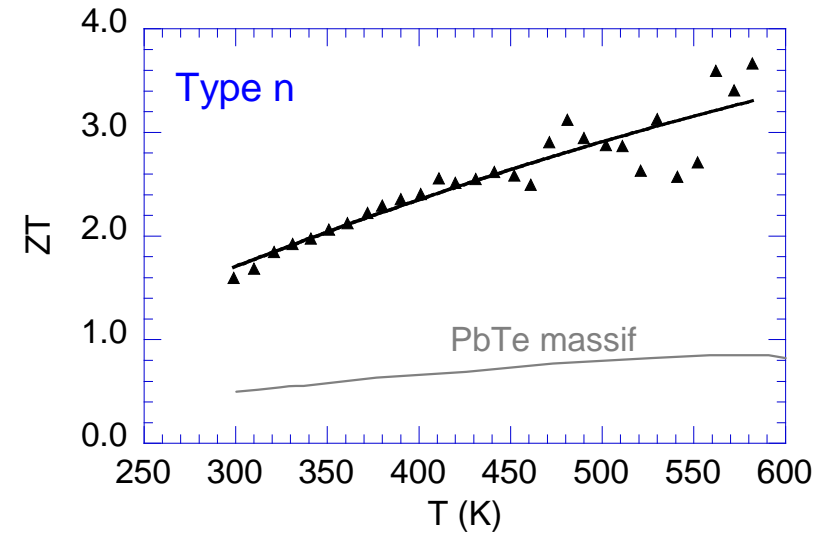
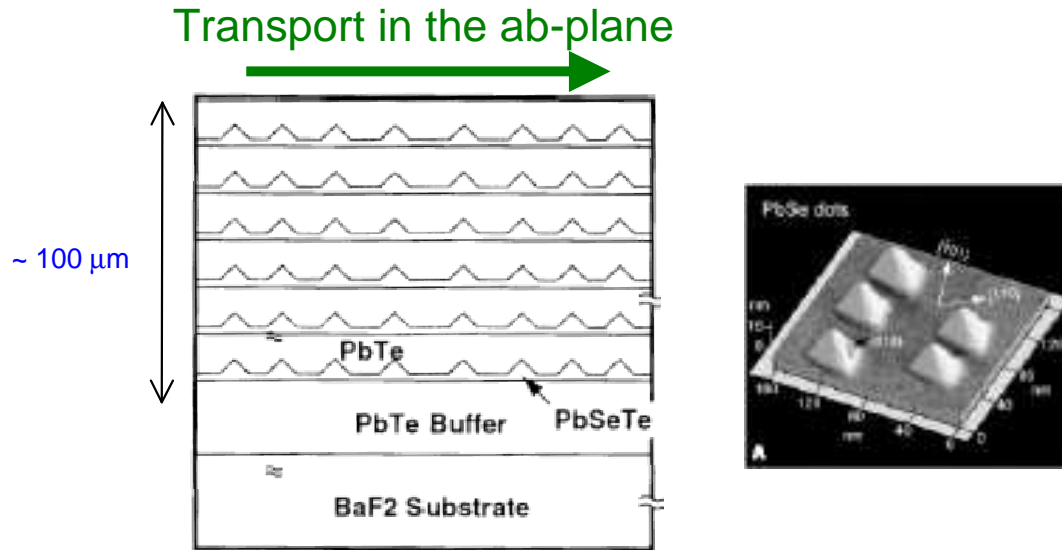


- (D.O.S.) more favourable (stronger dependence of DOS on E)
→ increase of α without increasing ρ
- additional degree of freedom (size) for tailoring of the transport
- possibility to explore the anisotropy of transport properties
- chance to decrease λ_{lattice} due to phonon scattering on interfaces
- $ZT_{0D} > ZT_{1D} > ZT_{2D} > ZT_{3D}$

Theoretical predictions – decrease of the dimensionality

1

Heterostructures PbSeTe/PbTe (MBE)



(Harman et al., J. Electron. Mater., **29**, L1, 2005)

Plots de PbSeTe dans des couches de PbTe

- Type n : ZT ~ 1,5 à 300 K (compared to 0,45 pour PbTe bulk),
- ZT ~ 3,5 à 570 K
- Type p : ZT ~ 1,1 à 300 K.

DUE TO:

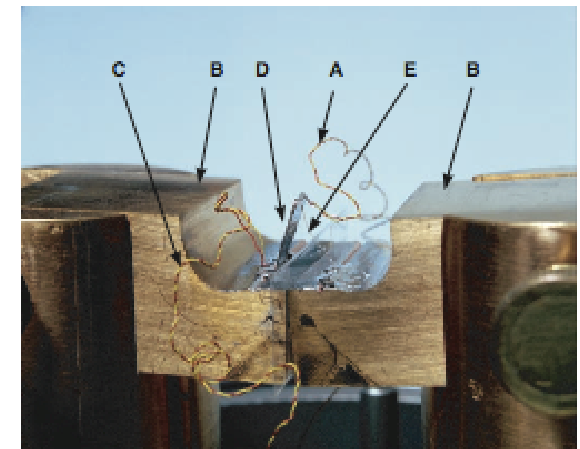
- Confinement of charge carriers in 2D
- Decrease of lattice thermal conductivity due to scattering

-EXAMPLE (laboratory):

(Harman et al., Science., **297**, 2002)

