

Testing the Kerr-nature of black hole candidates

Cosimo Bambi
(LMU München & Fudan University)

6th FER0 Meeting
30 – 31 August 2012, Prague, Czech Republic



ARNOLD SOMMERFELD
CENTER FOR THEORETICAL PHYSICS



Plan of the talk

- **Introduction (motivations, theoretical and observational facts)**
- **Probing the geometry of the space-time around astrophysical black hole candidates (continuum-fitting method)**
- **Are jets powered by the black hole spin?**

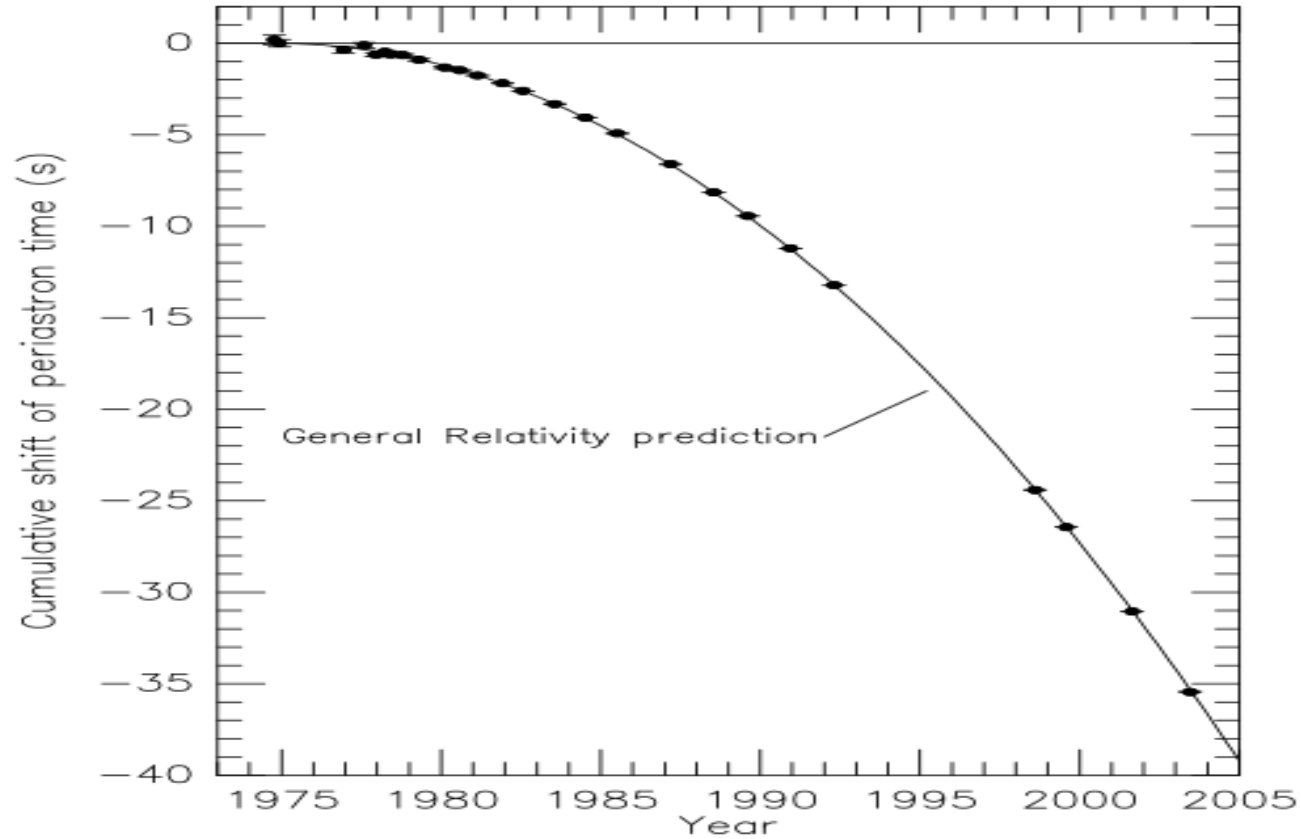
Introduction

- **Introduction**
- **Probing the geometry of the space-time around astrophysical black hole candidates**
- **Are jets powered by the black hole spin?**

