

**Abstract:** The dynamic of three one dimensional non relativistic spinless quantum particles interacting through delta potentials is governed by the Hamiltonian

$$\sum_{i=1}^3 -\frac{\Delta_i}{2m_i} + \sum_{1 \leq i < j \leq 3} Z_i Z_j \delta(x_i - x_j) \quad \text{acting on} \quad \bigotimes_{i=1}^3 L^2(\mathbb{R})$$

where  $x_i \in \mathbb{R}$  denotes the position of the  $i^{\text{th}}$  particle,  $\Delta_i := \partial_{x_i}^2$ ,  $m_i > 0$ ,  $Z_i \in \mathbb{R}$  the mass and the charge of this  $i^{\text{th}}$  particle. The question we address is: for what values of the masses and the charges does this Hamiltonian possess a bound state, i.e. a discrete eigenvalue. We shall give a fairly complete picture in the particular case,  $m_1 = M > m_2 = m_3 = m$ ,  $Z_1 > 0$ ,  $Z_2 = Z_3 = -1$ . This case corresponds to a dynamical Helium-type of atom. Applications to the study of atoms in high magnetic field and to trions on carbon nanotube will be briefly reviewed. Despite the physical jargon, this will be a genuine mathematical seminar in spectral theory. This is the result of a collaboration with H. Cornean and B. Ricaud.