- Cooling: junction cooled 44 K below RT (31 K pour Bi_2Te_3)
- Power generation : 2,2 W/cm² for $\Delta T = 220$ K

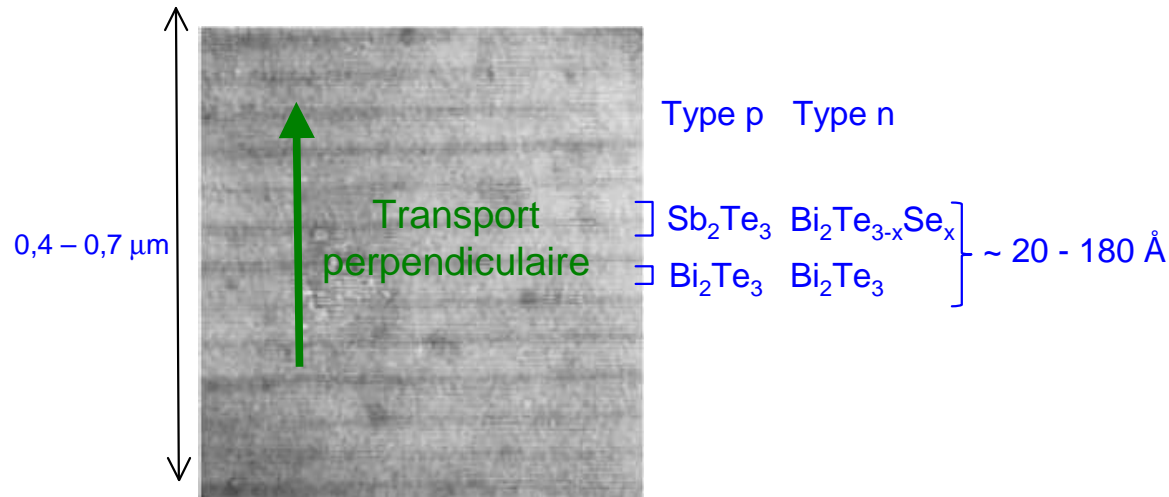
(Harman et al., APL., **88**, 243504, 2006)



Superstructures based on (Bi,Sb,Te,Se) - MOCVD

(Venkatasubramanian et al., PRB, **60**, 3091, 2000, Nature, **413**, 2001)

1



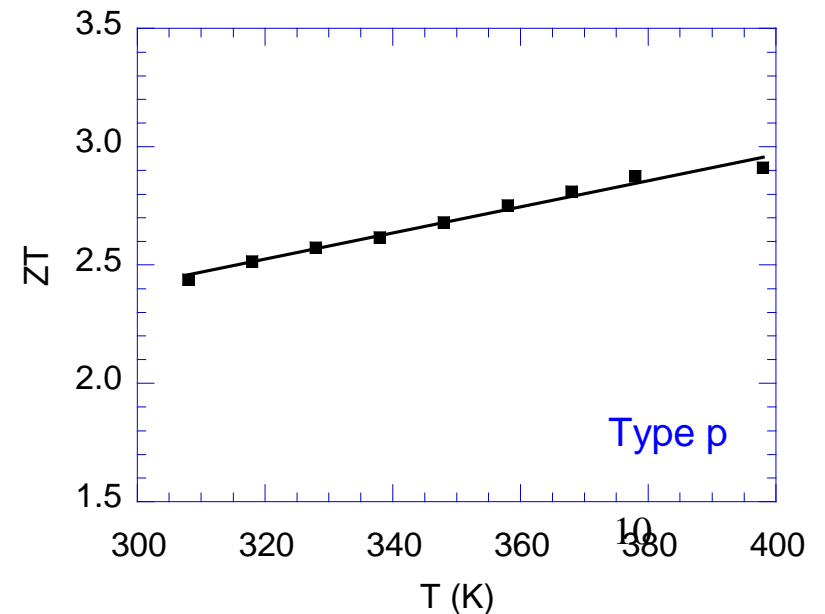
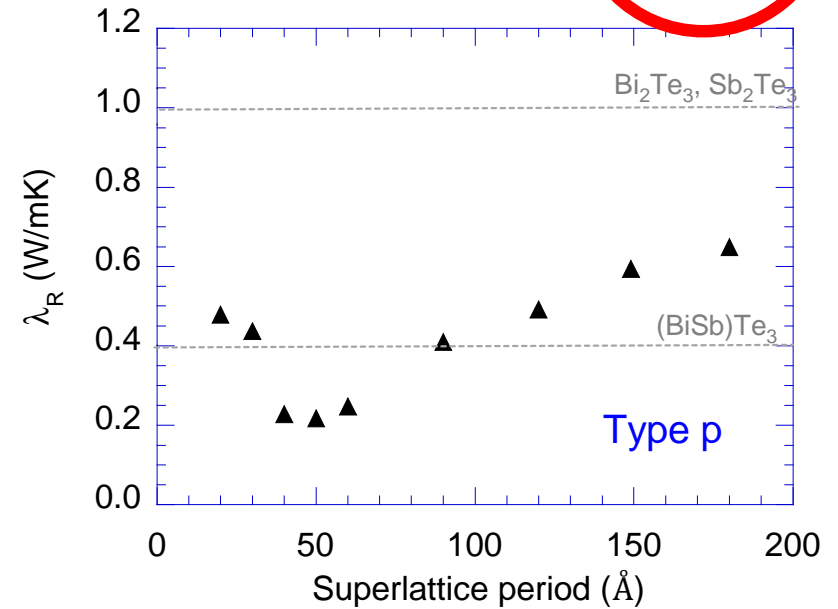
Negligible confinement of charge carriers **BUT**

Interfaces block short wavelength phonons!