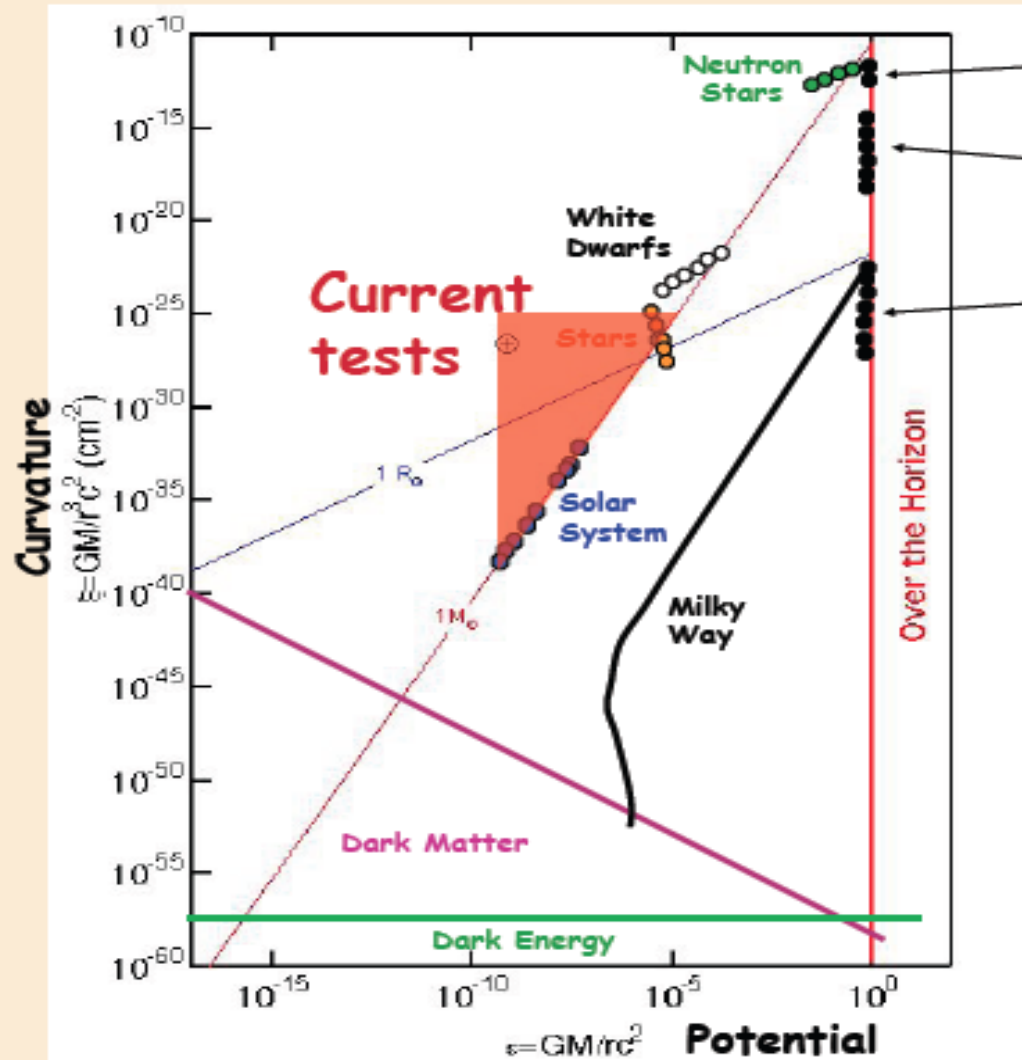
Tests of General Relativity

- **Earth's gravitational field:**
Lunar Laser Ranging experiments, Gravity Probe B, . . .
- **Solar System:**
Cassini mission, . . .
- **Observation of binary pulsars:**
PSR B1913+16, PSR J0737-3039, . . .

Orbital decay of PSR B1913+16



From Weisberg & Taylor 2005



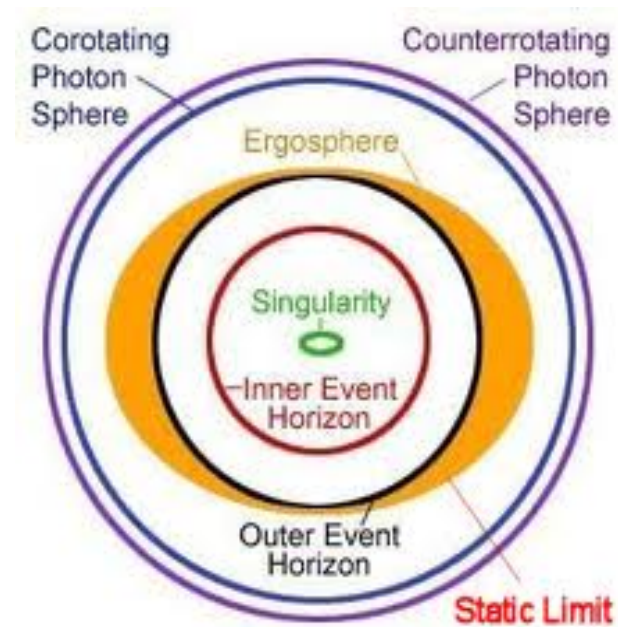
X-ray Binaries
 Intermediate Mass Black-Holes
 Active Galactic Nuclei

GRAVITATIONAL FIELDS IN ASTROPHYSICAL SYSTEMS

Psaltis 2008

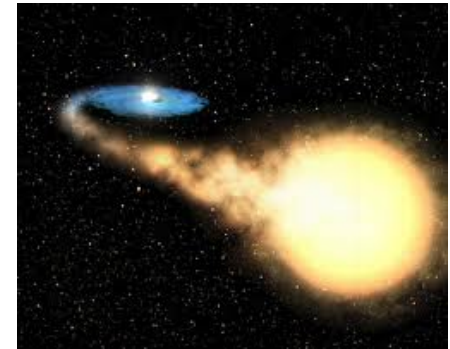
Black holes in GR (Theory)

- **Final product of the gravitational collapse → Black hole**
- **4D General Relativity → Kerr black hole**
- **Only 2 parameters: the mass M and the spin J ($a_* = J/M^2$)**
- **Kerr bound: $|a_*| < 1$**

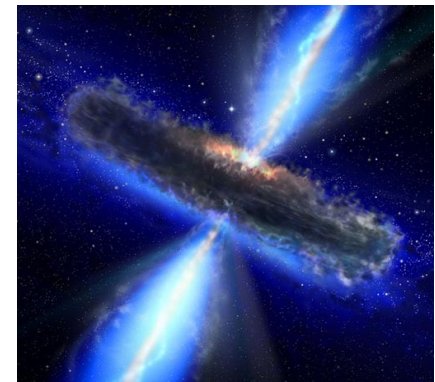


Black hole candidates (Observations)

- **Stellar-mass BH candidates in X-ray binary systems (5 – 20 Solar masses)** →



- **Super-massive BH candidates in galactic nuclei ($10^5 - 10^{10}$ Solar masses)** →



- **Intermediate-mass BH candidates in ULXS ($10^2 - 10^4$ Solar masses?)** →



Stellar-mass BH candidates

- **Dark objects in X-ray binary systems**

- **Mass function:**
$$f(M_{BH}) = \frac{K^3 T}{2\pi G_N} = \frac{M_{BH}^3 \sin^3 i}{(M_{BH} + M_c)^2} \quad K = v \sin i$$

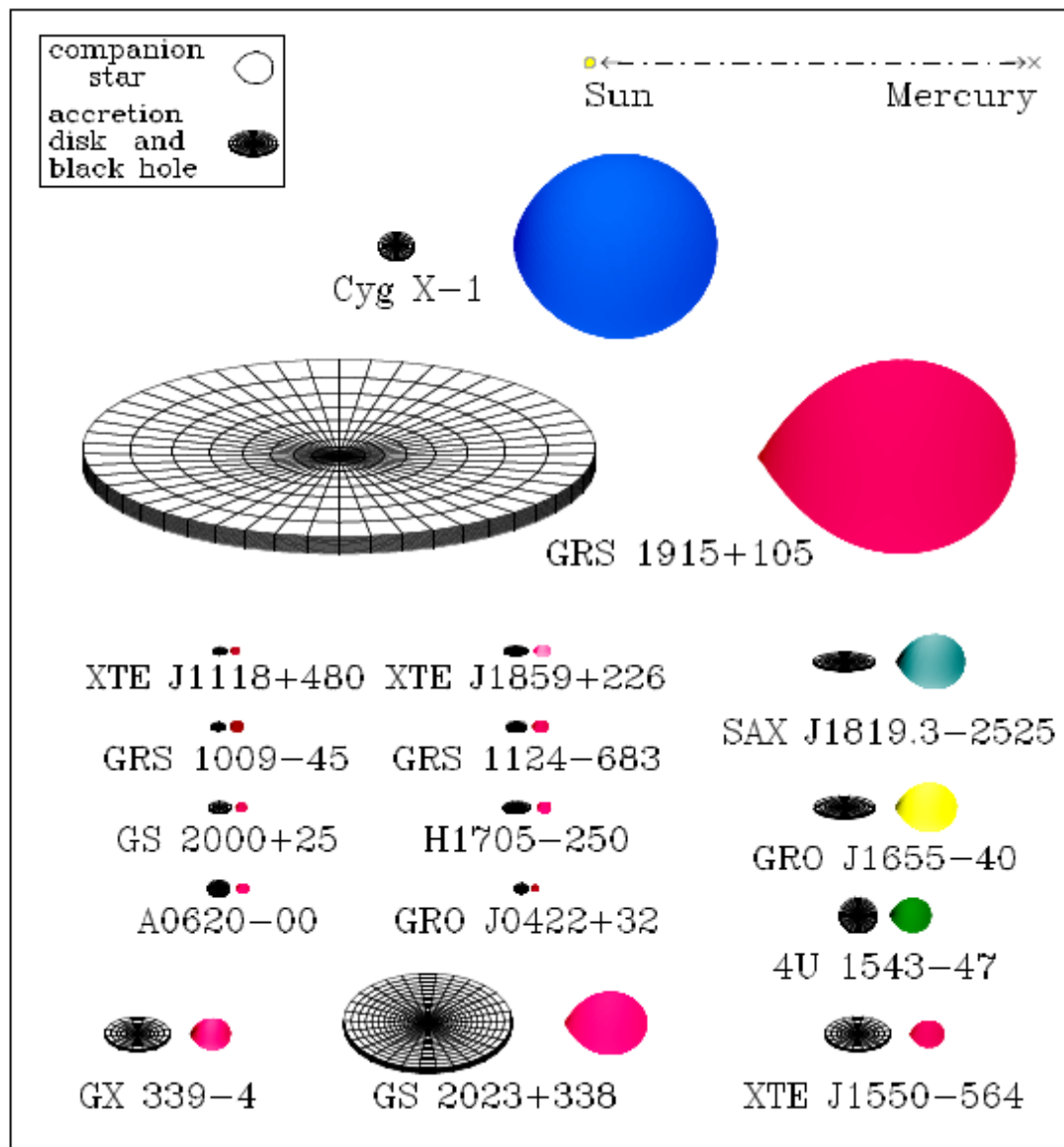
- **In general, a good estimate of M_c and i is necessary**

- **Maximum mass for relativistic stars about 3 Solar masses (see Rhoades & Ruffini 1974 and Kalogera & Baym 1996)**

Coordinate Name	Common Name/Prefix	Year	Spec.	P _{orb} (hr)	f(M) (M _⊙)	M ₁ (M _⊙)
0422+32	(GRO J)	1992/1	M2V	5.1	1.19±0.02	3.7–5.0
0538–641	LMC X–3	–	B3V	40.9	2.3±0.3	5.9–9.2
0540–697	LMC X–1	–	O7III	93.8 ^d	0.13±0.05 ^d	4.0–10.0: ^e
0620–003	(A)	1975/1 ^f	K4V	7.8	2.72±0.06	8.7–12.9
1009–45	(GRS)	1993/1	K7/M0V	6.8	3.17±0.12	3.6–4.7: ^e
1118+480	(XTE J)	2000/2	K5/M0V	4.1	6.1±0.3	6.5–7.2
1124–684	Nova Mus 91	1991/1	K3/K5V	10.4	3.01±0.15	6.5–8.2
1354–64 ^g	(GS)	1987/2	GIV	61.1 ^g	5.75±0.30	–
1543–475	(4U)	1971/4	A2V	26.8	0.25±0.01	8.4–10.4
1550–564	(XTE J)	1998/5	G8/K8IV	37.0	6.86±0.71	8.4–10.8
1650–500 ^h	(XTE J)	2001/1	K4V	7.7	2.73±0.56	–
1655–40	(GRO J)	1994/3	F3/F5IV	62.9	2.73±0.09	6.0–6.6
1659–487	GX 339–4	1972/10 ⁱ	–	42.1 ^{j,k}	5.8±0.5	–
1705–250	Nova Oph 77	1977/1	K3/7V	12.5	4.86±0.13	5.6–8.3
1819.3–2525	V4641 Sgr	1999/4	B9III	67.6	3.13±0.13	6.8–7.4
1859+226	(XTE J)	1999/1	–	9.2: ^e	7.4±1.1: ^e	7.6–12.0: ^e
1915+105	(GRS)	1992/Q ^l	K/MIII	804.0	9.5±3.0	10.0–18.0
1956+350	Cyg X–1	–	O9.7Iab	134.4	0.244±0.005	6.8–13.3
2000+251	(GS)	1988/1	K3/K7V	8.3	5.01±0.12	7.1–7.8
2023+338	V404 Cyg	1989/1 ^f	K0III	155.3	6.08±0.06	10.1–13.4