Thermoelectric performance

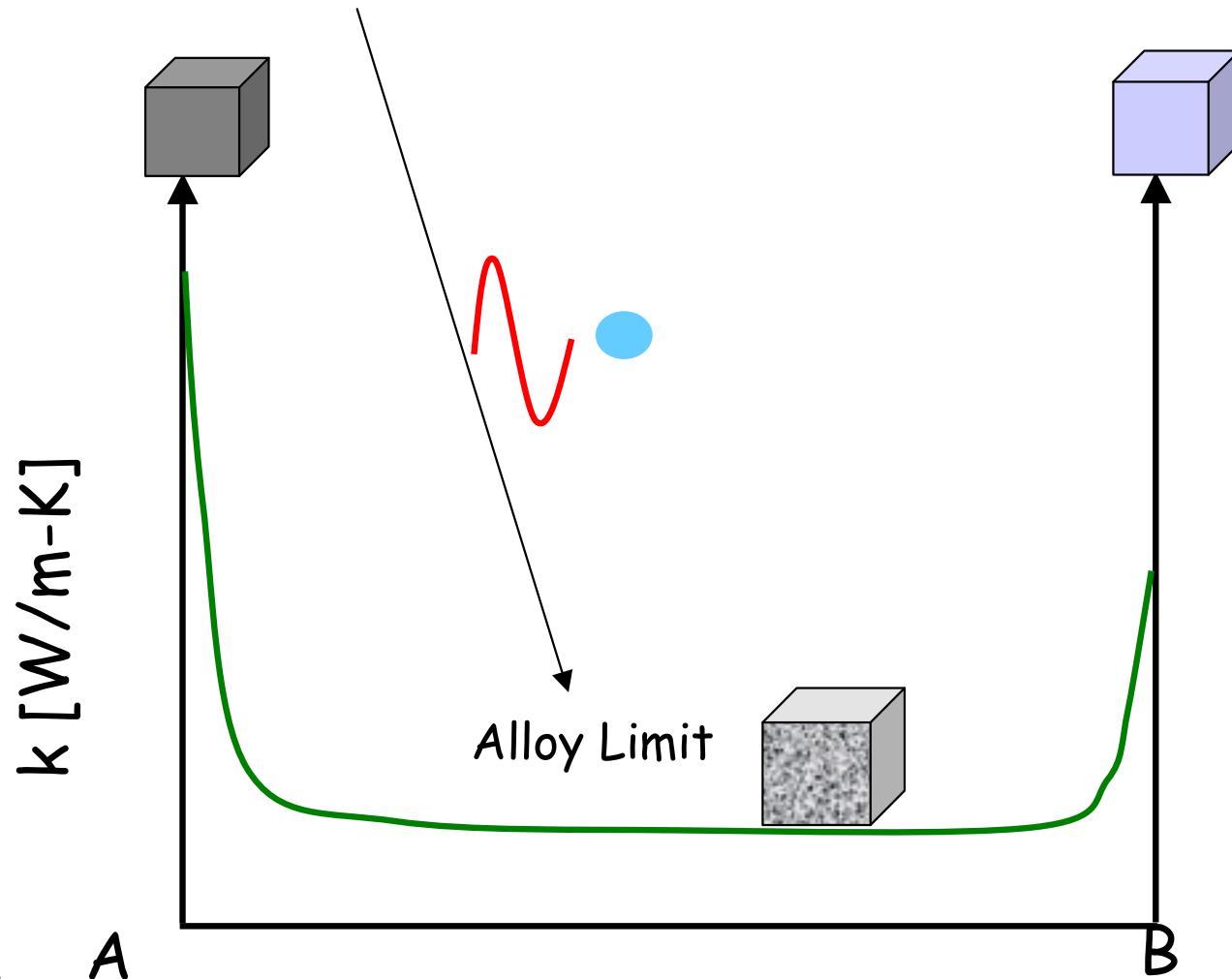
Type p : $ZT \sim 1,7 - 2,4$ à 300 K

Type n : $ZT \sim 1,4$ à 300 K



Alloy Limit of Thermal Conductivity

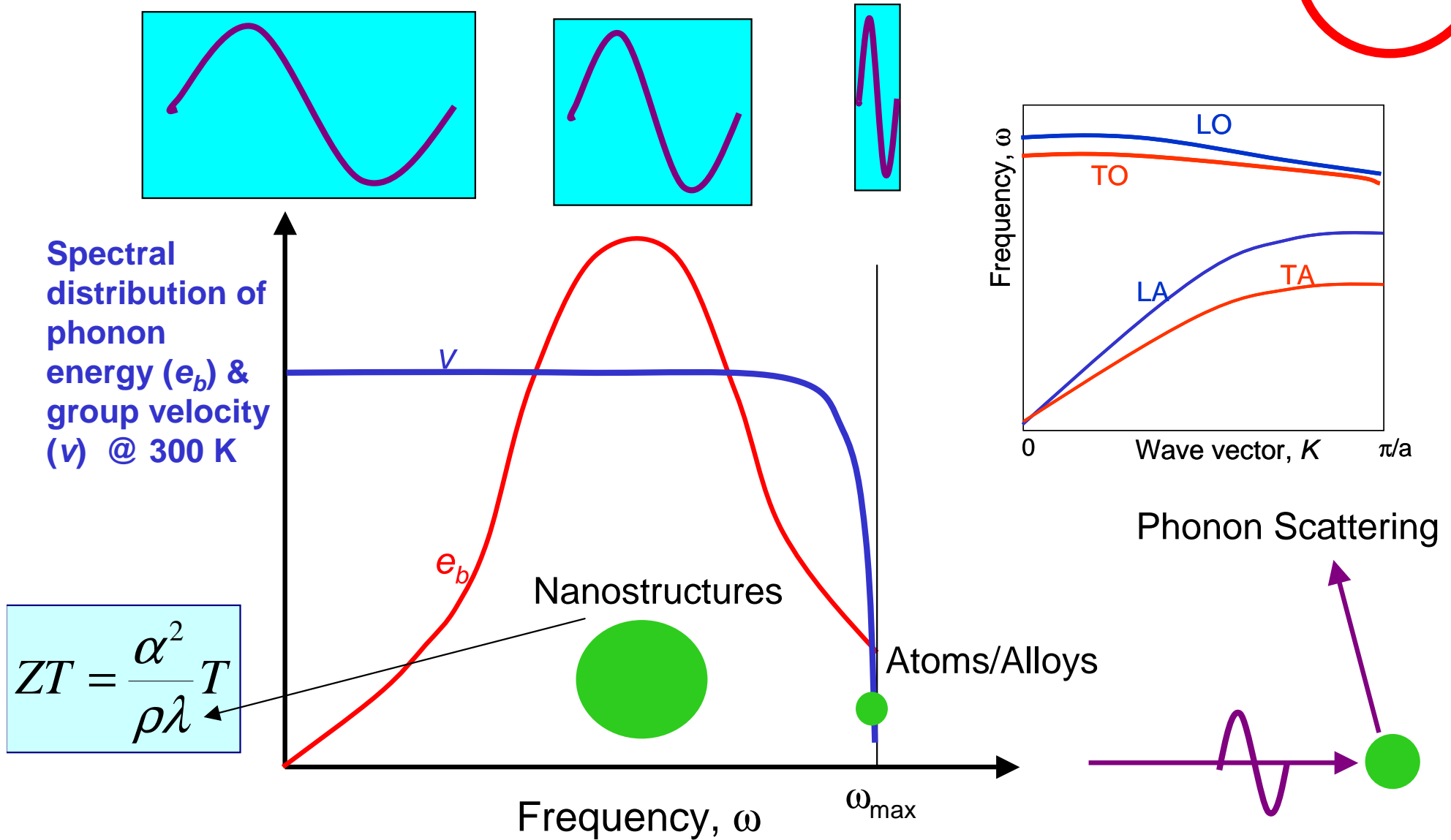
$$ZT = \frac{\alpha^2 T}{\rho \lambda}$$



Impurity and alloy atoms scatter only short - λ phonons that are absent at low T!