From Remillard & McClintock 2006

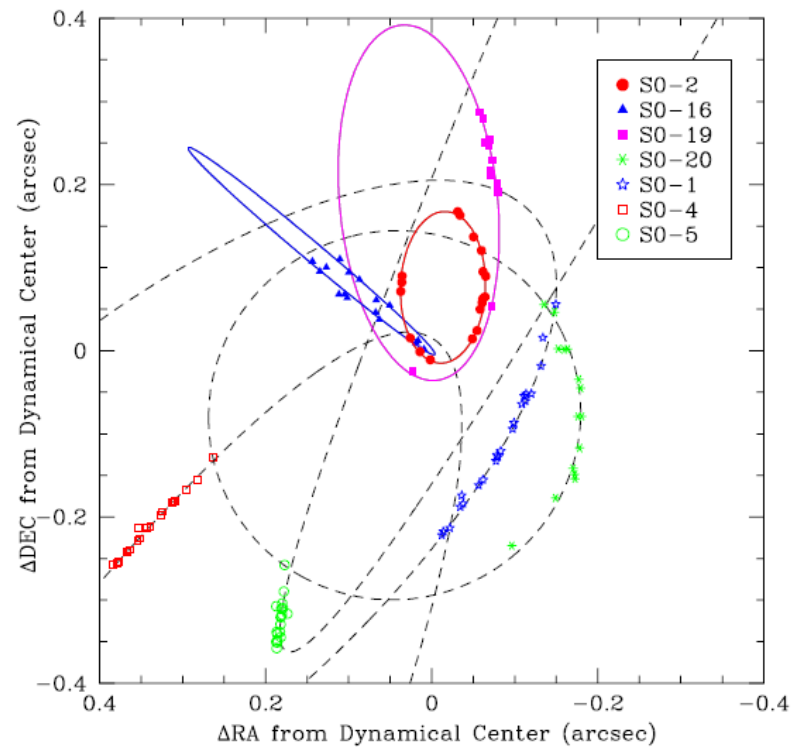
Black Hole Binaries in the Milky Way



From Remillard & McClintock 2006

Super-massive BH candidate in the Galaxy

- We study the orbital motion of individual stars
- Point-like central object with a mass of 4×10^6 Solar masses
- Radius < 45 AU ($600 R_{\text{Sch}}$)



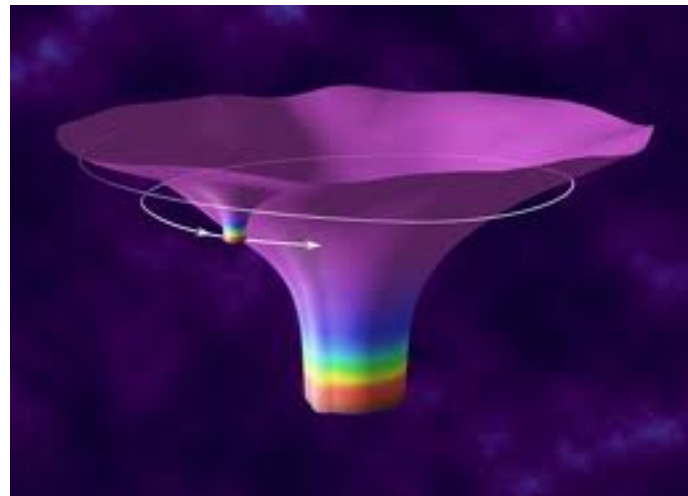
From Ghez et al., ApJ 620 (2005) 744

Probing the geometry of the space-time around astrophysical black hole candidates

- Introduction
- **Probing the geometry of the space-time around astrophysical black hole candidates**
- Are jets powered by the black hole spin?

Testing the Kerr BH Hypothesis with EMRIs

- **EMRI = Extreme Mass Ratio Inspiral**
- **LISA will be able to observe about $10^4 - 10^6$ cycles of GWs emitted by an EMRI while the stellar-mass body is in the strong field region of the super-massive object**
- **The quadrupole moment of the super-massive object can be measured with a precision at the level of $10^{-2} - 10^{-4}$**



Testing the Kerr BH Hypothesis with the radiation emitted by the gas of accretion

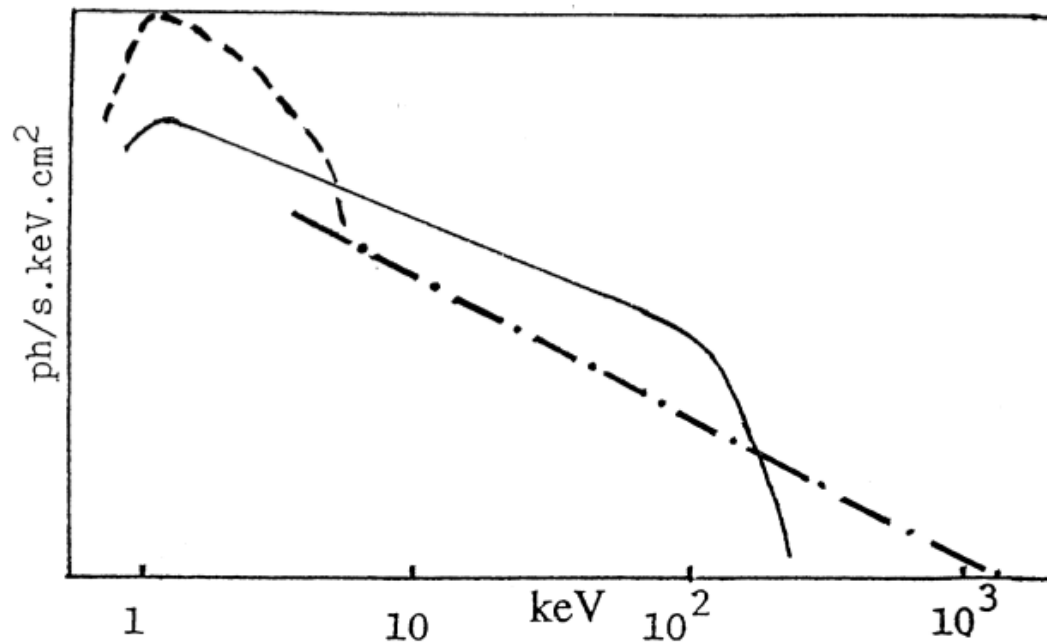
- **Significant progresses in the last ~ 5 years in the understanding of the electromagnetic spectrum of BH candidates**
- **Spin measurements:**
 - **Continuum-fitting method (stellar-mass BH candidates)**
 - **Relativistic iron line (both stellar-mass and super-massive BH candidates)**