NANOSTRUCTURING- decrease of thermal conductivity: Phonon Scattering with Imbedded Nanostructures

1



$$ZT = \frac{\alpha^2}{\rho\lambda} T$$

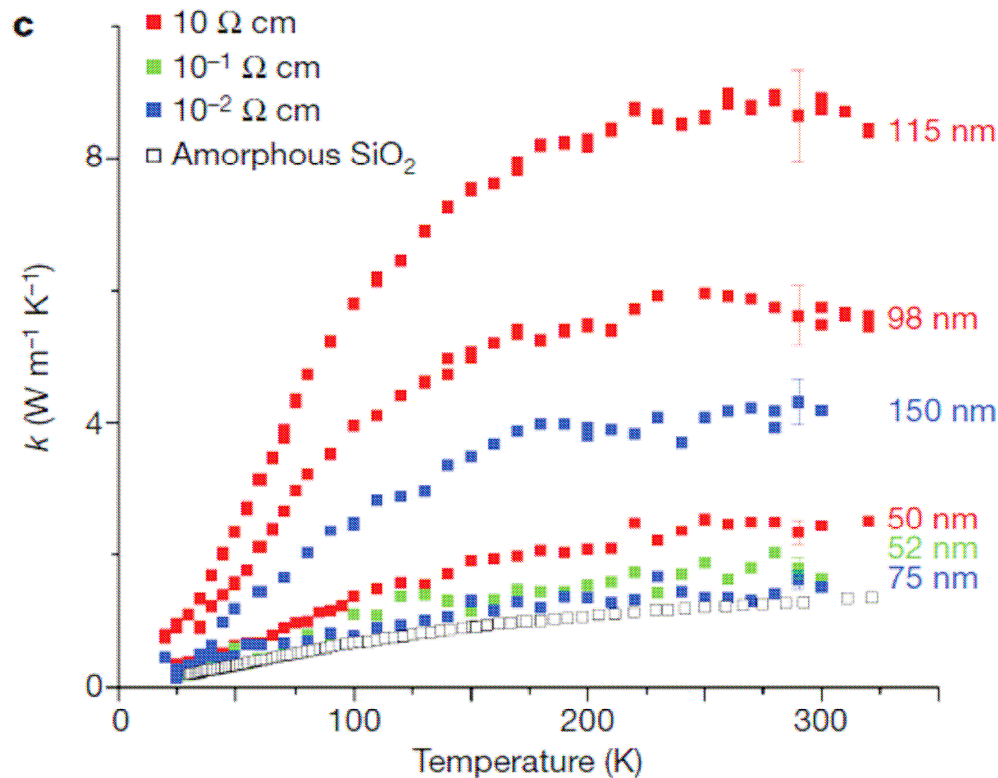
Long-wavelength or low-frequency phonons are scattered by imbedded nanostructures!