Some data are already available and more data will be available in a near future

- **High-frequency QPOs**
- **New VLBI experiments with unprecedented high-resolution imaging capabilities**

Continuum-fitting method

- The soft X-ray component of the spectrum of **stellar-mass** BH candidates is the thermal spectrum of a geometrically thin and optically thick accretion disk



Novikov-Thorne Model

- **Geometrically thin and optically thick accretion disk**
- **Relativistic generalization of the Shakura-Sunyaev model**

Assumptions:

- **Disk on the equatorial plane**
- **Gas's particles move on nearly geodesic circular orbits**
- **No magnetic fields**
- **No heat advection; energy radiated from the disk surface**
- **Inner edge of the disk at the ISCO, where stresses vanish**

→ **Efficiency = $1 - E_{\text{ISCO}}$**

Novikov-Thorne Model

- **Geometrically thin and optically thick accretion disk**
- **Relativistic generalization of the Shakura-Sunyaev model**

Assumptions:

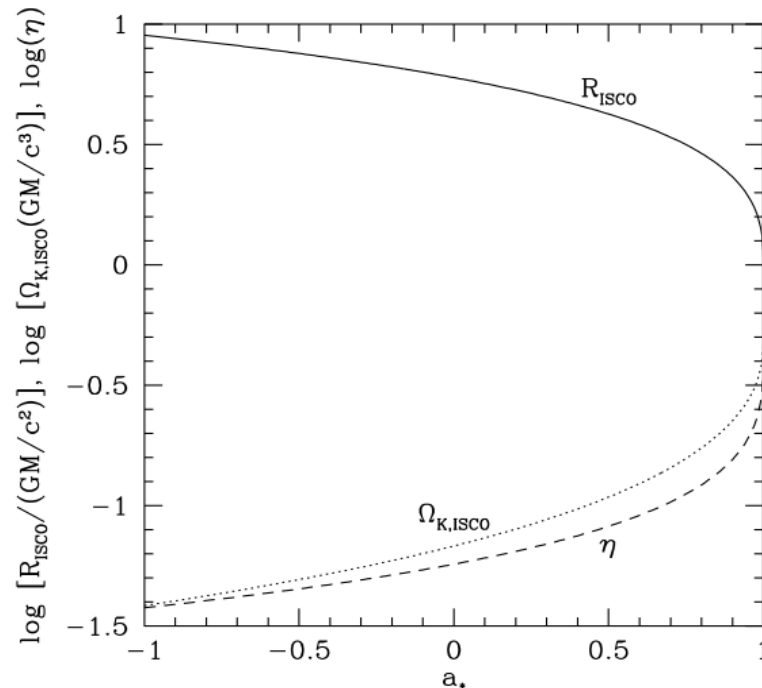
- **Disk on the equatorial plane**
- **Gas's particles move on nearly geodesic circular orbits**
- **No magnetic fields**
- **No heat advection; energy radiated from the disk surface**
- **Inner edge of the disk at the ISCO, where stresses vanish**

→ **Efficiency = $1 - E_{\text{ISCO}}$**

Selection criterion:
 $0.08 L_{\text{EDD}} < L < 0.30 L_{\text{EDD}}$

Continuum-fitting method in Kerr background

- 5 parameters (BH mass, BH spin, BH distance, viewing angle, mass accretion rate)
- BH mass, BH distance, viewing angle \rightarrow BH spin, mass accretion rate



Spin measurements from the Harvard group

Black Hole	Spin a_*	Reference
GRS 1915+105	> 0.98	McClintock et al. 2006
Cygnus X-1	> 0.97	Gou et al. 2011
LMC X-1	0.92 ± 0.06	Gou et al. 2009
M33 X-7	0.84 ± 0.05	Liu et al. 2008, 2010
4U 1543-47	0.80 ± 0.05	Shafee et al. 2006
GRO J1655-40	0.70 ± 0.05	Shafee et al. 2006
XTE J1550-564	0.34 ± 0.24	Steiner et al. 2011
LMC X-3	< 0.3	Davis et al. 2006
A0620-00	0.12 ± 0.18	Gou et al. 2009

Testing the Kerr BH Hypothesis

- **To test the Kerr-nature of an astrophysical black hole candidates we need to consider a more general background, which includes the Kerr solution as special case**
- **In addition to the mass and the spin, the compact object will be characterized by one or more “deformation parameters”, measuring possible deformations from the Kerr geometry**
- **The Kerr black hole hypothesis is verified if observations require vanishing deformation parameters**

Johannsen-Psaltis metric

$$ds^2 = - \left(1 - \frac{2Mr}{\Sigma}\right) (1 + h) dt^2 + \frac{\Sigma(1 + h)}{\Delta + a^2 h \sin^2 \theta} dr^2 + \Sigma d\theta^2 - \frac{4aMr \sin^2 \theta}{\Sigma} (1 + h) dt d\phi + \left[\sin^2 \theta \left(r^2 + a^2 + \frac{2a^2 Mr \sin^2 \theta}{\Sigma} \right) + \frac{a^2 (\Sigma + 2Mr) \sin^4 \theta}{\Sigma} h \right] d\phi^2,$$

$$\Sigma = r^2 + a^2 \cos^2 \theta,$$

$$\Delta = r^2 - 2Mr + a^2,$$

$$h = \sum_{k=0}^{\infty} \left(\epsilon_{2k} + \frac{Mr}{\Sigma} \epsilon_{2k+1} \right) \left(\frac{M^2}{\Sigma} \right)^k$$

Basic features of the code

- **Geometry of the background:**

Johannsen-Psaltis space-time (Johannsen & Psaltis 2011) with three free parameters – mass, spin parameter, deformation parameter. No restrictions on the values of the spin parameter and of the deformation parameter

- **Relativistic effects:**

All relativistic effects are included. Ray-tracing technique used

- **Self-irradiation: Not included**

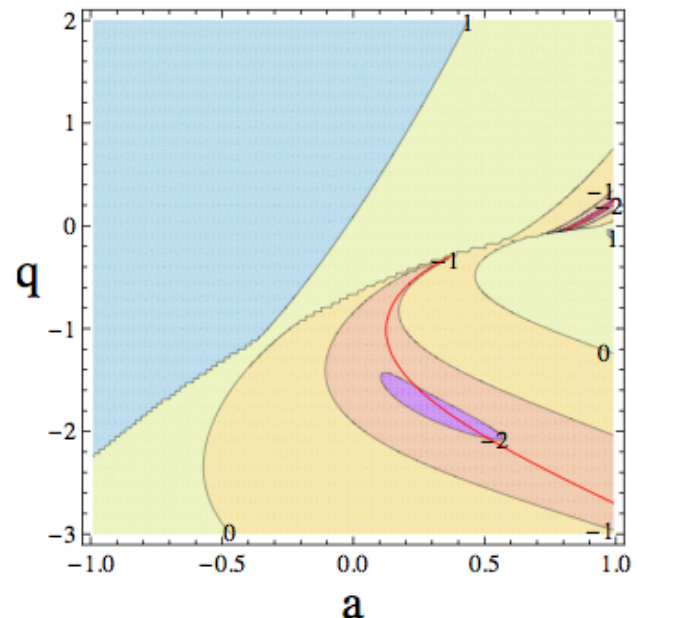
- **Non-zero torque at the inner edge of the disk: Not included**

- **Color factor: Constant. Set by the user**

- **Radiation emission: Isotropic or limb-darkened**

M33 X-7

- **X-ray binary system in the galaxy M33. Mass, distance from us, and inclination angle of the disk are known with good precision**
- **Chandra and XMM-Newton data in the high-soft state**
- **Spin parameter: 0.84 ± 0.05 (Liu et al. 2008, 2010)**
- **Allowed region in the spin parameter – deformation parameter plane: work in progress . . .**

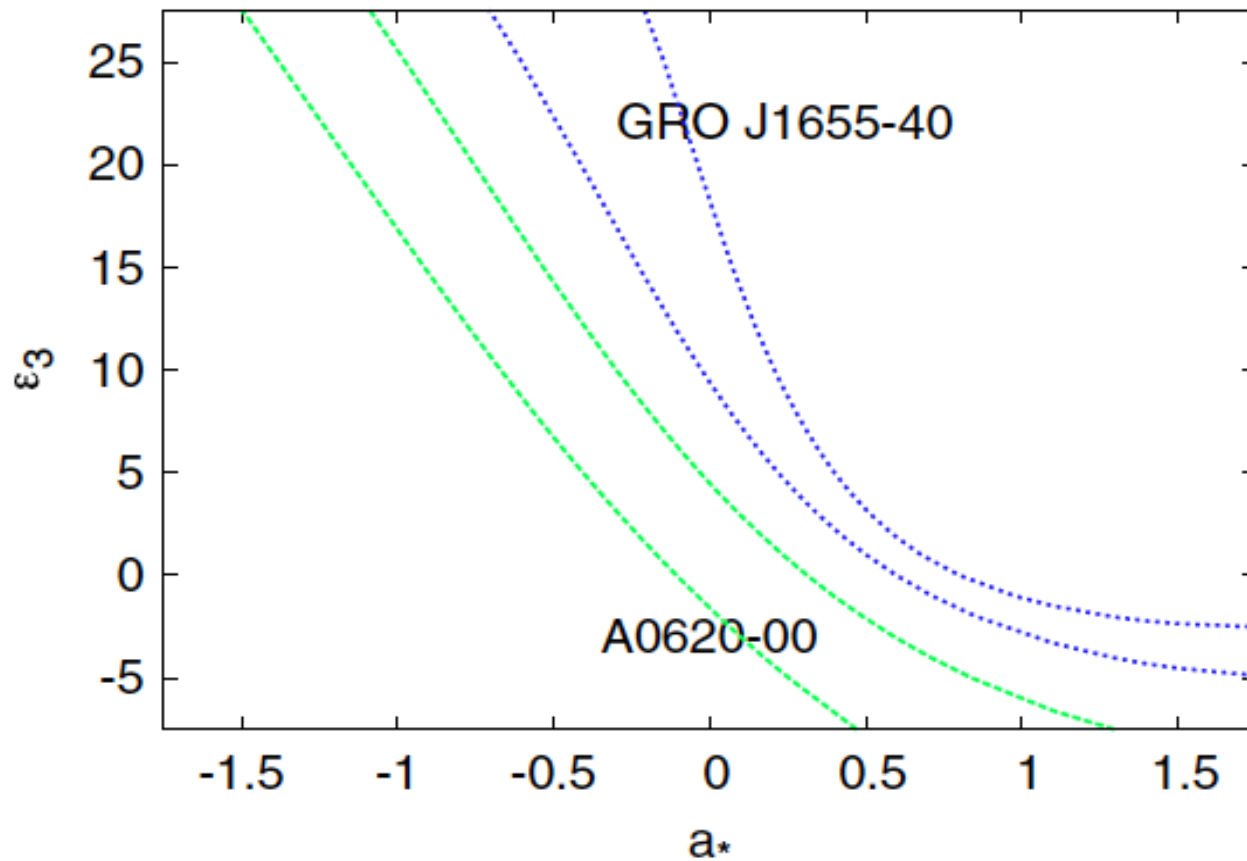


From Bambi & Barausse 2011

Spin parameter – Deformation parameter plane

- The continuum-fitting method measures the radiative efficiency:

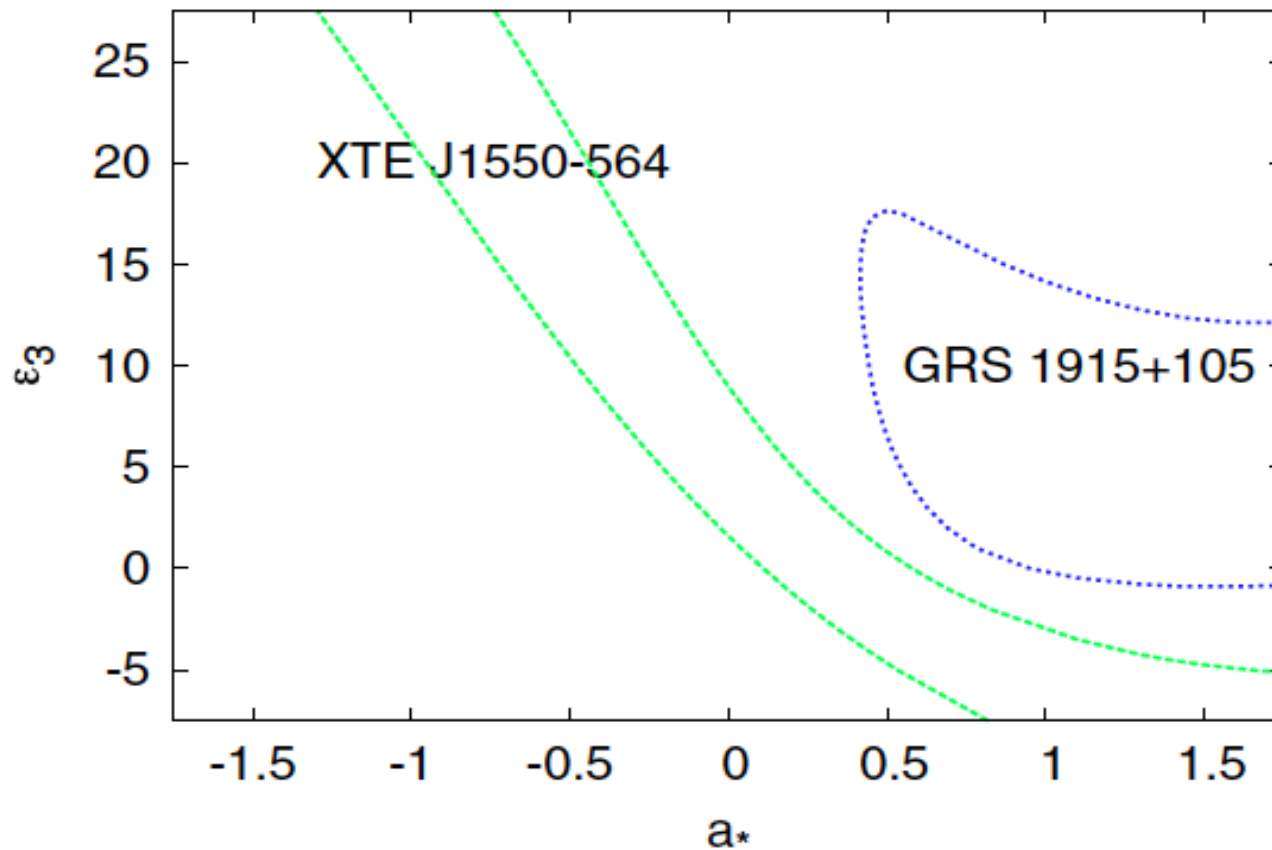
$$\text{Efficiency} = 1 - E_{\text{ISCO}}$$



Spin parameter – Deformation parameter plane

- The continuum-fitting method measures the radiative efficiency:

$$\text{Efficiency} = 1 - E_{\text{ISCO}}$$



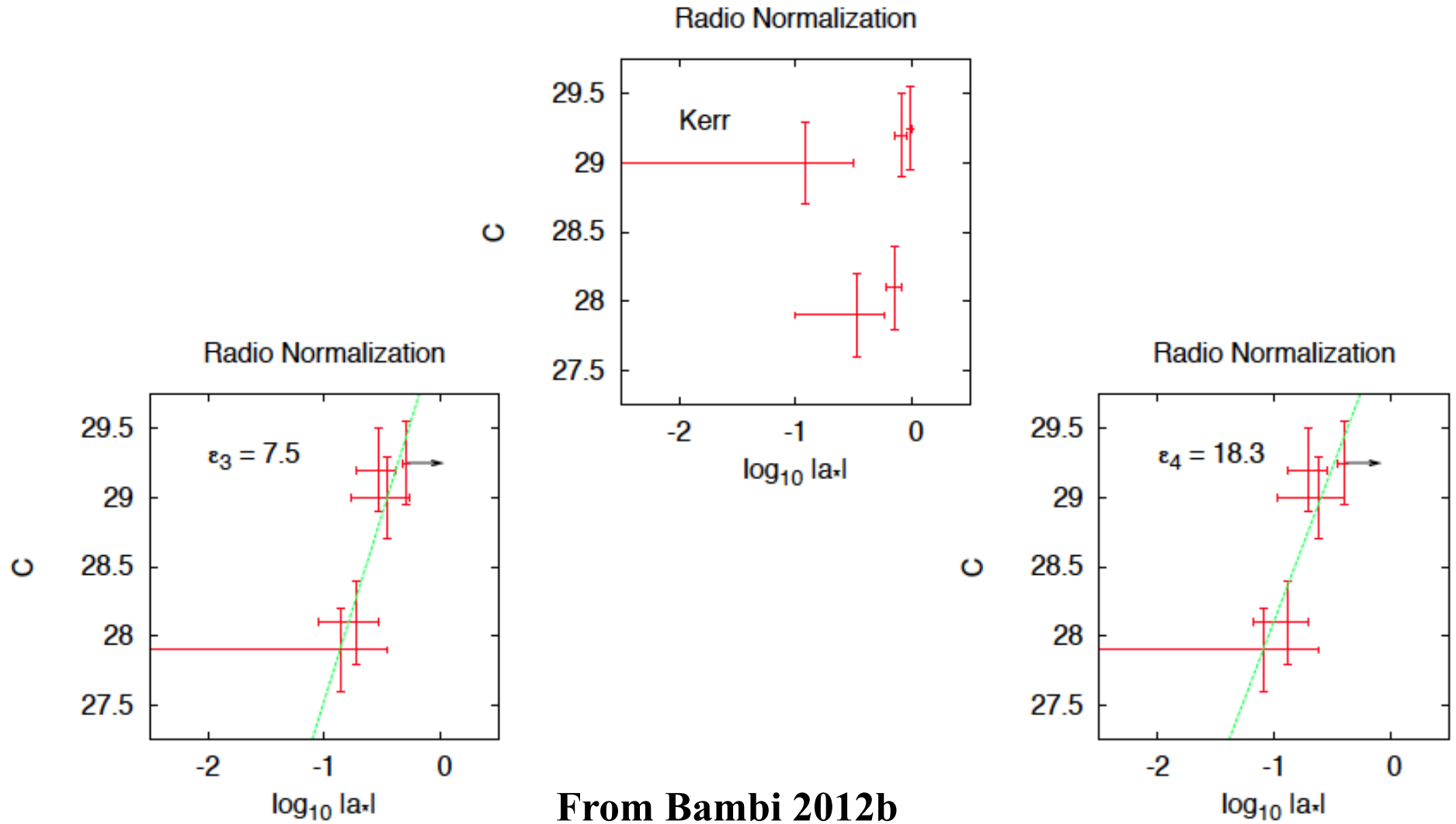
Are jets powered by the black hole spin?