NANOSTRUCTURING- decrease of thermal conductivity: Phonon Scattering on nanostructure interface

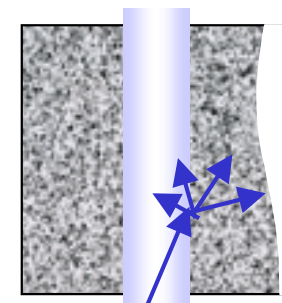
1

“Phonon engineering” thermoelectrics

Artificial nanostructuring: Si nanowires

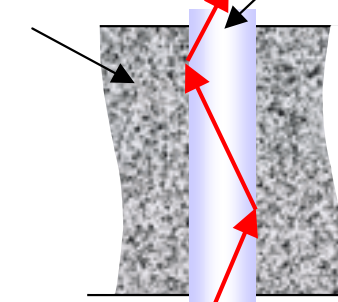


(Hochbaum et al., Nature 451 (2008), 163)



phonon
 $d > l_{mfp}^{ph}$

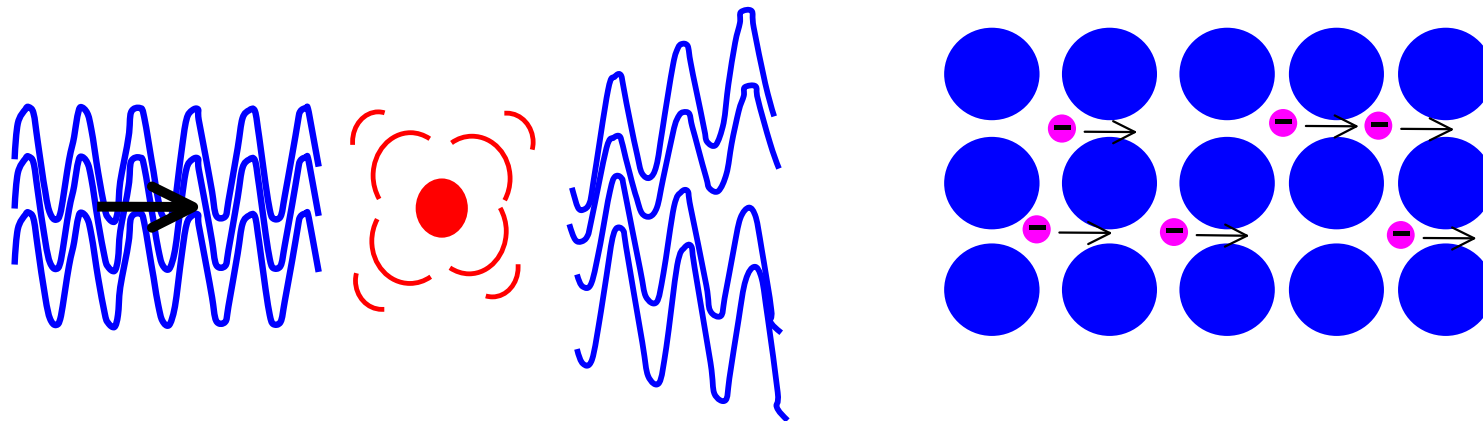
insulator conductor



electron
 $d < \lambda_{dB}^e$

Complex material science and advanced synthesis technology:-

Open structures and very complex crystal structures with many atoms with different mass in unit cell can \Leftrightarrow identify materials with a weak link between thermal and electric properties \Leftrightarrow **concept of «Phonon Glass Electron Crystal (called PGEC)»**, G. Slack, 1994.



« Phonon Glass » \rightarrow I_{phonon} very low
 λ_r very low

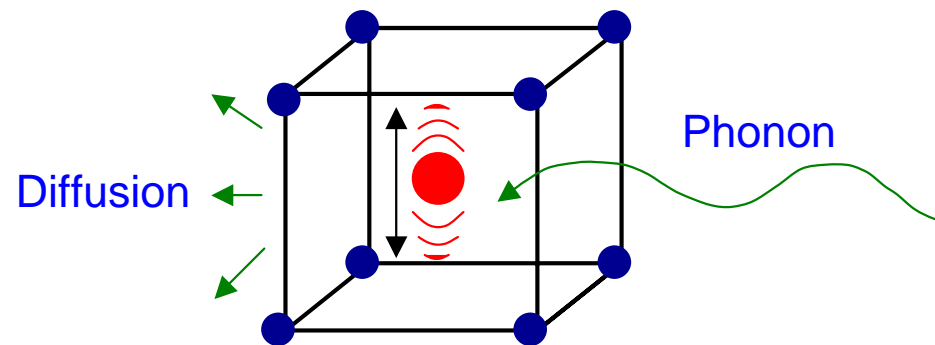
&

« Electron crystal » \rightarrow I_{electron} high
 μ also high

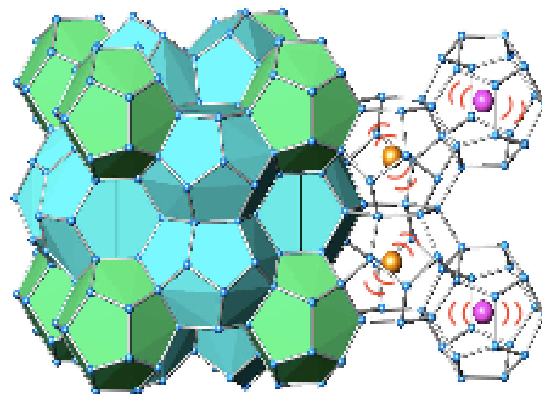
Open crystal structures : materials with « cages »

2

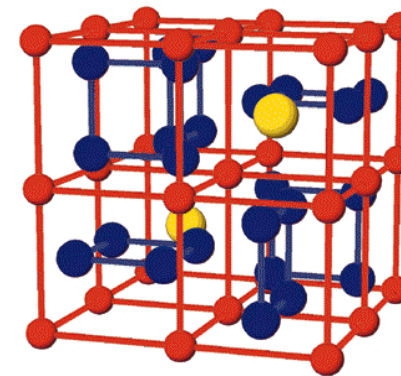
Materials with open crystallographic positions which can serve as efficient “host” for inserted atoms , only weakly bonded with basic structural frame → can vibrate around central position (« rattlers ») → heat carrying phonons experience thus important damping from these local Einstein modes....



Interesting materials...



Clathrates
($\text{Ba}_8\text{Ga}_{16}\text{Ge}_{30}$)



Skutterudites
($\text{Co}_4\text{Sb}_{12}$)

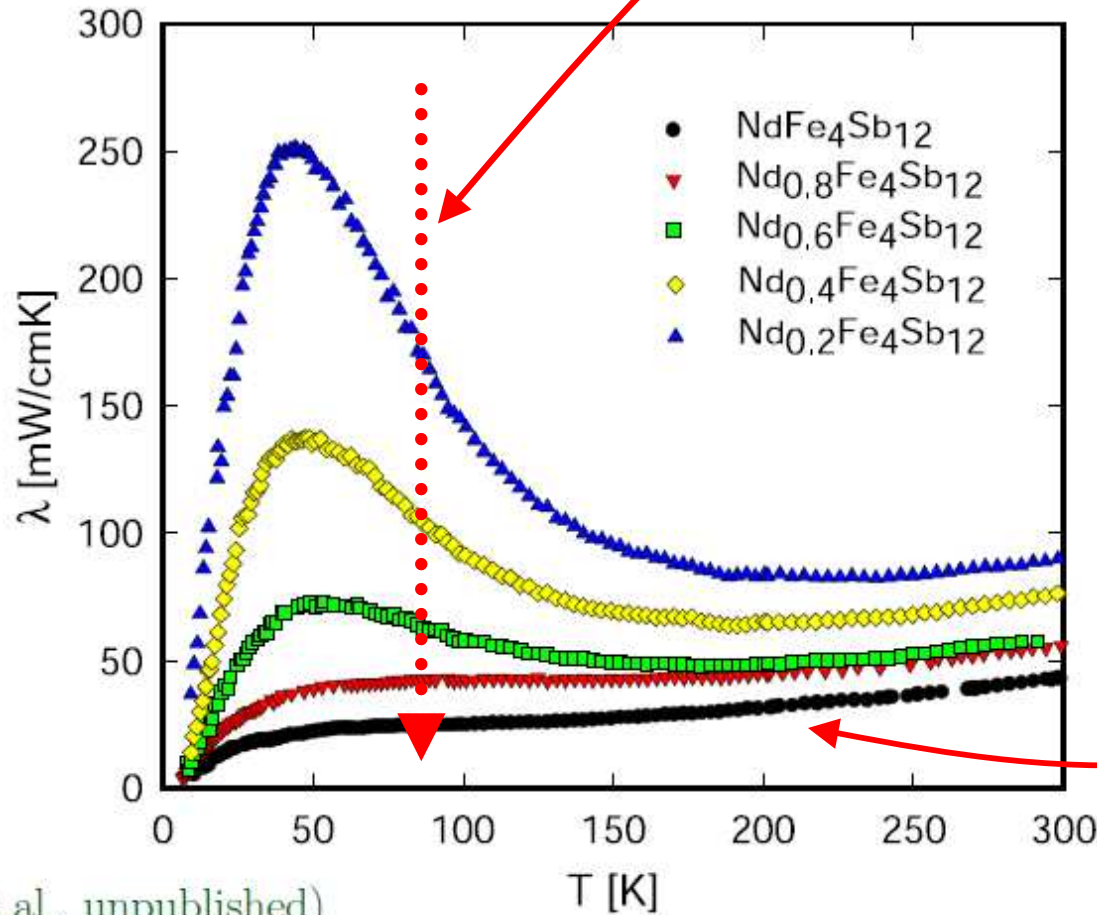
Decrease of thermal conductivity via phonon-phonon scattering

$$ZT = \frac{\alpha^2}{\rho\lambda} T$$

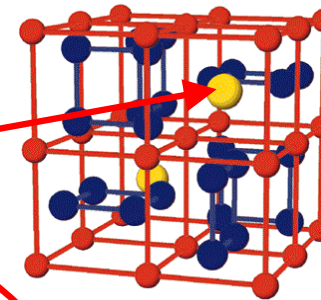
RATTLING ATOMS

“Phonon engineering” thermoelectrics

Internal nanostructuring: The skutterudite $\text{Nd}_y\text{Fe}_4\text{Sb}_{12}$