- Introduction
- Probing the geometry of the space-time around astrophysical black hole candidates
- **Are jets powered by the black hole spin?**

Jets

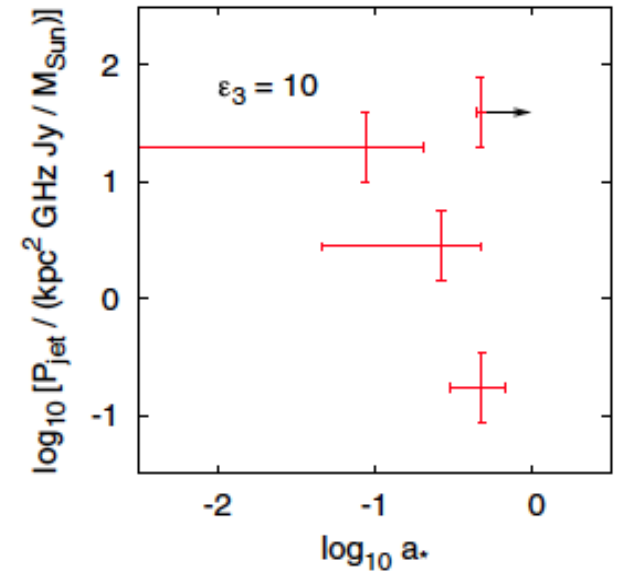
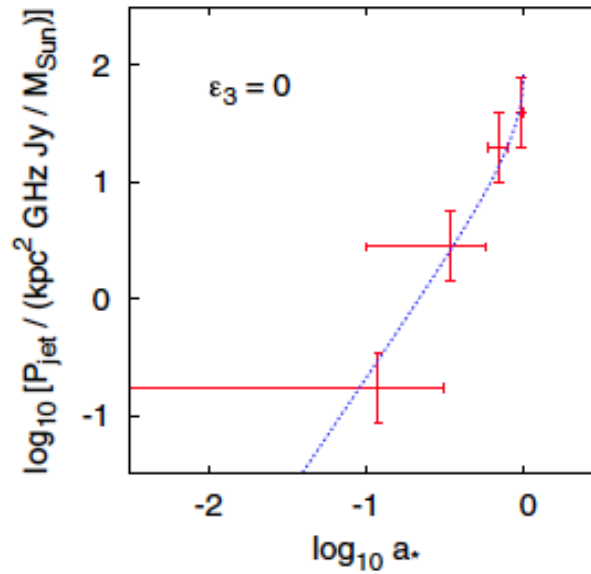
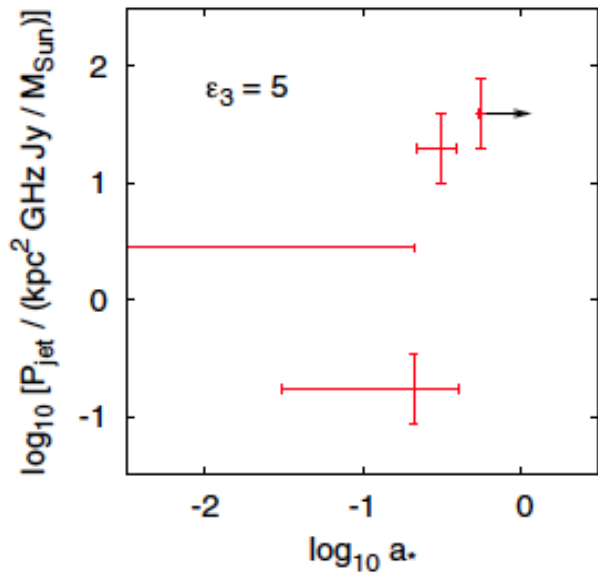
- **Jets are commonly produced by accreting BH candidates**
- **Two kinds of jets in the case of stellar-mass BH candidates: steady jets (in the hard state) and transient jets (usually when the source switches from the hard to the soft state)**
- **The exact mechanism producing these jets is not known**
- **For steady jets, a quite appealing scenario is the Blandford-Znajek mechanism, in which the jet is powered by the rotational energy of the BH**
- **No observational evidence for a correlation between jet power and BH spin (Fender, Gallo & Russell 2010)**
- **Claim of observational evidence for a correlation between power of transient jets and BH spin (Narayan & McClintock 2012)**

Steady jets



From Bambi 2012b

Transient jets



From Bambi 2012a

Conclusion

- **There is a body of observational evidence supporting the existence of dark and compact objects in the Galaxy and in the Universe. These objects are thought to be Kerr black holes**
- **The Kerr black hole hypothesis can be tested with the already available X-ray data by extending the continuum-fitting method to non-Kerr backgrounds**
- **One typically finds a degeneracy between the spin and the deformation parameter**
- **This degeneracy can be broken by adding another measurement (e.g. the power of steady/transient jets)**