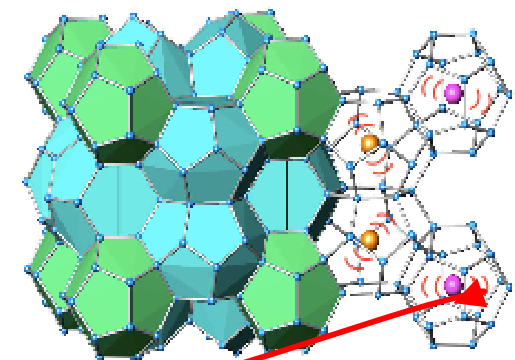
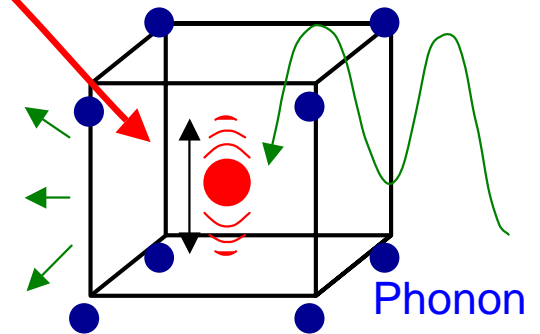


Skutterudites
($\text{Co}_4\text{Sb}_{12}$)



2

Scattering

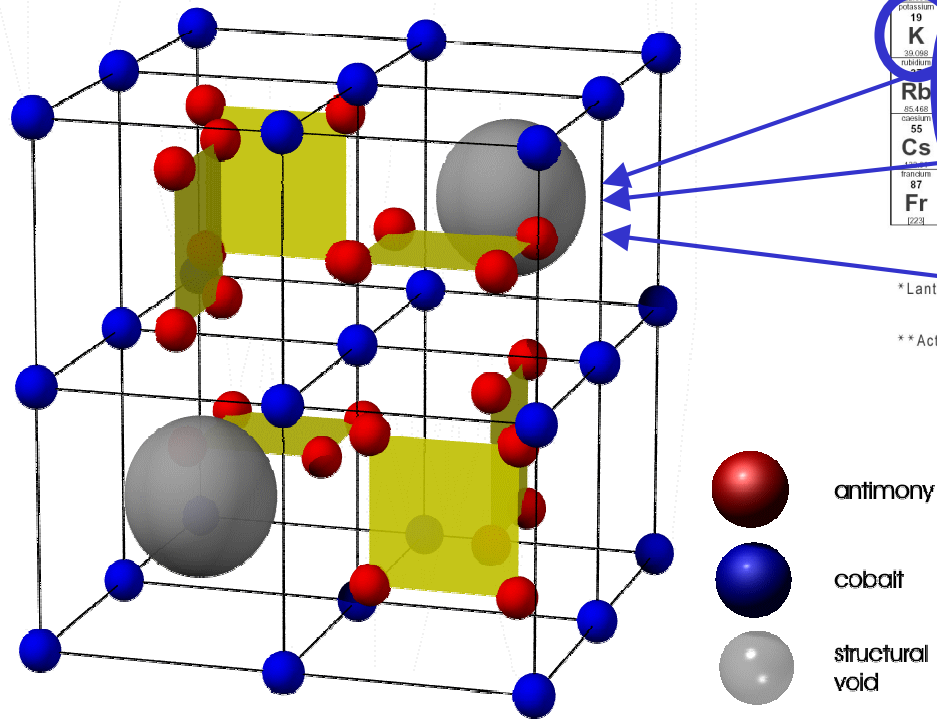


Clathrates
($\text{Ba}_8\text{Ga}_{16}\text{Ge}_{30}$)




16

Partially filled skutterudites based on $\text{Co}_4\text{Sb}_{12}$

2

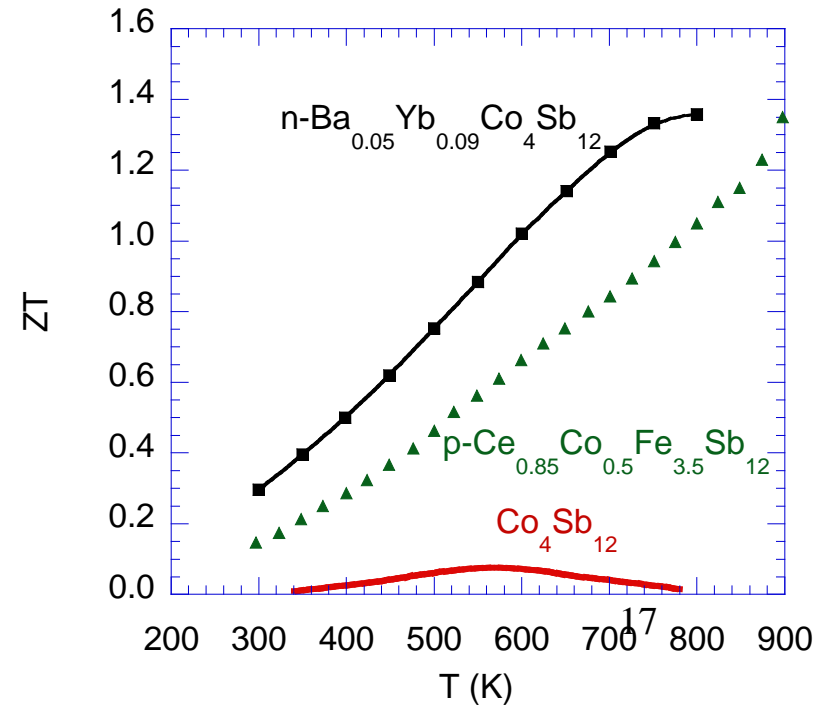


hydrogen 1 H 1.0079	helium 2 He 4.0026																	lithium 3 Li 6.941	beryllium 4 Be 9.0122											boron 5 B 10.811	carbon 6 C 12.011	nitrogen 7 N 14.007	oxygen 8 O 15.999	fluorine 9 F 18.998	neon 10 Ne 20.180
sodium 11 Na 22.990	magnesium 12 Mg 24.305											aluminum 13 Al 26.982	silicon 14 Si 28.086	phosphorus 15 P 30.974	sulfur 16 S 32.065	chlorine 17 Cl 35.453	argon 18 Ar 39.948																		
potassium 19 K 39.098	calcium 20 Ca 40.078											gallium 31 Ga 72.64	germanium 32 Ge 72.64	arsenic 33 As 74.922	selecnium 34 Se 78.96	bromine 35 Br 79.904	krypton 36 Kr 83.80																		
rubidium 37 Rb 85.468	strontium 38 Sr 87.62											indium 49 In 114.82	tin 50 Sn 118.71	antimony 51 Sb 121.76	tellurium 52 Te 127.60	iodine 53 I 126.90	xenon 54 Xe 131.29																		
cesium 55 Cs 132.91	barium 56 Ba 137.33	* 7-10	lanthanum 57 La 138.91	cerium 58 Ce 140.12	praseodymium 59 Pr 140.91	neodymium 60 Nd 144.24	promethium 61 Pm [144.91]	europium 62 Eu 151.96	gadolinium 63 Gd 157.25	terbium 64 Tb 158.93	dysprosium 65 Dy 162.50	holmium 66 Ho 164.93	erbium 67 Er 167.26	thulium 68 Tm 168.93	ytterbium 69 Yb 173.04	lutetium 70 Lu 174.967																			
francium 87 Fr [223]	radium 88 Ra [226]	** 89-102	actinium 89 Ac [227]	thorium 90 Th 232.04	protactinium 91 Pa 231.04	uranium 92 U 238.03	neptunium 93 Np [237]	plutonium 94 Pu [244]	americium 95 Am [243]	curium 96 Cm [247]	berkelium 97 Bk [247]	californium 98 Cf [251]	einsteinium 99 Es [252]	fermium 100 Fm [257]	mendelevium 101 Md [258]	nobelium 102 No [259]																			

 antimony
 cobalt
 structural void

Rich class of compounds, voids, rattling, filling, doping,...

Materials n et p with $ZT > 1$ can be obtained...



High Temperature Oxide Thermoelectrics

2

New class of compound, metallic oxides, stable chemically at high temperatures, studied are cobaltites and manganites, then chromites,..

- Layered cobaltites

- $\text{Ca}_3\text{Co}_4\text{O}_9$
- $(\text{Bi,Pb})_2\text{Sr}_2\text{Co}_{1.82}\text{O}_y$
- Na_xCoO_2

- 3D - cobaltites

- 2D - cuprates

- 3D - Manganites

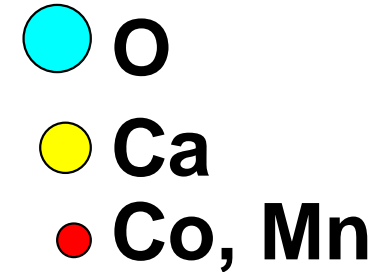
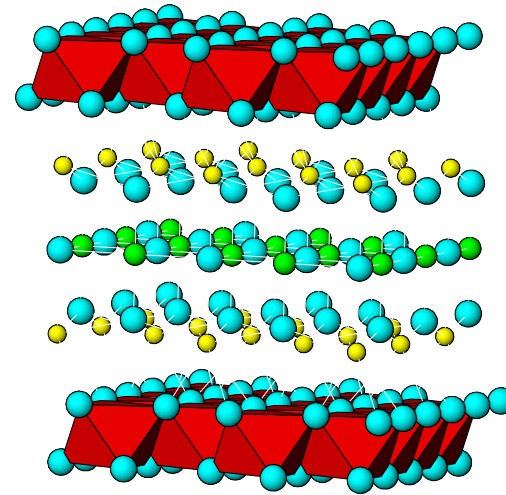
- $\text{Ca}_{0.95}\text{La}_{0.05}\text{MnO}_3$

- 3D - Titanates

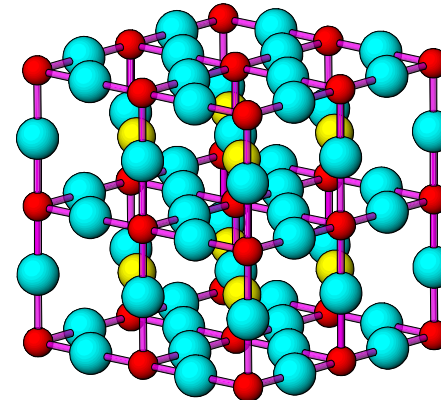
- $\text{Sr}_{0.95}\text{La}_{0.05}\text{TiO}_3$

- Spinels

$\alpha > 0$



$\alpha < 0$



Gradual increase of ZT during last 60 years...

